MOSEK Command Line Tools

Release 8.1.0.15(beta)

MOSEK ApS

2017

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CHAPTER

ONE

INTRODUCTION

The **MOSEK** Optimization Suite 8.1.0.15(beta) is a powerful software package capable of solving large-scale optimization problems of the following kind:

- linear,
- conic quadratic (also known as second-order cone),
- convex quadratic,
- semidefinite,
- and general convex.

Integer constrained variables are supported for all problem classes except for semidefinite and general convex problems. In order to obtain an overview of features in the **MOSEK** Optimization Suite consult the product introduction guide.

The most widespread class of optimization problems is *linear optimization problems*, where all relations are linear. The tremendous success of both applications and theory of linear optimization can be ascribed to the following factors:

- The required data are simple, i.e. just matrices and vectors.
- Convexity is guaranteed since the problem is convex by construction.
- Linear functions are trivially differentiable.
- There exist very efficient algorithms and software for solving linear problems.
- Duality properties for linear optimization are nice and simple.

Even if the linear optimization model is only an approximation to the true problem at hand, the advantages of linear optimization may outweigh the disadvantages. In some cases, however, the problem formulation is inherently nonlinear and a linear approximation is either intractable or inadequate. *Conic optimization* has proved to be a very expressive and powerful way to introduce nonlinearities, while preserving all the nice properties of linear optimization listed above.

The fundamental expression in linear optimization is a linear expression of the form

$$Ax - b \in \mathcal{K}$$

where $\mathcal{K} = \{y : y \geq 0\}$, i.e.,

$$\begin{aligned} Ax - b &= y, \\ y &\in \mathcal{K}. \end{aligned}$$

In conic optimization a wider class of convex sets $\mathcal{K}$ is allowed, for example in 3 dimensions $\mathcal{K}$ may correspond to an ice cream cone. The conic optimizer in **MOSEK** supports three structurally different types of cones $\mathcal{K}$, which allows a surprisingly large number of nonlinear relations to be modelled (as described in the **MOSEK** modeling cookbook), while preserving the nice algorithmic and theoretical properties of linear optimization.

1.1 Why the Command Line Tools?

The **MOSEK** capabilities can be accessed from the command line without the need to use any programming language. The user can input optimization problems using files in a variety of *formats*, or via the AMPL language shell.

The Command Line Tools provides access to:

- Linear Optimization (LO)
- Conic Quadratic (Second-Order Cone) Optimization (CQO, SOCO)
- Convex Quadratic and Quadratically Constrained Optimization (QCQO)
- Semidefinite Optimization (SDO)
- General Convex Optimization problems (via AMPL).

as well as to additional utilities for:

- problem analysis,
- sensitivity analysis,
- infeasibility diagnostics.

CHAPTER

TWO

CONTACT INFORMATION

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Website	mosek.com	
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	support@mosek.com	Technical support, questions and bug reports
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Mailing Address		
	MOSEK ApS	
	Fruebjergvej 3	
	Symbion Science Park, Box 16	
	2100 Copenhagen O	
	Denmark	

You can get in touch with **MOSEK** using popular social media as well:

Blogger	http://blog.mosek.com/
Google Group	https://groups.google.com/forum/#!forum/mosek
Twitter	https://twitter.com/mosektw
Google+	https://plus.google.com/+Mosek/posts
Linkedin	https://www.linkedin.com/company/mosek-aps

In particular **Twitter** is used for news, updates and release announcements.

CHAPTER

THREE

LICENSE AGREEMENT

Before using the **MOSEK** software, please read the license agreement available in the distribution at `<MSKHOME>/mosek/8/mosek-eula.pdf` or on the **MOSEK** website https://mosek.com/sales/license-agreement.

MOSEK uses some third-party open-source libraries. Their license details follows.

zlib

MOSEK includes the *zlib* library obtained from the zlib website. The license agreement for *zlib* is shown in Listing 3.1.

Listing 3.1: *zlib* license.

```
zlib.h -- interface of the 'zlib' general purpose compression library
version 1.2.7, May 2nd, 2012

Copyright (C) 1995-2012 Jean-loup Gailly and Mark Adler

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   misrepresented as being the original software.
3. This notice may not be removed or altered from any source distribution.

Jean-loup Gailly        Mark Adler
jloup@gzip.org          madler@alumni.caltech.edu
```

fplib

MOSEK includes the floating point formatting library developed by David M. Gay obtained from the netlib website. The license agreement for *fplib* is shown in Listing 3.2.

Listing 3.2: *fplib* license.

```
/****************************************************************
 *
```

```
* The author of this software is David M. Gay.
*
* Copyright (c) 1991, 2000, 2001 by Lucent Technologies.
*
* Permission to use, copy, modify, and distribute this software for any
* purpose without fee is hereby granted, provided that this entire notice
* is included in all copies of any software which is or includes a copy
* or modification of this software and in all copies of the supporting
* documentation for such software.
*
* THIS SOFTWARE IS BEING PROVIDED "AS IS", WITHOUT ANY EXPRESS OR IMPLIED
* WARRANTY.  IN PARTICULAR, NEITHER THE AUTHOR NOR LUCENT MAKES ANY
* REPRESENTATION OR WARRANTY OF ANY KIND CONCERNING THE MERCHANTABILITY
* OF THIS SOFTWARE OR ITS FITNESS FOR ANY PARTICULAR PURPOSE.
*
***************************************************************/
```

CHAPTER

FOUR

INSTALLATION

In this section we discuss how to install and setup the **MOSEK** Command Line Tools.

Important: Before running this **MOSEK** interface please make sure that you:

- Installed **MOSEK** correctly. Some operating systems require extra steps. See the Installation guide for instructions and common troubleshooting tips.
- Set up a license. See the Licensing guide for instructions.

Locating Files

The files in Command Line Tools are organized as reported in Table 4.1.

Table 4.1: Relevant files for the Command Line Tools.

Relative Path	Description	Label
`<MSKHOME>/mosek/8/tools/platform/<PLATFORM>/bin`	Binaries	`<BINDIR>`
`<MSKHOME>/mosek/8/tools/platform/<PLATFORM>/bin/mosek`	Mosek executable	
`<MSKHOME>/mosek/8/tools/examples/data`	Examples	`<EXDIR>`

where

- `<MSKHOME>` is the folder in which the **MOSEK** package has been installed,
- `<PLATFORM>` is the actual platform among those supported by **MOSEK**, i.e. `win32x86`, `win64x86`, `linux64x86` or `osx64x86`.

Setting up paths

The executable file is ready for use. It may be convenient to add the directory `<BINDIR>` to the environment variable `PATH`, and then **MOSEK** can simply be used by typing

```
mosek
```

in the command line.

4.1 Testing the installation

To test that Command Line Tools has been installed correctly go to the examples directory `<EXDIR>` and run **MOSEK** on any of the input files, for example `lo1.mps`:

```
mosek lo1.mps
```

Is should produce output similar to:

```
MOSEK Version 8.0.0.53 (Build date: 2017-1-12 22:21:45)
Copyright (c) MOSEK ApS, Denmark. WWW: mosek.com
Platform: Linux/64-X86

Open file 'lo1.mps'
Reading started.

[....]

Optimizer started.
Interior-point optimizer started.

[....]

Interior-point solution summary
  Problem status  : PRIMAL_AND_DUAL_FEASIBLE
  Solution status : OPTIMAL
  Primal.  obj: 8.3333333280e+01    nrm: 5e+01    Viol.  con: 1e-08    var: 0e+00
  Dual.    obj: 8.3333333242e+01    nrm: 4e+00    Viol.  con: 2e-10    var: 5e-09

Basic solution summary
  Problem status  : PRIMAL_AND_DUAL_FEASIBLE
  Solution status : OPTIMAL
  Primal.  obj: 8.3333333333e+01    nrm: 5e+01    Viol.  con: 7e-15    var: 0e+00
  Dual.    obj: 8.3333333245e+01    nrm: 4e+00    Viol.  con: 2e-10    var: 5e-09

[....]

Open file 'lo1.sol'
Start writing.
done writing. Time: 0.00

Open file 'lo1.bas'
Start writing.
done writing. Time: 0.00

Return code - 0  [MSK_RES_OK]
```

CHAPTER

FIVE

THE COMMAND LINE TOOL

5.1 Introduction

The **MOSEK** command line tool is used to solve optimization problems from the operating system command line. It is invoked as follows

```
mosek [options] [filename]
```

where both `[options]` and `[filename]` are optional arguments:

- `[options]` consists of command line arguments that modify the behavior of **MOSEK**. They are listed in Section *5.3*.
- `filename` is a file describing the optimization problem. The **MOSEK** command line accepts files in any of the *supported file formats* or in the AMPL *nl* file.

If no arguments are given, **MOSEK** will return its version and platform, i.e.

```
andrea@Bistrup:~$ mosek/8/tools/platform/linux64x86/bin/mosek

MOSEK Version 8.0.0.32(BETA) (Build date: 2016-7-12 10:29:26)
Copyright (c) MOSEK ApS, Denmark. WWW: mosek.com
Platform: Linux/64-X86


*** No input file specified. No optimization is performed.

Return code - 0  [MSK_RES_OK]
```

5.2 Command Line Example

In this section there are some examples on how to use the **MOSEK** command line. Please refer to Section *5.3* for the complete list of available command line options.

5.2.1 Solve an Optimization Problem

The simplest case is to solve a problem stored in file, say `lo1.mps`:

```
mosek lo1.mps
```

The solver will

- read `lo1.mps` from disk,
- solve the problem and
- store the relevant solution files (see *14.8*) if any solution exists.

These steps are clear from the solver output in the following listing.

```
MOSEK Version 8.0.0.34(BETA) (Build date: 2016-8-24 00:51:13)
Copyright (c) MOSEK ApS, Denmark. WWW: mosek.com
Platform: Linux/64-X86

Open file '/home/andrea/mosek/8/tools/examples/data/lo1.mps'
Reading started.
Using 'obj' as objective vector
Read 13 number of A nonzeros in 0.00 seconds.
Using 'rhs' as rhs vector
Using 'bound' as bound vector
Reading terminated. Time: 0.00

Read summary
  Type              : LO (linear optimization problem)
  Objective sense   : max
  Scalar variables : 4
  Matrix variables : 0
  Constraints       : 3
  Cones             : 0
  Time              : 0.0

Problem
  Name                   : lo1
  Objective sense        : max
  Type                   : LO (linear optimization problem)
  Constraints            : 3
  Cones                  : 0
  Scalar variables       : 4
  Matrix variables       : 0
  Integer variables      : 0

Optimizer started.
Interior-point optimizer started.
Presolve started.
Linear dependency checker started.
Linear dependency checker terminated.
Eliminator started.
Freed constraints in eliminator : 0
Eliminator terminated.
Eliminator - tries                  : 1                 time                   : 0.00
Lin. dep.  - tries                  : 1                 time                   : 0.00
Lin. dep.  - number                 : 0
Presolve terminated. Time: 0.00
Optimizer  - threads                : 2
Optimizer  - solved problem         : the primal
Optimizer  - Constraints            : 3
Optimizer  - Cones                  : 0
Optimizer  - Scalar variables       : 6                 conic                  : 0
Optimizer  - Semi-definite variables: 0                 scalarized             : 0
Factor     - setup time             : 0.00              dense det. time        : 0.00
Factor     - ML order time          : 0.00              GP order time          : 0.00
Factor     - nonzeros before factor : 6                 after factor           : 6
Factor     - dense dim.             : 0                 flops                  : 1.06e+02
ITE PFEAS    DFEAS    GFEAS    PRSTATUS   POBJ              DOBJ              MU       TIME
0   8.0e+00  3.2e+00  3.5e+00  1.00e+00   1.000000000e+01   0.000000000e+00   1.0e+00  0.01
1   4.2e+00  2.5e+00  4.7e-01  0.00e+00   3.093970927e+01   2.766058702e+01   2.6e+00  0.01
2   4.2e-01  2.5e-01  4.6e-02  -1.82e-02  6.511676243e+01   6.308843559e+01   2.6e-01  0.01
3   3.6e-02  2.1e-02  3.9e-03  5.84e-01   8.096141239e+01   8.061962333e+01   2.2e-02  0.01
4   1.5e-05  9.1e-06  1.7e-06  9.43e-01   8.333280389e+01   8.333241803e+01   9.2e-06  0.01
5   1.5e-09  9.1e-10  1.7e-10  1.00e+00   8.333333328e+01   8.333333324e+01   9.2e-10  0.01
Basis identification started.
```

```
Primal basis identification phase started.
ITER      TIME
0         0.00
Primal basis identification phase terminated. Time: 0.00
Dual basis identification phase started.
ITER      TIME
0         0.00
Dual basis identification phase terminated. Time: 0.00
Basis identification terminated. Time: 0.00
Interior-point optimizer terminated. Time: 0.01.

Optimizer terminated. Time: 0.02

Interior-point solution summary
  Problem status  : PRIMAL_AND_DUAL_FEASIBLE
  Solution status : OPTIMAL
  Primal.  obj: 8.3333333280e+01    nrm: 5e+01    Viol.  con: 1e-08    var: 0e+00
  Dual.    obj: 8.3333333242e+01    nrm: 4e+00    Viol.  con: 2e-10    var: 5e-09

Basic solution summary
  Problem status  : PRIMAL_AND_DUAL_FEASIBLE
  Solution status : OPTIMAL
  Primal.  obj: 8.3333333333e+01    nrm: 5e+01    Viol.  con: 7e-15    var: 0e+00
  Dual.    obj: 8.3333333245e+01    nrm: 4e+00    Viol.  con: 2e-10    var: 5e-09

Optimizer summary
  Optimizer                 -                        time: 0.02
    Interior-point          - iterations : 5         time: 0.01
      Basis identification  -                        time: 0.00
        Primal              - iterations : 0         time: 0.00
        Dual                - iterations : 0         time: 0.00
        Clean primal        - iterations : 0         time: 0.00
        Clean dual          - iterations : 0         time: 0.00
    Simplex                 -                        time: 0.00
      Primal simplex        - iterations : 0         time: 0.00
      Dual simplex          - iterations : 0         time: 0.00
    Mixed integer           - relaxations: 0         time: 0.00

Open file '/home/andrea/mosek/8/tools/examples/data/lo1.sol'
Start writing.
done writing. Time: 0.00

Open file '/home/andrea/mosek/8/tools/examples/data/lo1.bas'
Start writing.
done writing. Time: 0.00

Return code - 0  [MSK_RES_OK]
```

5.2.2 Change a Solver Parameter

Using the *-d* option it is possible to set the solver parameters. The next command shows how to switch off the presolver and solve a problem stored in a file called `lo1.opf`.

```
mosek -d MSK_IPAR_PRESOLVE_USE MSK_OFF lo1.opf
```

If multiple parameters must be specified, option *-d* must be repeated for each one. For instance say also the time limit must be set:

```
mosek -d MSK_IPAR_PRESOLVE_USE MSK_OFF -d MSK_DPAR_OPTIMIZER_MAX_TIME 1.0 lo1.opf
```

Please refer to *13.2* for the complete list of available solver parameters.

5.2.3 Convert a File

The **MOSEK** command line can also be used to convert between two file formats supported by **MOSEK**. This can be achieved using the *-out* option. Moreover using *-x* the solver will not actually solve the problem.

Warning: The target file type must support the problem type of the source file, otherwise the conversion will be partial.

For instance in case a MPS file must be converted in a more readable OPF format, the following line can be used

```
mosek -x -out lo1.opf lo1.mps
```

The output produced is

```
MOSEK Version 8.0.0.34(BETA) (Build date: 2016-8-24 00:51:13)
Copyright (c) MOSEK ApS, Denmark. WWW: mosek.com
Platform: Linux/64-X86

Open file '/home/andrea/mosek/8/tools/examples/data/lo1.mps'
Reading started.
Using 'obj' as objective vector
Read 13 number of A nonzeros in 0.00 seconds.
Using 'rhs' as rhs vector
Using 'bound' as bound vector
Reading terminated. Time: 0.01

Read summary
  Type             : LO (linear optimization problem)
  Objective sense  : max
  Scalar variables : 4
  Matrix variables : 0
  Constraints      : 3
  Cones            : 0
  Time             : 0.0

Open file 'lo1.opf'
Start writing.
done writing. Time: 0.00

Return code - 0  [MSK_RES_OK]
```

Note: The output clearly shows how the solver does not actually solve the given problem.

5.3 Command Line Arguments

The following list shows the available command-line arguments for **MOSEK**:

`-anapro`
: Analyze the problem data.

`-anasoli <name>`
: Analyze the initial solution name e.g. *-anasoli bas*.

`-anasolo <name>`
: Analyze the final solution name e.g. *-anasolo itg*.

`-a`
: **MOSEK** is started in AMPL mode.

`-basi <name>`
: Input basis solution file name.

`-baso <name>`
: Output basis solution file name.

`-d <name> <value>`
: Define the value `value` for the **MOSEK** parameter `name`.

`-dbgmem <name>`
: Name of memory debug file.

`-f`
: Complete license information is printed.

`-h, -?`
: Help.

`-inti <name>`
: Input integer solution file name.

`-into <name>`
: Output integer solution file name.

`-itri <name>`
: Input interior point solution file name.

`-itro <name>`
: Output interior point solution file name.

`-info <name>`
: Infeasible subproblem output file name.

`-infrepo <name>`
: Feasibility reparation output file.

`-l,-L <dir>`
: `dir` is the directory where the **MOSEK** license file is located (typically named `mosek.lic`).

`-max`
: The problem is maximized.

`-min`
: The problem is minimized.

`-n`
: Ignore errors in subsequent parameter settings.

`-out <name>`
: Write the task to a data file named *name*. See Section *14*.

`-p <name>, -pari <name>`
: Name of the input parameter file.

`-paro <name>`
: Name of the output parameter file.

`-r`
: If the option is present, the program returns *-1* if an error occurred otherwise *0*.

`-removeitg`
: Removes all integer constraints after reading the problem.

`-rout <name>`
: If the option is present, the program writes the return code to file *name*.

`-q <name>`
: Name of a optional log file.

`-sen <file>`
: Perform sensitivity analysis based on file.

`-silent`
: As little information as possible is send to the terminal.

`-toconic`
: Translate to conic form after reading.

`-v`
: **MOSEK** version is printed and no optimization is performed.

`-w`
: If this options is on, then **MOSEK** will wait for a license.

`-x`
: Do not run the optimizer. Useful for converting between file formats.

`-=`
: List all possible parameters.

5.4 The Parameter File

Occasionally system or algorithmic parameters in **MOSEK** should be changed be the user. One way of changing parameters is to use a so-called parameter file which is a plain text file. It can for example can have the format

```
BEGIN MOSEK
% This is a comment.
% The subsequent line tells MOSEK that an optimal
% basis should be computed by the interior-point optimizer.
MSK_IPAR_INTPNT_BASIS       MSK_BI_ALWAYS
MSK_DPAR_INTPNT_TOL_PFEAS   1.0e-9
END MOSEK
```

Note that the file begins with the line `BEGIN MOSEK` and is terminated with the line `END MOSEK`, this is required. Moreover, everything that appears after an `%` is considered to be a comment and is ignored. Similarly, empty lines are ignored. The important lines are those which begins with a valid **MOSEK** parameter name such as *MSK_IPAR_INTPNT_BASIS*. Immediately after parameter name follows the new value for the parameter. All the **MOSEK** parameter names are listed in Section *13.2*.

Using the parameter file

The parameter file can be given any name, but let us assume it has the name `mosek.par`. If **MOSEK** should use the parameter settings in that file, then *-p* should be on the command line when **MOSEK** is invoked. An example of such a command line is

```
mosek -p mosek.par afiro.mps
```

Command-line parameters override those from the parameter file in case of repetition. For instance

```
mosek -p mosek.par -d MSK_IPAR_NUM_THREAD 1 -d MSK_DPAR_INTPNT_TOL_PFEAS   1.0e-8 afiro.mps
```

will set the *MSK_IPAR_NUM_THREADS* parameter to one, while the the *MSK_DPAR_INTPNT_TOL_PFEAS* will be set to 10^{-8}, using the value provided on the command line.

f.. _doc.cmd.ampl:

CHAPTER

SIX

THE MOSEK-BUNDLED AMPL SHELL

AMPL is a modeling language for specifying linear and nonlinear optimization models in a natural way. AMPL also makes it easy to solve the problem and e.g. display the solution or part of it.

We will not discuss the specifics of the AMPL language here but instead refer the reader to *[FGK03]*, http://ampl.com/BOOK/download.html and the AMPL website http://www.ampl.com.

AMPL cannot solve optimization problems by itself but requires a link to an appropriate optimizer such as **MOSEK**. The **MOSEK** distribution includes

- an AMPL link which makes it possible to use **MOSEK** as an optimizer within AMPL,
- the official AMPL interpreter repackaged `mampl` that uses the **MOSEK** license manager instead of the standard AMPL one.

Warning: It is possible to specify problems in AMPL that cannot be solved by **MOSEK**. The optimization problem must be a smooth convex optimization problem as discussed in Section 7.

Note: To use **MOSEK** from AMPL you need to correctly setup the system path to the **MOSEK** command line tool.

6.1 Invoking the AMPL shell

The **MOSEK** distribution by default comes with the AMPL shell included. Assuming `MSKHOME` is the folder in which **MOSEK** has been installed, it is located under

```
{MSKHOME}/mosek/8/tools/platform/{PLATFORM}/bin/
```

for Linux and OSX users (`PLATFORM` must be among `linux64x86`, `osx64x86`), and under

```
{MSKHOME}\mosek\8\tools\platform\{PLATFORM}\bin\
```

for Windows users (`PLATFORM` must be among `win32x86`, `win64x86`).

To invoke the AMPL shell included in the **MOSEK** distribution type:

```
mampl
```

6.2 An example

In many instances, you can successfully apply **MOSEK** simply by specifying the model and data, setting the solver option to **MOSEK**, and typing `solve`.

The problem we want to solve is a simple linear optimization problem. The AMPL formulation is in Listing 6.1.

Listing 6.1: An example of optimization problem using AMPL language.

```
set NUTR ordered;
set FOOD ordered;

param cost {FOOD} >= 0;
param f_min {FOOD} >= 0, default 0;
param f_max {j in FOOD} >= f_min[j], default Infinity;

param n_min {NUTR} >= 0, default 0;
param n_max {i in NUTR} >= n_min[i], default Infinity;

param amt {NUTR,FOOD} >= 0;

# ------------------------------------------------------

var Buy {j in FOOD} >= f_min[j], <= f_max[j];

# ------------------------------------------------------

minimize Total_Cost:  sum {j in FOOD} cost[j] * Buy[j];

minimize Nutr_Amt {i in NUTR}: sum {j in FOOD} amt[i,j] * Buy[j];

# ------------------------------------------------------

subject to Diet {i in NUTR}:
   n_min[i] <= sum {j in FOOD} amt[i,j] * Buy[j] <= n_max[i];
```

We can specify the input data using an input file again following the AMPL language, as reported in Listing 6.2.

Listing 6.2: An example of data for an optimization problem using AMPL language.

```
param:  FOOD:                     cost  f_min  f_max :=
  "Quarter Pounder w/ Cheese"    1.84     .      .
  "McLean Deluxe w/ Cheese"      2.19     .      .
  "Big Mac"                      1.84     .      .
  "Filet-O-Fish"                 1.44     .      .
  "McGrilled Chicken"            2.29     .      .
  "Fries, small"                  .77     .      .
  "Sausage McMuffin"             1.29     .      .
  "1% Lowfat Milk"                .60     .      .
  "Orange Juice"                  .72     .      . ;

param:  NUTR:   n_min  n_max :=
        Cal      2000      .
        Carbo     350    375
        Protein    55      .
        VitA      100      .
        VitC      100      .
        Calc      100      .
        Iron      100      . ;

param amt (tr):
                              Cal  Carbo Protein   VitA   VitC  Calc  Iron :=
  "Quarter Pounder w/ Cheese" 510     34     28     15      6    30    20
  "McLean Deluxe w/ Cheese"   370     35     24     15     10    20    20
  "Big Mac"                   500     42     25      6      2    25    20
  "Filet-O-Fish"              370     38     14      2      0    15    10
```

```
  "McGrilled Chicken"          400     42     31      8     15     15      8
  "Fries, small"               220     26      3      0     15      0      2
  "Sausage McMuffin"           345     27     15      4      0     20     15
  "1% Lowfat Milk"             110     12      9     10      4     30      0
  "Orange Juice"                80     20      1      2    120      2      2 ;
```

First to invoke the AMPL shell type:

```
mampl
```

when the AMPL shell has started type the commands:

```
ampl: model diet.mod;
ampl: data diet.dat;
ampl: option solver mosek;
ampl: solve;
```

The resulting output is:

```
MOSEK finished.
Problem status    - PRIMAL_AND_DUAL_FEASIBLE
Solution status   - OPTIMAL
Primal objective  - 14.8557377
Dual objective    - 14.8557377

Objective = Total_Cost
```

6.3 Determining the outcome of an optimization

The AMPL parameter `solve_result_num` is used to indicate the outcome of the optimization process. It is used as follows

```
ampl: display solve_result_num
```

Please refer to table Table 6.1 for possible values of this parameter.

Table 6.1: Interpretation of `solve_result_num`.

Value	Message
0	the solution is optimal.
100	suboptimal primal solution.
101	superoptimal (dual feasible) solution.
150	the solution is near optimal.
200	primal infeasible problem.
300	dual infeasible problem.
400	too many iterations.
500	solution status is unknown.
501	ill-posed problem, solution status is unknown.
> 501	Mapped **MOSEK** response code. See note below.

Note: **MOSEK** response codes are mapped on AMPL return code greater than 501. In order to get the actual response code the base value `501` must be subtracted. For example: say the AMPL return code is `502`, then it corresponds to **MOSEK** response code `1`.

6.4 Optimizer options

6.4.1 The MOSEK parameter database

The **MOSEK** optimizer has options and parameters controlling such things as the termination criterion and which optimizer is used. These parameters can be modified within AMPL as shown in the example below:

```
ampl: model diet.mod;
ampl: data diet.dat;
ampl: option solver mosek;
ampl: option mosek_options
ampl? 'msk_ipar_optimizer = msk_optimizer_primal_simplex \
ampl? msk_ipar_sim_max_iterations = 100000';
ampl: solve;
```

In the example above a string called `mosek_options` is created which contains the parameter settings. Each parameter setting has the format

```
parameter name = value
```

where `parameter name` can be any valid **MOSEK** parameter name. See Section *13.2* for a description of all valid **MOSEK** parameters.

An alternative way of specifying the options is

```
ampl: option mosek_options
ampl? 'msk_ipar_optimizer = msk_optimizer_primal_simplex'
ampl? 'msk_ipar_sim_max_iterations = 100000';
```

New options can also be appended to an existing option string as shown below

```
ampl: option mosek_options $mosek_options
ampl? ' msk_ipar_sim_print_freq = 0 msk_ipar_sim_max_iterations = 1000';
```

The expression `$mosek_options` expands to the current value of the option. Line two in the example appends an additional value `msk_ipar_sim_max_iterations` to the option string.

6.4.2 Options

outlev

Controls the amount of printed output. 0 means no printed output and a higher value means more printed output. An example of setting `outlev` is as follows:

```
ampl: option mosek_options 'outlev=2';
```

wantsol

We refer the reader to the AMPL manual *[FGK03]* for details about this option.

6.5 Constraint and variable names

AMPL assigns meaningful names to all the constraints and variables. Since **MOSEK** uses item names in error and log messages, it may be useful to pass the AMPL names to **MOSEK**.

Using the command

```
ampl: option auxfiles rc;
```

before the

```
ampl: solve;
```

command makes **MOSEK** obtain the constraint and variable names automatically.

6.6 Which solution is returned to AMPL

The **MOSEK** optimizer can produce three types of solutions: basic, integer, and interior point solutions. For nonlinear problems only an interior solution is available. For linear optimization problems optimized by the interior-point optimizer with basis identification turned on both a basic and an interior point solution are calculated. The simplex algorithm produces only a basic solution. Whenever both an interior and a basic solution are available, the basic solution is returned. For problems containing integer variables, the integer solution is returned to AMPL.

6.7 Hot-start

Frequently, a sequence of optimization problems is solved where each problem differs only slightly from the previous problem. In that case it may be advantageous to use the previous optimal solution to warm-start the optimizer. Such a facility is available in **MOSEK** only when the simplex optimizer is used.

The warm-start facility exploits the AMPL variable suffix `sstatus` to communicate the optimal basis back to AMPL, and AMPL uses this facility to communicate an initial basis to **MOSEK**. The following example demonstrates this feature.

```
ampl: model diet.mod;
ampl: data diet.dat;
ampl: option solver mosek;
ampl: option mosek_options
ampl? 'msk_ipar_optimizer = msk_optimizer_primal_simplex outlev=2';
ampl: solve;
ampl: display Buy.sstatus;
ampl: solve;
```

The resulting output is:

```
Accepted: msk_ipar_optimizer                 = MSK_OPTIMIZER_PRIMAL_SIMPLEX
Accepted: outlev                             = 2

Computer   - Platform               : Linux/64-X86
Computer   - CPU type               : Intel-P4
MOSEK      - task name              :
MOSEK      - objective sense        : min
MOSEK      - problem type           : LO (linear optimization problem)
MOSEK      - constraints            : 7                 variables             : 9
MOSEK      - integer variables      : 0
Optimizer started.
Simplex optimizer started.
Presolve started.
Linear dependency checker started.
Linear dependency checker terminated.
Presolve   - Stk. size (kb) : 0
Eliminator - tries                  : 0                 time                  : 0.00
```

```
Eliminator - elim's                : 0
Lin. dep.  - tries                 : 1                 time                   : 0.00
Lin. dep.  - number                : 0
Presolve terminated. Time: 0.00
Primal simplex optimizer started.
Primal simplex optimizer setup started.
Primal simplex optimizer setup terminated.
Optimizer  - solved problem        : the primal
Optimizer  - constraints           : 7                 variables              : 9
Optimizer  - hotstart              : no
ITER      DEGITER(%)  PFEAS       DFEAS       POBJ                  DOBJ                  TIME␣
 ↪      TOTTIME
0           0.00        1.40e+03    NA          1.2586666667e+01      NA                    0.00␣
 ↪      0.01
3           0.00        0.00e+00    NA          1.4855737705e+01      NA                    0.00␣
 ↪      0.01
Primal simplex optimizer terminated.
Simplex optimizer terminated. Time: 0.00.
Optimizer terminated. Time: 0.01
Return code - 0  [MSK_RES_OK]
MOSEK finished.
Problem status     : PRIMAL_AND_DUAL_FEASIBLE
Solution status    : OPTIMAL
Primal objective   : 14.8557377
Dual objective     : 14.8557377

Objective = Total_Cost
Buy.sstatus [*] :=
'Quarter Pounder w/ Cheese'  bas
'McLean Deluxe w/ Cheese'  low
'Big Mac'  low
Filet-O-Fish  low
'McGrilled Chicken'  low
'Fries, small'  bas
'Sausage McMuffin'  low
'1% Lowfat Milk'  bas
'Orange Juice'  low
;
Accepted: msk_ipar_optimizer                 = MSK_OPTIMIZER_PRIMAL_SIMPLEX
Accepted: outlev                             = 2
Basic solution
Problem status  : UNKNOWN
Solution status : UNKNOWN
Primal - objective: 1.4855737705e+01   eq. infeas.: 3.97e+03 max bound infeas.: 2.00e+03
Dual   - objective: 0.0000000000e+00   eq. infeas.: 7.14e-01 max bound infeas.: 0.00e+00

Computer   - Platform             : Linux/64-X86
Computer   - CPU type              : Intel-P4
MOSEK      - task name             :
MOSEK      - objective sense       : min
MOSEK      - problem type          : LO (linear optimization problem)
MOSEK      - constraints           : 7                 variables              : 9
MOSEK      - integer variables     : 0
Optimizer started.
Simplex optimizer started.
Presolve started.
Presolve   - Stk. size (kb) : 0
Eliminator - tries                 : 0                 time                   : 0.00
Eliminator - elim's                : 0
Lin. dep.  - tries                 : 0                 time                   : 0.00
Lin. dep.  - number                : 0
Presolve terminated. Time: 0.00
Primal simplex optimizer started.
```

```
Primal simplex optimizer setup started.
Primal simplex optimizer setup terminated.
Optimizer  - solved problem         : the primal
Optimizer  - constraints            : 7                 variables             : 9
Optimizer  - hotstart               : yes
Optimizer  - Num. basic             : 7                 Basis rank            : 7
Optimizer  - Valid bas. fac.        : no
ITER      DEGITER(%)  PFEAS       DFEAS       POBJ                  DOBJ                  TIME␣
↪     TOTTIME
0           0.00        0.00e+00    NA          1.4855737705e+01      NA                    0.00␣
↪     0.01
0           0.00        0.00e+00    NA          1.4855737705e+01      NA                    0.00␣
↪     0.01
Primal simplex optimizer terminated.
Simplex optimizer terminated. Time: 0.00.
Optimizer terminated. Time: 0.01
Return code - 0  [MSK_RES_OK]
MOSEK finished.
Problem status    : PRIMAL_AND_DUAL_FEASIBLE
Solution status   : OPTIMAL
Primal objective  : 14.8557377
Dual objective    : 14.8557377

Objective = Total_Cost
```

Please note that the second solve takes fewer iterations since the previous optimal basis is reused.

6.8 The infeasibility report

For linear optimization problems without any integer constrained variables **MOSEK** can generate an infeasibility report automatically. The report provides important information about the infeasibility.

The generation of the infeasibility report is turned on using the parameter setting

```
option auxfiles rc;
option mosek_options 'msk_ipar_infeas_report_auto=msk_on';
```

For further details about infeasibility report see Section *11*.

6.9 Sensitivity analysis

MOSEK can calculate sensitivity information for the objective and constraints. To enable sensitivity information set the option:

```
sensitivity = 1
```

Results are returned in variable/constraint suffixes as follows:

- `.down` Smallest value of objective coefficient/right hand side before the optimal basis changes.
- `.up` Largest value of objective coefficient/right hand side before the optimal basis changes.
- `.current` Current value of objective coefficient/right hand side.

For ranged constraints sensitivity information is returned only for the lower bound.

The example below returns sensitivity information on the `diet` model.

```
ampl: model diet.mod;
ampl: data diet.dat;
ampl: option solver mosek;
ampl: option mosek_options 'sensitivity=1';

ampl: solve;
#display sensitivity information and current solution.
ampl: display _var.down,_var.current,_var.up,_var;
#display sensitivity information and optimal dual values.
ampl: display _con.down,_con.current,_con.up,_con;
```

The resulting output is:

```
Return code - 0  [MSK_RES_OK]
MOSEK finished.
Problem status    : PRIMAL_AND_DUAL_FEASIBLE
Solution status   : OPTIMAL
Primal objective  : 14.8557377
Dual objective    : 14.8557377


suffix up OUT;
suffix down OUT;
suffix current OUT;
Objective = Total_Cost
:  _var.down _var.current       _var.up        _var      :=
1   1.37385       1.84             1.86075    4.38525
2   1.8677        2.19      Infinity          0
3   1.82085       1.84      Infinity          0
4   1.35466       1.44      Infinity          0
5   1.57633       2.29      Infinity          0
6   0.094         0.77             0.794851   6.14754
7   1.22759       1.29      Infinity          0
8   0.57559       0.6              0.910769   3.42213
9   0.657279      0.72      Infinity          0
;
ampl: display _con.down,_con.current,_con.up,_con;
:     _con.down    _con.current   _con.up      _con       :=
1   -Infinity           2000      3965.37    0
2         297.6          350       375       0.0277049
3   -Infinity            55       172.029   0
4          63.0531       100       195.388   0.0267541
5   -Infinity           100       132.213   0
6   -Infinity           100       234.221   0
7          17.6923       100       142.821   0.0248361
;
```

6.10 Using the command line version of the AMPL interface

AMPL can generate a data file containing all the optimization problem and all relevant information which can then be read and solved by the **MOSEK** command line tool.

When the problem has been loaded into AMPL, the commands

```
ampl: option auxfiles rc;
ampl: write  bprob;
```

will make AMPL write the appropriate data files, i.e.

```
prob.nl
prob.col
prob.row
```

Then the problem can be solved using the command line version of **MOSEK** as follows

```
mosek prob.nl outlev=10 -a
```

The `-a` command line option indicates that **MOSEK** is invoked in AMPL mode. When **MOSEK** is invoked in AMPL mode the normal **MOSEK** command line options should appear *after* the `-a` option except for the file name which should be the first argument. As the above example demonstrates **MOSEK** accepts command line options as specified by the AMPL `convention`. Which command line arguments **MOSEK** accepts in AMPL mode can be viewed by executing

```
mosek -= -a
```

For linear, quadratic and quadratic constrained problems a text file representation of the problem can be obtained using one of the commands

```
mosek prob.nl -a -x -out prob.mps
mosek prob.nl -a -x -out prob.opf
mosek prob.nl -a -x -out prob.lp
```

CHAPTER

SEVEN

PROBLEM FORMULATION AND SOLUTIONS

In this chapter we will discuss the following issues:

- The formal, mathematical formulations of the problem types that **MOSEK** can solve and their duals.
- The solution information produced by **MOSEK**.
- The infeasibility certificate produced by **MOSEK** if the problem is infeasible.

7.1 Linear Optimization

A linear optimization problem can be written as

$$\begin{array}{lccccc} \text{minimize} & & & c^T x + c^f & & \\ \text{subject to} & l^c & \leq & Ax & \leq & u^c, \\ & l^x & \leq & x & \leq & u^x, \end{array} \tag{7.1}$$

where

- m is the number of constraints.
- n is the number of decision variables.
- $x \in \mathbb{R}^n$ is a vector of decision variables.
- $c \in \mathbb{R}^n$ is the linear part of the objective function.
- $A \in \mathbb{R}^{m \times n}$ is the constraint matrix.
- $l^c \in \mathbb{R}^m$ is the lower limit on the activity for the constraints.
- $u^c \in \mathbb{R}^m$ is the upper limit on the activity for the constraints.
- $l^x \in \mathbb{R}^n$ is the lower limit on the activity for the variables.
- $u^x \in \mathbb{R}^n$ is the upper limit on the activity for the variables.

A primal solution (x) is *(primal) feasible* if it satisfies all constraints in (7.1). If (7.1) has at least one primal feasible solution, then (7.1) is said to be (primal) feasible.

In case (7.1) does not have a feasible solution, the problem is said to be *(primal) infeasible*

7.1.1 Duality for Linear Optimization

Corresponding to the primal problem (7.1), there is a dual problem

$$\begin{array}{lcccc} \text{maximize} & (l^c)^T s_l^c - (u^c)^T s_u^c + (l^x)^T s_l^x - (u^x)^T s_u^x + c^f & & & \\ & A^T y + s_l^x - s_u^x & = & c, & \\ \text{subject to} & -y + s_l^c - s_u^c & = & 0, & \\ & s_l^c, s_u^c, s_l^x, s_u^x & \geq & 0. & \end{array} \tag{7.2}$$

If a bound in the primal problem is plus or minus infinity, the corresponding dual variable is fixed at 0, and we use the convention that the product of the bound value and the corresponding dual variable is 0. E.g.

$$l_j^x = -\infty \quad \Rightarrow \quad (s_l^x)_j = 0 \text{ and } l_j^x \cdot (s_l^x)_j = 0.$$

This is equivalent to removing variable $(s_l^x)_j$ from the dual problem. A solution

$$(y, s_l^c, s_u^c, s_l^x, s_u^x)$$

to the dual problem is feasible if it satisfies all the constraints in (7.2). If (7.2) has at least one feasible solution, then (7.2) is *(dual) feasible*, otherwise the problem is *(dual) infeasible*.

A Primal-dual Feasible Solution

A solution

$$(x, y, s_l^c, s_u^c, s_l^x, s_u^x)$$

is denoted a *primal-dual feasible solution*, if (x) is a solution to the primal problem (7.1) and $(y, s_l^c, s_u^c, s_l^x, s_u^x)$ is a solution to the corresponding dual problem (7.2).

The Duality Gap

Let

$$(x^*, y^*, (s_l^c)^*, (s_u^c)^*, (s_l^x)^*, (s_u^x)^*)$$

be a primal-dual feasible solution, and let

$$(x^c)^* := Ax^*.$$

For a primal-dual feasible solution we define the *duality gap* as the difference between the primal and the dual objective value,

$$\begin{array}{l} c^T x^* + c^f - \left\{ (l^c)^T (s_l^c)^* - (u^c)^T (s_u^c)^* + (l^x)^T (s_l^x)^* - (u^x)^T (s_u^x)^* + c^f \right\} \\ \quad = \sum_{i=0}^{m-1} \left[(s_l^c)_i^* ((x_i^c)^* - l_i^c) + (s_u^c)_i^* (u_i^c - (x_i^c)^*) \right] \\ \quad + \sum_{j=0}^{n-1} \left[(s_l^x)_j^* (x_j - l_j^x) + (s_u^x)_j^* (u_j^x - x_j^*) \right] \geq 0 \end{array} \tag{7.3}$$

where the first relation can be obtained by transposing and multiplying the dual constraints (7.2) by x^* and $(x^c)^*$ respectively, and the second relation comes from the fact that each term in each sum is nonnegative. It follows that the primal objective will always be greater than or equal to the dual objective.

An Optimal Solution

It is well-known that a linear optimization problem has an optimal solution if and only if there exist feasible primal and dual solutions so that the duality gap is zero, or, equivalently, that the *complementarity conditions*

$$\begin{array}{rcll} (s_l^c)_i^* ((x_i^c)^* - l_i^c) & = & 0, & i = 0, \ldots, m-1, \\ (s_u^c)_i^* (u_i^c - (x_i^c)^*) & = & 0, & i = 0, \ldots, m-1, \\ (s_l^x)_j^* (x_j^* - l_j^x) & = & 0, & j = 0, \ldots, n-1, \\ (s_u^x)_j^* (u_j^x - x_j^*) & = & 0, & j = 0, \ldots, n-1, \end{array}$$

are satisfied.

If (7.1) has an optimal solution and **MOSEK** solves the problem successfully, both the primal and dual solution are reported, including a status indicating the exact state of the solution.

7.1.2 Infeasibility for Linear Optimization

Primal Infeasible Problems

If the problem (7.1) is infeasible (has no feasible solution), **MOSEK** will report a certificate of primal infeasibility: The dual solution reported is the certificate of infeasibility, and the primal solution is undefined.

A certificate of primal infeasibility is a feasible solution to the modified dual problem

$$\begin{array}{ll} \text{maximize} & (l^c)^T s_l^c - (u^c)^T s_u^c + (l^x)^T s_l^x - (u^x)^T s_u^x \\ \text{subject to} & \\ & \begin{array}{c} A^T y + s_l^x - s_u^x = 0, \\ -y + s_l^c - s_u^c = 0, \\ s_l^c, s_u^c, s_l^x, s_u^x \geq 0, \end{array} \end{array} \tag{7.4}$$

such that the objective value is strictly positive, i.e. a solution

$$(y^*, (s_l^c)^*, (s_u^c)^*, (s_l^x)^*, (s_u^x)^*)$$

to (7.4) so that

$$(l^c)^T (s_l^c)^* - (u^c)^T (s_u^c)^* + (l^x)^T (s_l^x)^* - (u^x)^T (s_u^x)^* > 0.$$

Such a solution implies that (7.4) is unbounded, and that its dual is infeasible. As the constraints to the dual of (7.4) are identical to the constraints of problem (7.1), we thus have that problem (7.1) is also infeasible.

Dual Infeasible Problems

If the problem (7.2) is infeasible (has no feasible solution), **MOSEK** will report a certificate of dual infeasibility: The primal solution reported is the certificate of infeasibility, and the dual solution is undefined.

A certificate of dual infeasibility is a feasible solution to the modified primal problem

$$\begin{array}{lccccc} \text{minimize} & & & c^T x & & \\ \text{subject to} & \hat{l}^c & \leq & Ax & \leq & \hat{u}^c, \\ & \hat{l}^x & \leq & x & \leq & \hat{u}^x, \end{array} \tag{7.5}$$

where

$$\hat{l}_i^c = \left\{ \begin{array}{ll} 0 & \text{if } l_i^c > -\infty, \\ -\infty & \text{otherwise,} \end{array} \right\} \quad \text{and} \quad \hat{u}_i^c := \left\{ \begin{array}{ll} 0 & \text{if } u_i^c < \infty, \\ \infty & \text{otherwise,} \end{array} \right\}$$

and

$$\hat{l}_j^x = \left\{ \begin{array}{ll} 0 & \text{if } l_j^x > -\infty, \\ -\infty & \text{otherwise,} \end{array} \right\} \quad \text{and} \quad \hat{u}_j^x := \left\{ \begin{array}{ll} 0 & \text{if } u_j^x < \infty, \\ \infty & \text{otherwise,} \end{array} \right\}$$

such that

$$c^T x < 0.$$

Such a solution implies that (7.5) is unbounded, and that its dual is infeasible. As the constraints to the dual of (7.5) are identical to the constraints of problem (7.2), we thus have that problem (7.2) is also infeasible.

Primal and Dual Infeasible Case

In case that both the primal problem (7.1) and the dual problem (7.2) are infeasible, **MOSEK** will report only one of the two possible certificates — which one is not defined (**MOSEK** returns the first certificate found).

Minimalization vs. Maximalization

When the objective sense of problem (7.1) is maximization, i.e.

$$\begin{array}{lccccc} \text{maximize} & & & c^T x + c^f & & \\ \text{subject to} & l^c & \leq & Ax & \leq & u^c, \\ & l^x & \leq & x & \leq & u^x, \end{array}$$

the objective sense of the dual problem changes to minimization, and the domain of all dual variables changes sign in comparison to (7.2). The dual problem thus takes the form

$$\begin{array}{ll} \text{minimize} & (l^c)^T s_l^c - (u^c)^T s_u^c + (l^x)^T s_l^x - (u^x)^T s_u^x + c^f \\ \text{subject to} & \\ & A^T y + s_l^x - s_u^x = c, \\ & -y + s_l^c - s_u^c = 0, \\ & s_l^c, s_u^c, s_l^x, s_u^x \leq 0. \end{array}$$

This means that the duality gap, defined in (7.3) as the primal minus the dual objective value, becomes nonpositive. It follows that the dual objective will always be greater than or equal to the primal objective. The primal infeasibility certificate will be reported by **MOSEK** as a solution to the system

$$\begin{array}{l} A^T y + s_l^x - s_u^x = 0, \\ -y + s_l^c - s_u^c = 0, \\ s_l^c, s_u^c, s_l^x, s_u^x \leq 0, \end{array} \tag{7.6}$$

such that the objective value is strictly negative

$$(l^c)^T (s_l^c)^* - (u^c)^T (s_u^c)^* + (l^x)^T (s_l^x)^* - (u^x)^T (s_u^x)^* < 0.$$

Similarly, the certificate of dual infeasibility is an x satisfying the requirements of (7.5) such that $c^T x > 0$.

7.2 Conic Quadratic Optimization

Conic quadratic optimization is an extension of linear optimization (see Section 7.1) allowing conic domains to be specified for subsets of the problem variables. A conic quadratic optimization problem can be written as

$$\begin{array}{lccccc} \text{minimize} & & & c^T x + c^f & & \\ \text{subject to} & l^c & \leq & Ax & \leq & u^c, \\ & l^x & \leq & x & \leq & u^x, \\ & & & x \in \mathcal{K}, & & \end{array} \tag{7.7}$$

where set $\mathcal{K}$ is a Cartesian product of convex cones, namely $\mathcal{K} = \mathcal{K}_1 \times \cdots \times \mathcal{K}_p$. Having the domain restriction, $x \in \mathcal{K}$, is thus equivalent to

$$x^t \in \mathcal{K}_t \subseteq \mathbb{R}^{n_t},$$

where $x = (x^1, \ldots, x^p)$ is a partition of the problem variables. Please note that the n-dimensional Euclidean space $\mathbb{R}^n$ is a cone itself, so simple linear variables are still allowed.

MOSEK supports only a limited number of cones, specifically:

- The $\mathbb{R}^n$ set.
- The quadratic cone:

$$\mathcal{Q}^n = \left\{ x \in \mathbb{R}^n : x_1 \geq \sqrt{\sum_{j=2}^{n} x_j^2} \right\}.$$

- The rotated quadratic cone:

$$\mathcal{Q}_r^n = \left\{ x \in \mathbb{R}^n : 2x_1x_2 \geq \sum_{j=3}^{n} x_j^2, \quad x_1 \geq 0, \quad x_2 \geq 0 \right\}.$$

Although these cones may seem to provide only limited expressive power they can be used to model a wide range of problems as demonstrated in *[MOSEKApS12]*.

7.2.1 Duality for Conic Quadratic Optimization

The dual problem corresponding to the conic quadratic optimization problem (7.7) is given by

$$\begin{array}{ll} \text{maximize} & (l^c)^T s_l^c - (u^c)^T s_u^c + (l^x)^T s_l^x - (u^x)^T s_u^x + c^f \\ \text{subject to} & \\ & \begin{array}{c} A^T y + s_l^x - s_u^x + s_n^x = c \\ -y + s_l^c - s_u^c = 0, \\ s_l^c, s_u^c, s_l^x, s_u^x \geq 0, \\ s_n^x \in \mathcal{K}^*, \end{array} \end{array} \tag{7.8}$$

where the dual cone $\mathcal{K}^*$ is a Cartesian product of the cones

$$\mathcal{K}^* = \mathcal{K}_1^* \times \cdots \times \mathcal{K}_p^*,$$

where each $\mathcal{K}_t^*$ is the dual cone of $\mathcal{K}_t$. For the cone types **MOSEK** can handle, the relation between the primal and dual cone is given as follows:

- The $\mathbb{R}^n$ set:

$$\mathcal{K}_t = \mathbb{R}^{n_t} \quad \Leftrightarrow \quad \mathcal{K}_t^* = \{ s \in \mathbb{R}^{n_t} : \quad s = 0 \}.$$

- The quadratic cone:

$$\mathcal{K}_t = \mathcal{Q}^{n_t} \quad \Leftrightarrow \quad \mathcal{K}_t^* = \mathcal{Q}^{n_t} = \left\{ s \in \mathbb{R}^{n_t} : s_1 \geq \sqrt{\sum_{j=2}^{n_t} s_j^2} \right\}.$$

- The rotated quadratic cone:

$$\mathcal{K}_t = \mathcal{Q}_r^{n_t} \quad \Leftrightarrow \quad \mathcal{K}_t^* = \mathcal{Q}_r^{n_t} = \left\{ s \in \mathbb{R}^{n_t} : 2s_1s_2 \geq \sum_{j=3}^{n_t} s_j^2, \quad s_1 \geq 0, \quad s_2 \geq 0 \right\}.$$

Please note that the dual problem of the dual problem is identical to the original primal problem.

7.2.2 Infeasibility for Conic Quadratic Optimization

In case **MOSEK** finds a problem to be infeasible it reports a certificate of infeasibility. This works exactly as for linear problems (see Section *7.1.2*).

Primal Infeasible Problems

If the problem (7.7) is infeasible, **MOSEK** will report a certificate of primal infeasibility: The dual solution reported is the certificate of infeasibility, and the primal solution is undefined.

A certificate of primal infeasibility is a feasible solution to the problem

$$\begin{array}{ll} \text{maximize} & (l^c)^T s_l^c - (u^c)^T s_u^c + (l^x)^T s_l^x - (u^x)^T s_u^x \\ \text{subject to} & \\ & \begin{array}{rcl} A^T y + s_l^x - s_u^x + s_n^x & = & 0, \\ -y + s_l^c - s_u^c & = & 0, \\ s_l^c, s_u^c, s_l^x, s_u^x & \geq & 0, \\ s_n^x \in \mathcal{K}^*, & & \end{array} \end{array}$$

such that the objective value is strictly positive.

Dual infeasible problems

If the problem (7.8) is infeasible, **MOSEK** will report a certificate of dual infeasibility: The primal solution reported is the certificate of infeasibility, and the dual solution is undefined.

A certificate of dual infeasibility is a feasible solution to the problem

$$\begin{array}{lccccc} \text{minimize} & & & c^T x & & \\ \text{subject to} & \hat{l}^c & \leq & Ax & \leq & \hat{u}^c, \\ & \hat{l}^x & \leq & x & \leq & \hat{u}^x, \\ & & & x \in \mathcal{K}, & & \end{array}$$

where

$$\hat{l}_i^c = \left\{ \begin{array}{ll} 0 & \text{if } l_i^c > -\infty, \\ -\infty & \text{otherwise,} \end{array} \right\} \quad \text{and} \quad \hat{u}_i^c := \left\{ \begin{array}{ll} 0 & \text{if } u_i^c < \infty, \\ \infty & \text{otherwise,} \end{array} \right\}$$

and

$$\hat{l}_j^x = \left\{ \begin{array}{ll} 0 & \text{if } l_j^x > -\infty, \\ -\infty & \text{otherwise,} \end{array} \right\} \quad \text{and} \quad \hat{u}_j^x := \left\{ \begin{array}{ll} 0 & \text{if } u_j^x < \infty, \\ \infty & \text{otherwise,} \end{array} \right\}$$

such that the objective value is strictly negative.

7.3 Semidefinite Optimization

Semidefinite optimization is an extension of conic quadratic optimization (see Section 7.2) allowing positive semidefinite matrix variables to be used in addition to the usual scalar variables. A semidefinite optimization problem can be written as

$$\begin{array}{lccccll} \text{minimize} & & & \sum_{j=0}^{n-1} c_j x_j + \sum_{j=0}^{p-1} \langle \overline{C}_j, \overline{X}_j \rangle + c^f & & & \\ \text{subject to} & l_i^c & \leq & \sum_{j=0}^{n-1} a_{ij} x_j + \sum_{j=0}^{p-1} \langle \overline{A}_{ij}, \overline{X}_j \rangle & \leq & u_i^c, & i = 0, \ldots, m-1 \\ & l_j^x & \leq & x_j & \leq & u_j^x, & j = 0, \ldots, n-1 \\ & & & x \in \mathcal{K}, \overline{X}_j \in \mathcal{S}_+^{r_j}, & & & j = 0, \ldots, p-1 \end{array} \tag{7.9}$$

where the problem has p symmetric positive semidefinite variables $\overline{X}_j \in \mathcal{S}_+^{r_j}$ of dimension r_j with symmetric coefficient matrices $\overline{C}_j \in \mathcal{S}^{r_j}$ and $\overline{A}_{i,j} \in \mathcal{S}^{r_j}$. We use standard notation for the matrix inner product, i.e., for $U, V \in \mathbb{R}^{m \times n}$ we have

$$\langle U, V \rangle := \sum_{i=0}^{m-1} \sum_{j=0}^{n-1} U_{ij} V_{ij}.$$

With semidefinite optimization we can model a wide range of problems as demonstrated in *[MOSEKApS12]*.

7.3.1 Duality for Semidefinite Optimization

The dual problem corresponding to the semidefinite optimization problem (7.9) is given by

$$\begin{array}{ll} \text{maximize} & (l^c)^T s_l^c - (u^c)^T s_u^c + (l^x)^T s_l^x - (u^x)^T s_u^x + c^f \\ \text{subject to} & \\ & c - A^T y + s_u^x - s_l^x = s_n^x, \\ & \overline{C}_j - \sum_{i=0}^m y_i \overline{A}_{ij} = \overline{S}_j, \qquad j = 0, \ldots, p-1 \\ & s_l^c - s_u^c = y, \\ & s_l^c, s_u^c, s_l^x, s_u^x \geq 0, \\ & s_n^x \in \mathcal{K}^*, \quad \overline{S}_j \in \mathcal{S}_+^{r_j}, \qquad j = 0, \ldots, p-1 \end{array} \tag{7.10}$$

where $A \in \mathbb{R}^{m\times n}$, $A_{ij} = a_{ij}$, which is similar to the dual problem for conic quadratic optimization (see Section *7.2.1*), except for the addition of dual constraints

$$\left(\overline{C}_j - \sum_{i=0}^{m} y_i \overline{A}_{ij}\right) \in \mathcal{S}_+^{r_j}.$$

Note that the dual of the dual problem is identical to the original primal problem.

7.3.2 Infeasibility for Semidefinite Optimization

In case **MOSEK** finds a problem to be infeasible it reports a certificate of the infeasibility. This works exactly as for linear problems (see Section *7.1.2*).

Primal Infeasible Problems

If the problem (7.9) is infeasible, **MOSEK** will report a certificate of primal infeasibility: The dual solution reported is a certificate of infeasibility, and the primal solution is undefined.

A certificate of primal infeasibility is a feasible solution to the problem

$$\begin{array}{lll}
\text{maximize} & (l^c)^T s_l^c - (u^c)^T s_u^c + (l^x)^T s_l^x - (u^x)^T s_u^x & \\
\text{subject to} & & \\
& A^T y + s_l^x - s_u^x + s_n^x = 0, & \\
& \sum_{i=0}^{m-1} y_i \overline{A}_{ij} + \overline{S}_j = 0, & j = 0, \ldots, p-1 \\
& -y + s_l^c - s_u^c = 0, & \\
& s_l^c, s_u^c, s_l^x, s_u^x \geq 0, & \\
& s_n^x \in \mathcal{K}^*, \quad \overline{S}_j \in \mathcal{S}_+^{r_j}, & j = 0, \ldots, p-1
\end{array}$$

such that the objective value is strictly positive.

Dual Infeasible Problems

If the problem (7.10) is infeasible, **MOSEK** will report a certificate of dual infeasibility: The primal solution reported is the certificate of infeasibility, and the dual solution is undefined.

A certificate of dual infeasibility is a feasible solution to the problem

$$\begin{array}{lccccll}
\text{minimize} & & & \sum_{j=0}^{n-1} c_j x_j + \sum_{j=0}^{p-1} \langle \overline{C}_j, \overline{X}_j \rangle & & & \\
\text{subject to} & \hat{l}_i^c & \leq & \sum_{j=1}^{n} a_{ij} x_j + \sum_{j=0}^{p-1} \langle \overline{A}_{ij}, \overline{X}_j \rangle & \leq & \hat{u}_i^c, & i = 0, \ldots, m-1 \\
& \hat{l}^x & \leq & x & \leq & \hat{u}^x, & \\
& & & x \in \mathcal{K}, \quad \overline{X}_j \in \mathcal{S}_+^{r_j}, & & & j = 0, \ldots, p-1
\end{array}$$

where

$$\hat{l}_i^c = \begin{cases} 0 & \text{if } l_i^c > -\infty, \\ -\infty & \text{otherwise,} \end{cases} \quad \text{and} \quad \hat{u}_i^c := \begin{cases} 0 & \text{if } u_i^c < \infty, \\ \infty & \text{otherwise,} \end{cases}$$

and

$$\hat{l}_j^x = \begin{cases} 0 & \text{if } l_j^x > -\infty, \\ -\infty & \text{otherwise,} \end{cases} \quad \text{and} \quad \hat{u}_j^x := \begin{cases} 0 & \text{if } u_j^x < \infty, \\ \infty & \text{otherwise,} \end{cases}$$

such that the objective value is strictly negative.

7.4 Quadratic and Quadratically Constrained Optimization

A convex quadratic and quadratically constrained optimization problem is an optimization problem of the form

$$\begin{array}{lccccll} \text{minimize} & & & \frac{1}{2}x^T Q^o x + c^T x + c^f & & & \\ \text{subject to} & l_k^c & \leq & \frac{1}{2}x^T Q^k x + \sum_{j=0}^{n-1} a_{kj} x_j & \leq & u_k^c, & k = 0, \ldots, m-1, \\ & l_j^x & \leq & x_j & \leq & u_j^x, & j = 0, \ldots, n-1, \end{array} \tag{7.11}$$

where Q^o and all Q^k are symmetric matrices. Moreover for convexity, Q^o must be a positive semidefinite matrix and Q^k must satisfy

$$\begin{array}{rcl} -\infty < l_k^c & \Rightarrow & Q^k \text{ is negative semidefinite,} \\ u_k^c < \infty & \Rightarrow & Q^k \text{ is positive semidefinite,} \\ -\infty < l_k^c \leq u_k^c < \infty & \Rightarrow & Q^k = 0. \end{array}$$

The convexity requirement is very important and **MOSEK** checks whether it is fullfiled.

7.4.1 A Recommendation

Any convex quadratic optimization problem can be reformulated as a conic quadratic optimization problem, see *[MOSEKApS12]* and in particular *[And13]*. In fact **MOSEK** does such conversion internally as a part of the solution process for the following reasons:

- the conic optimizer is numerically more robust than the one for quadratic problems.
- the conic optimizer is usually faster because quadratic cones are simpler than quadratic functions, even though the conic reformulation usually has more constraints and variables than the original quadratic formulation.
- it is easy to dualize the conic formuation if deemed worthwhile potentially leading to (huge) computational savings.

However, instead of relying on the automatic reformulation we recommend to formulate the problem as conic problem from scratch because:

- it saves the computational overhead of the reformulation including the convexity check. A conic problem is convex by construction and hence no convexity check is neeeded for conic problems.
- usually the modeller can do a better reformulation than the automatic method because the modeller can exploit the knowledge of what is being modelled.

To summarize we recommend to formulate quadratic problems and in particular quadratically constrained problems directly in conic form.

7.4.2 Duality for Quadratic and Quadratically Constrained Optimization

The dual problem corresponding to the quadratic and quadratically constrained optimization problem (7.11) is given by

$$\begin{array}{ll} \text{maximize} & (l^c)^T s_l^c - (u^c)^T s_u^c + (l^x)^T s_l^x - (u^x)^T s_u^x + \frac{1}{2}x^T \left\{ \sum_{k=0}^{m-1} y_k Q^k - Q^o \right\} x + c^f \\ \text{subject to} & \\ & A^T y + s_l^x - s_u^x + \left\{ \sum_{k=0}^{m-1} y_k Q^k - Q^o \right\} x = c, \\ & -y + s_l^c - s_u^c = 0, \\ & s_l^c, s_u^c, s_l^x, s_u^x \geq 0. \end{array} \tag{7.12}$$

The dual problem is related to the dual problem for linear optimization (see Section *7.1.1*), but depends on the variable x which in general can not be eliminated. In the solutions reported by **MOSEK**, the value of x is the same for the primal problem (7.11) and the dual problem (7.12).

7.4.3 Infeasibility for Quadratic and Quadratically Constrained Optimization

In case **MOSEK** finds a problem to be infeasible it reports a certificate of infeasibility. This works exactly as for linear problems (see Section *7.1.2*).

Primal Infeasible Problems

If the problem (7.11) with all $Q^k = 0$ is infeasible, **MOSEK** will report a certificate of primal infeasibility. As the constraints are the same as for a linear problem, the certificate of infeasibility is the same as for linear optimization (see Section *7.1.2.1*).

Dual Infeasible Problems

If the problem (7.12) with all $Q^k = 0$ is infeasible, **MOSEK** will report a certificate of dual infeasibility. The primal solution reported is the certificate of infeasibility, and the dual solution is undefined.

A certificate of dual infeasibility is a feasible solution to the problem

$$\begin{array}{lccccc} \text{minimize} & & & c^T x & & \\ \text{subject to} & \hat{l}^c & \leq & Ax & \leq & \hat{u}^c, \\ & 0 & \leq & Q^o x & \leq & 0, \\ & \hat{l}^x & \leq & x & \leq & \hat{u}^x, \end{array}$$

where

$$\hat{l}_i^c = \left\{ \begin{array}{ll} 0 & \text{if } l_i^c > -\infty, \\ -\infty & \text{otherwise,} \end{array} \right\} \quad \text{and} \quad \hat{u}_i^c := \left\{ \begin{array}{ll} 0 & \text{if } u_i^c < \infty, \\ \infty & \text{otherwise,} \end{array} \right\}$$

and

$$\hat{l}_j^x = \left\{ \begin{array}{ll} 0 & \text{if } l_j^x > -\infty, \\ -\infty & \text{otherwise,} \end{array} \right\} \quad \text{and} \quad \hat{u}_j^x := \left\{ \begin{array}{ll} 0 & \text{if } u_j^x < \infty, \\ \infty & \text{otherwise,} \end{array} \right\}$$

such that the objective value is strictly negative.

7.5 General Convex Optimization

MOSEK is capable of solving smooth (twice differentiable) convex nonlinear optimization problems of the form

$$\begin{array}{lccccc} \text{minimize} & & & f(x) + c^T x + c^f & & \\ \text{subject to} & l^c & \leq & g(x) + Ax & \leq & u^c, \\ & l^x & \leq & x & \leq & u^x, \end{array}$$

where

- m is the number of constraints.
- n is the number of decision variables.
- $x \in \mathbb{R}^n$ is a vector of decision variables.
- $c \in \mathbb{R}^n$ is the linear part objective function.
- $A \in \mathbb{R}^{m \times n}$ is the constraint matrix.
- $l^c \in \mathbb{R}^m$ is the lower limit on the activity for the constraints.
- $u^c \in \mathbb{R}^m$ is the upper limit on the activity for the constraints.
- $l^x \in \mathbb{R}^n$ is the lower limit on the activity for the variables.

- $u^x \in \mathbb{R}^n$ is the upper limit on the activity for the variables.
- $f : \mathbb{R}^n \to \mathbb{R}$ is a nonlinear function.
- $g : \mathbb{R}^n \to \mathbb{R}^m$ is a nonlinear vector function.

This means that the i-th constraint has the form

$$l_i^c \leq g_i(x) + \sum_{j=1}^{n} a_{ij} x_j \leq u_i^c.$$

The linear term Ax is included in $g(x)$ since it can be handled much more efficiently as a separate entity when optimizing.

The nonlinear functions f and g must be smooth in all $x \in [l^x; u^x]$. Moreover, $f(x)$ must be a convex function and $g_i(x)$ must satisfy

$$\begin{array}{rcl} -\infty < l_i^c & \Rightarrow & g_i(x) \text{ is concave,} \\ u_i^c < \infty & \Rightarrow & g_i(x) \text{ is convex,} \\ -\infty < l_i^c \leq u_i^c < \infty & \Rightarrow & g_i(x) = 0. \end{array}$$

7.5.1 Duality for General convex Optimization

Similar to the linear case, **MOSEK** reports dual information in the general nonlinear case. Indeed in this case the Lagrange function is defined by

$$\begin{array}{rcl} L(x, s_l^c, s_u^c, s_l^x, s_u^x) & := & f(x) + c^T x + c^f \\ & & -(s_l^c)^T (g(x) + Ax - l^c) - (s_u^c)^T (u^c - g(x) - Ax) \\ & & -(s_l^x)^T (x - l^x) - (s_u^x)^T (u^x - x), \end{array}$$

and the dual problem is given by

$$\begin{array}{lcl} \text{maximize} & L(x, s_l^c, s_u^c, s_l^x, s_u^x) & \\ \text{subject to} & \nabla_x L(x, s_l^c, s_u^c, s_l^x, s_u^x)^T & = \quad 0, \\ & s_l^c, s_u^c, s_l^x, s_u^x \geq 0, & \end{array}$$

which is equivalent to

$$\begin{array}{lcll} \text{maximize} & (l^c)^T s_l^c - (u^c)^T s_u^c + (l^x)^T s_l^x - (u^x)^T s_u^x + c^f & & \\ & +f(x) - g(x)^T y - (\nabla f(x)^T - \nabla g(x)^T y)^T x & & \\ \text{subject to} & A^T y + s_l^x - s_u^x - (\nabla f(x)^T - \nabla g(x)^T y) & = & c, \\ & -y + s_l^c - s_u^c & = & 0, \\ & s_l^c, s_u^c, s_l^x, s_u^x \geq 0. & & \end{array}$$

In this context we use the following definition for scalar functions

$$\nabla f(x) \quad = \quad \left[\frac{\partial f(x)}{\partial x_1}, \ldots, \frac{\partial f(x)}{\partial x_n} \right],$$

and accordingly for vector functions

$$\nabla g(x) \quad = \quad \begin{bmatrix} \nabla g_1(x) \\ \vdots \\ \nabla g_m(x) \end{bmatrix}.$$

CHAPTER

EIGHT

THE OPTIMIZERS FOR CONTINUOUS PROBLEMS

The most essential part of **MOSEK** are the optimizers. This chapter describes the optimizers for the class of *continuous problems* without integer variables, that is:

- linear problems,
- conic problems (quadratic and semidefinite),
- general convex problems.

MOSEK offers an interior-point optimizer for each class of problems and also a simplex optimizer for linear problems. The structure of a successful optimization process is roughly:

- **Presolve**
  1. *Elimination*: Reduce the size of the problem.
  2. *Dualizer*: Choose whether to solve the primal or the dual form of the problem.
  3. *Scaling*: Scale the problem for better numerical stability.
- **Optimization**
  1. *Optimize*: Solve the problem using selected method.
  2. *Terminate*: Stop the optimization when specific termination criteria have been met.
  3. *Report*: Return the solution or an infeasibility certificate.

The preprocessing stage is transparent to the user, but useful to know about for tuning purposes. The purpose of the preprocessing steps is to make the actual optimization more efficient and robust. We discuss the details of the above steps in the following sections.

8.1 Presolve

Before an optimizer actually performs the optimization the problem is preprocessed using the so-called presolve. The purpose of the presolve is to

1. remove redundant constraints,
2. eliminate fixed variables,
3. remove linear dependencies,
4. substitute out (implied) free variables, and
5. reduce the size of the optimization problem in general.

After the presolved problem has been optimized the solution is automatically postsolved so that the returned solution is valid for the original problem. Hence, the presolve is completely transparent. For further details about the presolve phase, please see *[AA95]* and *[AGMX96]*.

It is possible to fine-tune the behavior of the presolve or to turn it off entirely. If presolve consumes too much time or memory compared to the reduction in problem size gained it may be disabled. This

is done by setting the parameter *MSK_IPAR_PRESOLVE_USE* to *MSK_PRESOLVE_MODE_OFF*. The two most time-consuming steps of the presolve are

- the eliminator, and
- the linear dependency check.

Therefore, in some cases it is worthwhile to disable one or both of these.

Numerical issues in the presolve

During the presolve the problem is reformulated so that it hopefully solves faster. However, in rare cases the presolved problem may be harder to solve then the original problem. The presolve may also be infeasible although the original problem is not. If it is suspected that presolved problem is much harder to solve than the original, we suggest to first turn the eliminator off by setting the parameter *MSK_IPAR_PRESOLVE_ELIMINATOR_MAX_NUM_TRIES* to 0. If that does not help, then trying to turn entire presolve off may help.

Since all computations are done in finite precision, the presolve employs some tolerances when concluding a variable is fixed or a constraint is redundant. If it happens that **MOSEK** incorrectly concludes a problem is primal or dual infeasible, then it is worthwhile to try to reduce the parameters *MSK_DPAR_PRESOLVE_TOL_X* and *MSK_DPAR_PRESOLVE_TOL_S*. However, if reducing the parameters actually helps then this should be taken as an indication that the problem is badly formulated.

Eliminator

The purpose of the eliminator is to eliminate free and implied free variables from the problem using substitution. For instance, given the constraints

$$\begin{array}{rcl} y & = & \sum_j x_j, \\ y, x & \geq & 0, \end{array}$$

y is an implied free variable that can be substituted out of the problem, if deemed worthwhile. If the eliminator consumes too much time or memory compared to the reduction in problem size gained it may be disabled. This can be done by setting the parameter *MSK_IPAR_PRESOLVE_ELIMINATOR_MAX_NUM_TRIES* to 0. In rare cases the eliminator may cause that the problem becomes much hard to solve.

Linear dependency checker

The purpose of the linear dependency check is to remove linear dependencies among the linear equalities. For instance, the three linear equalities

$$\begin{array}{rcl} x_1 + x_2 + x_3 & = & 1, \\ x_1 + 0.5x_2 & = & 0.5, \\ 0.5x_2 + x_3 & = & 0.5. \end{array}$$

contain exactly one linear dependency. This implies that one of the constraints can be dropped without changing the set of feasible solutions. Removing linear dependencies is in general a good idea since it reduces the size of the problem. Moreover, the linear dependencies are likely to introduce numerical problems in the optimization phase. It is best practice to build models without linear dependencies, but that is not always easy for the user to control. If the linear dependencies are removed at the modelling stage, the linear dependency check can safely be disabled by setting the parameter *MSK_IPAR_PRESOLVE_LINDEP_USE* to *MSK_OFF*.

Dualizer

All linear, conic, and convex optimization problems have an equivalent dual problem associated with them. **MOSEK** has built-in heuristics to determine if it is more efficient to solve the primal or dual

problem. The form (primal or dual) is displayed in the **MOSEK** log and available as an information item from the solver. Should the internal heuristics not choose the most efficient form of the problem it may be worthwhile to set the dualizer manually by setting the parameters:

- *MSK_IPAR_INTPNT_SOLVE_FORM*: In case of the interior-point optimizer.
- *MSK_IPAR_SIM_SOLVE_FORM*: In case of the simplex optimizer.

Note that currently only linear and conic quadratic problems may be automatically dualized.

Scaling

Problems containing data with large and/or small coefficients, say $1.0e+9$ or $1.0e-7$, are often hard to solve. Significant digits may be truncated in calculations with finite precision, which can result in the optimizer relying on inaccurate data. Since computers work in finite precision, extreme coefficients should be avoided. In general, data around the same *order of magnitude* is preferred, and we will refer to a problem, satisfying this loose property, as being *well-scaled*. If the problem is not well scaled, **MOSEK** will try to scale (multiply) constraints and variables by suitable constants. **MOSEK** solves the scaled problem to improve the numerical properties.

The scaling process is transparent, i.e. the solution to the original problem is reported. It is important to be aware that the optimizer terminates when the termination criterion is met on the scaled problem, therefore significant primal or dual infeasibilities may occur after unscaling for badly scaled problems. The best solution of this issue is to reformulate the problem, making it better scaled.

By default **MOSEK** heuristically chooses a suitable scaling. The scaling for interior-point and simplex optimizers can be controlled with the parameters *MSK_IPAR_INTPNT_SCALING* and *MSK_IPAR_SIM_SCALING* respectively.

8.2 Using Multiple Threads in an Optimizer

Multithreading in interior-point optimizers

The interior-point optimizers in **MOSEK** have been parallelized. This means that if you solve linear, quadratic, conic, or general convex optimization problem using the interior-point optimizer, you can take advantage of multiple CPU's. By default **MOSEK** will automatically select the number of threads to be employed when solving the problem. However, the maximum number of threads employed can be changed by setting the parameter *MSK_IPAR_NUM_THREADS*. This should never exceed the number of cores on the computer.

The speed-up obtained when using multiple threads is highly problem and hardware dependent, and consequently, it is advisable to compare single threaded and multi threaded performance for the given problem type to determine the optimal settings. For small problems, using multiple threads is not be worthwhile and may even be counter productive because of the additional coordination overhead. Therefore, it may be advantageous to disable multithreading using the parameter *MSK_IPAR_INTPNT_MULTI_THREAD*.

The interior-point optimizer parallelizes big tasks such linear algebra computations.

Thread Safety

The **MOSEK** API is thread-safe provided that a task is only modified or accessed from one thread at any given time. Also accessing two or more separate tasks from threads at the same time is safe. Sharing an environment between threads is safe.

Determinism

The optimizers are run-to-run deterministic which means if a problem is solved twice on the same computer using the same parameter setting and exactly the same input then exactly the same results is obtained. One restriction is that no time limits must be imposed because the time taken to perform an operation on a computer is dependent on many factors such as the current workload.

8.3 Linear Optimization

8.3.1 Optimizer Selection

Two different types of optimizers are available for linear problems: The default is an interior-point method, and the alternative is the simplex method (primal or dual). The optimizer can be selected using the parameter *MSK_IPAR_OPTIMIZER*.

The Interior-point or the Simplex Optimizer?

Given a linear optimization problem, which optimizer is the best: the simplex or the interior-point optimizer? It is impossible to provide a general answer to this question. However, the interior-point optimizer behaves more predictably: it tends to use between 20 and 100 iterations, almost independently of problem size, but cannot perform warm-start. On the other hand the simplex method can take advantage of an initial solution, but is less predictable from cold-start. The interior-point optimizer is used by default.

The Primal or the Dual Simplex Variant?

MOSEK provides both a primal and a dual simplex optimizer. Predicting which simplex optimizer is faster is impossible, however, in recent years the dual optimizer has seen several algorithmic and computational improvements, which, in our experience, make it faster on average than the primal version. Still, it depends much on the problem structure and size. Setting the *MSK_IPAR_OPTIMIZER* parameter to *MSK_OPTIMIZER_FREE_SIMPLEX* instructs **MOSEK** to choose one of the simplex variants automatically.

To summarize, if you want to know which optimizer is faster for a given problem type, it is best to try all the options.

8.3.2 The Interior-point Optimizer

The purpose of this section is to provide information about the algorithm employed in the **MOSEK** interior-point optimizer for linear problems and about its termination criteria.

The homogeneous primal-dual problem

In order to keep the discussion simple it is assumed that **MOSEK** solves linear optimization problems of standard form

$$\begin{array}{lll} \text{minimize} & c^T x & \\ \text{subject to} & Ax & = b, \\ & x \geq 0. & \end{array} \tag{8.1}$$

This is in fact what happens inside **MOSEK**; for efficiency reasons **MOSEK** converts the problem to standard form before solving, then converts it back to the input form when reporting the solution.

Since it is not known beforehand whether problem (8.1) has an optimal solution, is primal infeasible or is dual infeasible, the optimization algorithm must deal with all three situations. This is the reason why **MOSEK** solves the so-called homogeneous model

$$\begin{array}{rcl} Ax - b\tau & = & 0, \\ A^T y + s - c\tau & = & 0, \\ -c^T x + b^T y - \kappa & = & 0, \\ x, s, \tau, \kappa & \geq & 0, \end{array} \tag{8.2}$$

where y and s correspond to the dual variables in (8.1), and τ and κ are two additional scalar variables. Note that the homogeneous model (8.2) always has solution since

$$(x, y, s, \tau, \kappa) = (0, 0, 0, 0, 0)$$

is a solution, although not a very interesting one. Any solution

$$(x^*, y^*, s^*, \tau^*, \kappa^*)$$

to the homogeneous model (8.2) satisfies

$$x_j^* s_j^* = 0 \text{ and } \tau^* \kappa^* = 0.$$

Moreover, there is always a solution that has the property $\tau^* + \kappa^* > 0$.

First, assume that $\tau^* > 0$. It follows that

$$\begin{array}{rcl} A\frac{x^*}{\tau^*} & = & b, \\ A^T \frac{y^*}{\tau^*} + \frac{s^*}{\tau^*} & = & c, \\ -c^T \frac{x^*}{\tau^*} + b^T \frac{y^*}{\tau^*} & = & 0, \\ x^*, s^*, \tau^*, \kappa^* & \geq & 0. \end{array}$$

This shows that $\frac{x^*}{\tau^*}$ is a primal optimal solution and $(\frac{y^*}{\tau^*}, \frac{s^*}{\tau *})$ is a dual optimal solution; this is reported as the optimal interior-point solution since

$$(x, y, s) = \left\{ \frac{x^*}{\tau^*}, \frac{y^*}{\tau^*}, \frac{s^*}{\tau^*} \right\}$$

is a primal-dual optimal solution (see Section *7.1* for the mathematical background on duality and optimality).

On other hand, if $\kappa^* > 0$ then

$$\begin{array}{rcl} Ax^* & = & 0, \\ A^T y^* + s^* & = & 0, \\ -c^T x^* + b^T y^* & = & \kappa^*, \\ x^*, s^*, \tau^*, \kappa^* & \geq & 0. \end{array}$$

This implies that at least one of

$$c^T x^* < 0 \tag{8.3}$$

or

$$b^T y^* > 0 \tag{8.4}$$

is satisfied. If (8.3) is satisfied then x^* is a certificate of dual infeasibility, whereas if (8.4) is satisfied then y^* is a certificate of primal infeasibility.

In summary, by computing an appropriate solution to the homogeneous model, all information required for a solution to the original problem is obtained. A solution to the homogeneous model can be computed using a primal-dual interior-point algorithm *[And09]*.

Interior-point Termination Criterion

For efficiency reasons it is not practical to solve the homogeneous model exactly. Hence, an exact optimal solution or an exact infeasibility certificate cannot be computed and a reasonable termination criterion has to be employed.

In the k-th iteration of the interior-point algorithm a trial solution

$$(x^k, y^k, s^k, \tau^k, \kappa^k)$$

to homogeneous model is generated, where

$$x^k, s^k, \tau^k, \kappa^k > 0.$$

Optimal case

Whenever the trial solution satisfies the criterion

$$\begin{array}{rcl} \left\| A\frac{x^k}{\tau^k} - b \right\|_\infty & \leq & \epsilon_p(1 + \|b\|_\infty), \\ \left\| A^T\frac{y^k}{\tau^k} + \frac{s^k}{\tau^k} - c \right\|_\infty & \leq & \epsilon_d(1 + \|c\|_\infty), \text{ and} \\ \min\left(\frac{(x^k)^T s^k}{(\tau^k)^2}, |\frac{c^T x^k}{\tau^k} - \frac{b^T y^k}{\tau^k}|\right) & \leq & \epsilon_g \max\left(1, \frac{\min(|c^T x^k|, |b^T y^k|)}{\tau^k}\right), \end{array} \tag{8.5}$$

the interior-point optimizer is terminated and

$$\frac{(x^k, y^k, s^k)}{\tau^k}$$

is reported as the primal-dual optimal solution. The interpretation of (8.5) is that the optimizer is terminated if

- $\frac{x^k}{\tau^k}$ is approximately primal feasible,
- $\left\{\frac{y^k}{\tau^k}, \frac{s^k}{\tau^k}\right\}$ is approximately dual feasible, and
- the duality gap is almost zero.

Dual infeasibility certificate

On the other hand, if the trial solution satisfies

$$-\epsilon_i c^T x^k > \frac{\|c\|_\infty}{\max(1, \|b\|_\infty)} \left\|Ax^k\right\|_\infty$$

then the problem is declared dual infeasible and x^k is reported as a certificate of dual infeasibility. The motivation for this stopping criterion is as follows: First assume that $\left\|Ax^k\right\|_\infty = 0$; then x^k is an exact certificate of dual infeasibility. Next assume that this is not the case, i.e.

$$\left\|Ax^k\right\|_\infty > 0,$$

and define

$$\bar{x} := \epsilon_i \frac{\max(1, \|b\|_\infty)}{\|Ax^k\|_\infty \|c\|_\infty} x^k.$$

It is easy to verify that

$$\|A\bar{x}\|_\infty = \epsilon_i \frac{\max(1, \|b\|_\infty)}{\|c\|_\infty} \text{ and } -c^T\bar{x} > 1,$$

which shows $\bar{x}$ is an approximate certificate of dual infeasibility, where ε_i controls the quality of the approximation. A smaller value means a better approximation.

Primal infeasibility certificate

Finally, if

$$\epsilon_i b^T y^k > \frac{\|b\|_\infty}{\max(1, \|c\|_\infty)} \left\|A^T y^k + s^k\right\|_\infty$$

then y^k is reported as a certificate of primal infeasibility.

Adjusting optimality criteria and near optimality

It is possible to adjust the tolerances ε_p, ε_d, ε_g and ε_i using parameters; see table for details.

Table 8.1: Parameters employed in termination criterion

ToleranceParameter	name
ε_p	*MSK_DPAR_INTPNT_TOL_PFEAS*
ε_d	*MSK_DPAR_INTPNT_TOL_DFEAS*
ε_g	*MSK_DPAR_INTPNT_TOL_REL_GAP*
ε_i	*MSK_DPAR_INTPNT_TOL_INFEAS*

The default values of the termination tolerances are chosen such that for a majority of problems appearing in practice it is not possible to achieve much better accuracy. Therefore, tightening the tolerances usually is not worthwhile. However, an inspection of (8.5) reveals that the quality of the solution depends on $\|b\|_\infty$ and $\|c\|_\infty$; the smaller the norms are, the better the solution accuracy.

The interior-point method as implemented by **MOSEK** will converge toward optimality and primal and dual feasibility at the same rate *[And09]*. This means that if the optimizer is stopped prematurely then it is very unlikely that either the primal or dual solution is feasible. Another consequence is that in most cases all the tolerances, ε_p, ε_d, ε_g and ε_i, have to be relaxed together to achieve an effect.

In some cases the interior-point method terminates having found a solution not too far from meeting the optimality condition (8.5). A solution is defined as *near optimal* if scaling the termination tolerances ε_p, ε_d, ε_g and ε_g by the same factor $\varepsilon_n \in [1.0, +\infty]$ makes the condition (8.5) satisfied. A near optimal solution is therefore of lower quality but still potentially valuable. If for instance the solver stalls, i.e. it can make no more significant progress towards the optimal solution, a near optimal solution could be available and be good enough for the user. Near infeasibility certificates are defined similarly. The value of ε_n can be adjusted with the parameter *MSK_DPAR_INTPNT_CO_TOL_NEAR_REL*.

The basis identification discussed in Section *8.3.2.4* requires an optimal solution to work well; hence basis identification should be turned off if the termination criterion is relaxed.

To conclude the discussion in this section, relaxing the termination criterion is usually not worthwhile.

Basis Identification

An interior-point optimizer does not return an optimal basic solution unless the problem has a unique primal and dual optimal solution. Therefore, the interior-point optimizer has an optional post-processing step that computes an optimal basic solution starting from the optimal interior-point solution. More information about the basis identification procedure may be found in *[AY96]*. In the following we provide an overall idea of the procedure.

There are some cases in which a basic solution could be more valuable:

- a basic solution is often more accurate than an interior-point solution,
- a basic solution can be used to warm-start the simplex algorithm in case of reoptimization,
- a basic solution is in general more sparse, i.e. more variables are fixed to zero. This is particularly appealing when solving continuous relaxations of mixed integer problems, as well as in all applications in which sparser solutions are preferred.

To illustrate how the basis identification routine works, we use the following trivial example:

$$\begin{array}{lll} \text{minimize} & x+y & \\ \text{subject to} & x+y & = \quad 1, \\ & x,y \geq 0. & \end{array}$$

It is easy to see that all feasible solutions are also optimal. In particular, there are two basic solutions, namely

$$\begin{array}{rcl} (x_1^*, y_1^*) & = & (1,0), \\ (x_2^*, y_2^*) & = & (0,1). \end{array}$$

The interior point algorithm will actually converge to the center of the optimal set, i.e. to $(x^*, y^*) = (1/2, 1/2)$ (to see this in **MOSEK** deactivate *Presolve*).

In practice, when the algorithm gets close to the optimal solution, it is possible to construct in polynomial time an initial basis for the simplex algorithm from the current interior point solution. This basis is used to warm-start the simplex algorithm that will provide the optimal basic solution. In most cases the constructed basis is optimal, or very few iterations are required by the simplex algorithm to make it optimal and hence the final *clean-up* phase be short. However, for some cases of ill-conditioned problems the additional simplex clean up phase may take of lot a time.

By default **MOSEK** performs a basis identification. However, if a basic solution is not needed, the basis identification procedure can be turned off. The parameters

- *MSK_IPAR_INTPNT_BASIS*,
- *MSK_IPAR_BI_IGNORE_MAX_ITER*, and
- *MSK_IPAR_BI_IGNORE_NUM_ERROR*

control when basis identification is performed.

The type of simplex algorithm to be used (primal/dual) can be tuned with the parameter *MSK_IPAR_BI_CLEAN_OPTIMIZER*, and the maximum number of iterations can be set with *MSK_IPAR_BI_MAX_ITERATIONS*.

Finally, it should be mentioned that there is no guarantee on which basic solution will be returned.

The Interior-point Log

Below is a typical log output from the interior-point optimizer:

```
Optimizer  - threads                : 1
Optimizer  - solved problem         : the dual
Optimizer  - Constraints            : 2
Optimizer  - Cones                  : 0
Optimizer  - Scalar variables       : 6                 conic                  : 0
Optimizer  - Semi-definite variables: 0                 scalarized             : 0
Factor     - setup time             : 0.00              dense det. time        : 0.00
Factor     - ML order time          : 0.00              GP order time          : 0.00
Factor     - nonzeros before factor : 3                 after factor           : 3
Factor     - dense dim.             : 0                 flops                  : 7.00e+001
ITE PFEAS    DFEAS    GFEAS    PRSTATUS   POBJ              DOBJ              MU       TIME
0   1.0e+000 8.6e+000 6.1e+000 1.00e+000  0.000000000e+000  -2.208000000e+003 1.0e+000 0.00
1   1.1e+000 2.5e+000 1.6e-001 0.00e+000  -7.901380925e+003 -7.394611417e+003 2.5e+000 0.00
2   1.4e-001 3.4e-001 2.1e-002 8.36e-001  -8.113031650e+003 -8.055866001e+003 3.3e-001 0.00
3   2.4e-002 5.8e-002 3.6e-003 1.27e+000  -7.777530698e+003 -7.766471080e+003 5.7e-002 0.01
4   1.3e-004 3.2e-004 2.0e-005 1.08e+000  -7.668323435e+003 -7.668207177e+003 3.2e-004 0.01
5   1.3e-008 3.2e-008 2.0e-009 1.00e+000  -7.668000027e+003 -7.668000015e+003 3.2e-008 0.01
6   1.3e-012 3.2e-012 2.0e-013 1.00e+000  -7.667999994e+003 -7.667999994e+003 3.2e-012 0.01
```

The first line displays the number of threads used by the optimizer and the second line tells that the optimizer chose to solve the dual problem rather than the primal problem. The next line displays the

problem dimensions as seen by the optimizer, and the `Factor...` lines show various statistics. This is followed by the iteration log.

Using the same notation as in Section *8.3.2* the columns of the iteration log have the following meaning:

- `ITE`: Iteration index k.
- `PFEAS`: $\left\|Ax^k - b\tau^k\right\|_\infty$. The numbers in this column should converge monotonically towards zero but may stall at low level due to rounding errors.
- `DFEAS`: $\left\|A^T y^k + s^k - c\tau^k\right\|_\infty$. The numbers in this column should converge monotonically towards zero but may stall at low level due to rounding errors.
- `GFEAS`: $|-c^T x^k + b^T y^k - \kappa^k|$. The numbers in this column should converge monotonically towards zero but may stall at low level due to rounding errors.
- `PRSTATUS`: This number converges to 1 if the problem has an optimal solution whereas it converges to -1 if that is not the case.
- `POBJ`: $c^T x^k/\tau^k$. An estimate for the primal objective value.
- `DOBJ`: $b^T y^k/\tau^k$. An estimate for the dual objective value.
- `MU`: $\frac{(x^k)^T s^k + \tau^k \kappa^k}{n+1}$. The numbers in this column should always converge to zero.
- `TIME`: Time spent since the optimization started.

8.3.3 The Simplex Optimizer

An alternative to the interior-point optimizer is the simplex optimizer. The simplex optimizer uses a different method that allows exploiting an initial guess for the optimal solution to reduce the solution time. Depending on the problem it may be faster or slower to use an initial guess; see section *8.3.1* for a discussion. **MOSEK** provides both a primal and a dual variant of the simplex optimizer.

Simplex Termination Criterion

The simplex optimizer terminates when it finds an optimal basic solution or an infeasibility certificate. A basic solution is optimal when it is primal and dual feasible; see Section *7.1* for a definition of the primal and dual problem. Due to the fact that computations are performed in finite precision **MOSEK** allows violations of primal and dual feasibility within certain tolerances. The user can control the allowed primal and dual tolerances with the parameters *MSK_DPAR_BASIS_TOL_X* and *MSK_DPAR_BASIS_TOL_S*.

Setting the parameter *MSK_IPAR_OPTIMIZER* to *MSK_OPTIMIZER_FREE_SIMPLEX* instructs **MOSEK** to select automatically between the primal and the dual simplex optimizers. Hence, **MOSEK** tries to choose the best optimizer for the given problem and the available solution. The same parameter can also be used to force one of the variants.

Starting From an Existing Solution

When using the simplex optimizer it may be possible to reuse an existing solution and thereby reduce the solution time significantly. When a simplex optimizer starts from an existing solution it is said to perform a *warm-start*. If the user is solving a sequence of optimization problems by solving the problem, making modifications, and solving again, **MOSEK** will warm-start automatically.

By default **MOSEK** uses presolve when performing a warm-start. If the optimizer only needs very few iterations to find the optimal solution it may be better to turn off the presolve.

Numerical Difficulties in the Simplex Optimizers

Though **MOSEK** is designed to minimize numerical instability, completely avoiding it is impossible when working in finite precision. **MOSEK** treats a "numerically unexpected behavior" event inside the optimizer as a *set-back*. The user can define how many set-backs the optimizer accepts; if that number is exceeded, the optimization will be aborted. Set-backs are a way to escape long sequences where the optimizer tries to recover from an unstable situation.

Examples of set-backs are: repeated singularities when factorizing the basis matrix, repeated loss of feasibility, degeneracy problems (no progress in objective) and other events indicating numerical difficulties. If the simplex optimizer encounters a lot of set-backs the problem is usually badly scaled; in such a situation try to reformulate it into a better scaled problem. Then, if a lot of set-backs still occur, trying one or more of the following suggestions may be worthwhile:

- Raise tolerances for allowed primal or dual feasibility: increase the value of
  - *MSK_DPAR_BASIS_TOL_X*, and
  - *MSK_DPAR_BASIS_TOL_S*.
- Raise or lower pivot tolerance: Change the *MSK_DPAR_SIMPLEX_ABS_TOL_PIV* parameter.
- Switch optimizer: Try another optimizer.
- Switch off crash: Set both *MSK_IPAR_SIM_PRIMAL_CRASH* and *MSK_IPAR_SIM_DUAL_CRASH* to 0.
- Experiment with other pricing strategies: Try different values for the parameters
  - *MSK_IPAR_SIM_PRIMAL_SELECTION* and
  - *MSK_IPAR_SIM_DUAL_SELECTION*.
- If you are using warm-starts, in rare cases switching off this feature may improve stability. This is controlled by the *MSK_IPAR_SIM_HOTSTART* parameter.
- Increase maximum number of set-backs allowed controlled by *MSK_IPAR_SIM_MAX_NUM_SETBACKS*.
- If the problem repeatedly becomes infeasible try switching off the special degeneracy handling. See the parameter *MSK_IPAR_SIM_DEGEN* for details.

The Simplex Log

Below is a typical log output from the simplex optimizer:

```
Optimizer  - solved problem         : the primal
Optimizer  - Constraints            : 667
Optimizer  - Scalar variables       : 1424              conic                  : 0
Optimizer  - hotstart               : no
ITER      DEGITER(%)  PFEAS       DFEAS       POBJ                   DOBJ                   TIME␣
 ↪      TOTTIME
0           0.00        1.43e+05    NA          6.5584140832e+03       NA                     0.00␣
 ↪      0.02
1000        1.10        0.00e+00    NA          1.4588289726e+04       NA                     0.13␣
 ↪      0.14
2000        0.75        0.00e+00    NA          7.3705564855e+03       NA                     0.21␣
 ↪      0.22
3000        0.67        0.00e+00    NA          6.0509727712e+03       NA                     0.29␣
 ↪      0.31
4000        0.52        0.00e+00    NA          5.5771203906e+03       NA                     0.38␣
 ↪      0.39
4533        0.49        0.00e+00    NA          5.5018458883e+03       NA                     0.42␣
 ↪      0.44
```

The first lines summarize the problem the optimizer is solving. This is followed by the iteration log, with the following meaning:

- `ITER`: Number of iterations.
- `DEGITER(%)`: Ratio of degenerate iterations.
- `PFEAS`: Primal feasibility measure reported by the simplex optimizer. The numbers should be 0 if the problem is primal feasible (when the primal variant is used).
- `DFEAS`: Dual feasibility measure reported by the simplex optimizer. The number should be 0 if the problem is dual feasible (when the dual variant is used).
- `POBJ`: An estimate for the primal objective value (when the primal variant is used).
- `DOBJ`: An estimate for the dual objective value (when the dual variant is used).
- `TIME`: Time spent since this instance of the simplex optimizer was invoked (in seconds).
- `TOTTIME`: Time spent since optimization started (in seconds).

8.4 Conic Optimization

For conic optimization problems only an interior-point type optimizer is available.

8.4.1 The Interior-point optimizer

The homogeneous primal-dual problem

The interior-point optimizer is an implementation of the so-called homogeneous and self-dual algorithm. For a detailed description of the algorithm, please see *[ART03]*. In order to keep our discussion simple we will assume that **MOSEK** solves a conic optimization problem of the form:

$$\begin{array}{lll} \text{minimize} & c^T x & \\ \text{subject to} & Ax & = b, \\ & x \in \mathcal{K} & \end{array} \tag{8.6}$$

where K is a convex cone. The corresponding dual problem is

$$\begin{array}{lll} \text{maximize} & b^T y & \\ \text{subject to} & A^T y + s & = c, \\ & x \in \mathcal{K}^* & \end{array} \tag{8.7}$$

where $\mathcal{K}^*$ is the dual cone of $\mathcal{K}$. See Section *7.2* for definitions.

Since it is not known beforehand whether problem (8.6) has an optimal solution, is primal infeasible or is dual infeasible, the optimization algorithm must deal with all three situations. This is the reason that **MOSEK** solves the so-called homogeneous model

$$\begin{array}{rcl} Ax - b\tau & = & 0, \\ A^T y + s - c\tau & = & 0, \\ -c^T x + b^T y - \kappa & = & 0, \\ x & \in & \mathcal{K}, \\ s & \in & \mathcal{K}^*, \\ \tau, \kappa & \geq & 0, \end{array} \tag{8.8}$$

where y and s correspond to the dual variables in (8.6), and τ and κ are two additional scalar variables. Note that the homogeneous model (8.8) always has a solution since

$$(x, y, s, \tau, \kappa) = (0, 0, 0, 0, 0)$$

is a solution, although not a very interesting one. Any solution

$$(x^*, y^*, s^*, \tau^*, \kappa^*)$$

to the homogeneous model (8.8) satisfies

$$(x^*)^T s^* + \tau^* \kappa^* = 0$$

i.e. complementarity. Observe that $x^* \in \mathcal{K}$ and $s^* \in \mathcal{K}^*$ implies

$$(x^*)^T s^* \geq 0$$

and therefore

$$\tau^* \kappa^* = 0.$$

since $\tau^*, \kappa^* \geq 0$. Hence, at least one of τ^* and κ^* is zero.

First, assume that $\tau^* > 0$ and hence $\kappa^* = 0$. It follows that

$$\begin{array}{rcl} A\frac{x^*}{\tau^*} & = & b, \\ A^T\frac{y^*}{\tau^*} + \frac{s^*}{\tau^*} & = & c, \\ -c^T\frac{x^*}{\tau^*} + b^T\frac{y^*}{\tau^*} & = & 0, \\ x^*/\tau^* & \in & \mathcal{K}, \\ s^*/\tau^* & \in & \mathcal{K}^*. \end{array}$$

This shows that $\frac{x^*}{\tau^*}$ is a primal optimal solution and $(\frac{y^*}{\tau^*}, \frac{s^*}{\tau^*})$ is a dual optimal solution; this is reported as the optimal interior-point solution since

$$(x, y, s) = \left(\frac{x^*}{\tau^*}, \frac{y^*}{\tau^*}, \frac{s^*}{\tau^*}\right)$$

is a primal-dual optimal solution.

On other hand, if $\kappa^* > 0$ then

$$\begin{array}{rcl} Ax^* & = & 0, \\ A^T y^* + s^* & = & 0, \\ -c^T x^* + b^T y^* & = & \kappa^*, \\ x^* & \in & \mathcal{K}, \\ s^* & \in & \mathcal{K}^*. \end{array}$$

This implies that at least one of

$$c^T x^* < 0 \tag{8.9}$$

or

$$b^T y^* > 0 \tag{8.10}$$

holds. If (8.9) is satisfied, then x^* is a certificate of dual infeasibility, whereas if (8.10) holds then y^* is a certificate of primal infeasibility.

In summary, by computing an appropriate solution to the homogeneous model, all information required for a solution to the original problem is obtained. A solution to the homogeneous model can be computed using a primal-dual interior-point algorithm *[And09]*.

Interior-point Termination Criterion

Since computations are performed in finite precision, and for efficiency reasons, it is not possible to solve the homogeneous model exactly in general. Hence, an exact optimal solution or an exact infeasibility certificate cannot be computed and a reasonable termination criterion has to be employed.

In every iteration k of the interior-point algorithm a trial solution

$$(x^k, y^k, s^k, \tau^k, \kappa^k)$$

to the homogeneous model is generated, where

$$x^k \in \mathcal{K}, s^k \in \mathcal{K}^*, \tau^k, \kappa^k > 0.$$

Therefore, it is possible to compute the values:

$$\begin{array}{rcl}
\rho_p^k & = & \arg\min_\rho \left\{\rho \mid \left\|A\frac{x^k}{\tau^k} - b\right\|_\infty \leq \rho\varepsilon_p(1 + \|b\|_\infty)\right\}, \\
\rho_d^k & = & \arg\min_\rho \left\{\rho \mid \left\|A^T\frac{y^k}{\tau^k} + \frac{s^k}{\tau^k} - c\right\|_\infty \leq \rho\varepsilon_d(1 + \|c\|_\infty)\right\}, \\
\rho_g^k & = & \arg\min_\rho \left\{\rho \mid \left(\frac{(x^k)^T s^k}{(\tau^k)^2}, |\frac{c^T x^k}{\tau^k} - \frac{b^T y^k}{\tau^k}|\right) \leq \rho\varepsilon_g \max\left(1, \frac{\min(|c^T x^k|, |b^T y^k|)}{\tau^k}\right)\right\}, \\
\rho_{pi}^k & = & \arg\min_\rho \left\{\rho \mid \left\|A^T y^k + s^k\right\|_\infty \leq \rho\varepsilon_i b^T y^k,\ b^T y^k > 0\right\} \text{ and} \\
\rho_{di}^k & = & \arg\min_\rho \left\{\rho \mid \left\|Ax^k\right\|_\infty \leq -\rho\varepsilon_i c^T x^k,\ c^T x^k < 0\right\}.
\end{array}$$

Note $\varepsilon_p, \varepsilon_d, \varepsilon_g$ and ε_i are nonnegative user specified tolerances.

Optimal Case

Observe ρ_p^k measures how far x^k/τ^k is from being a good approximate primal feasible solution. Indeed if $\rho_p^k \leq 1$, then

$$\left\|A\frac{x^k}{\tau^k} - b\right\|_\infty \leq \varepsilon_p(1 + \|b\|_\infty). \tag{8.11}$$

This shows the violations in the primal equality constraints for the solution x^k/τ^k is small compared to the size of b given ε_p is small.

Similarly, if $\rho_d^k \leq 1$, then $(y^k, s^k)/\tau^k$ is an approximate dual feasible solution. If in addition $\rho_g \leq 1$, then the solution $(x^k, y^k, s^k)/\tau^k$ is approximate optimal because the associated primal and dual objective values are almost identical.

In other words if $\max(\rho_p^k, \rho_d^k, \rho_g^k) \leq 1$, then

$$\frac{(x^k, y^k, s^k)}{\tau^k}$$

is an approximate optimal solution.

Dual Infeasibility Certificate

Next assume that $\rho_{di}^k \leq 1$ and hence

$$\left\|Ax^k\right\|_\infty \leq -\varepsilon_i c^T x^k \text{ and } -c^T x^k > 0$$

holds. Now in this case the problem is declared dual infeasible and x^k is reported as a certificate of dual infeasibility. The motivation for this stopping criterion is as follows. Let

$$\bar{x} := \frac{x^k}{-c^T x^k}$$

and it is easy to verify that

$$\|A\bar{x}\|_\infty \leq \varepsilon_i \text{ and } c^T\bar{x} = -1$$

which shows $\bar{x}$ is an approximate certificate of dual infeasibility, where ε_i controls the quality of the approximation.

Primal Infeasiblity Certificate

Next assume that $\rho_{pi}^k \leq 1$ and hence

$$\left\|A^T y^k + s^k\right\|_\infty \leq \varepsilon_i b^T y^k \text{ and } b^T y^k > 0$$

holds. Now in this case the problem is declared primal infeasible and (y^k, s^k) is reported as a certificate of primal infeasibility. The motivation for this stopping criterion is as follows. Let

$$\bar{y} := \frac{y^k}{b^T y^k} \text{ and } \bar{s} := \frac{s^k}{b^T y^k}$$

and it is easy to verify that

$$\left\|A^T \bar{y} + \bar{s}\right\|_\infty \leq \varepsilon_i \text{ and } b^T \bar{y} = 1$$

which shows (y^k, s^k) is an approximate certificate of dual infeasibility, where ε_i controls the quality of the approximation.

Adjusting optimality criteria and near optimality

It is possible to adjust the tolerances ε_p, ε_d, ε_g and ε_i using parameters; see table for details.

Table 8.2: Parameters employed in termination criterion

ToleranceParameter	name
ε_p	*MSK_DPAR_INTPNT_TOL_PFEAS*
ε_d	*MSK_DPAR_INTPNT_TOL_DFEAS*
ε_g	*MSK_DPAR_INTPNT_TOL_REL_GAP*
ε_i	*MSK_DPAR_INTPNT_TOL_INFEAS*

The default values of the termination tolerances are chosen such that for a majority of problems appearing in practice it is not possible to achieve much better accuracy. Therefore, tightening the tolerances usually is not worthwhile. However, an inspection of (8.11) reveals that the quality of the solution depends on $\|b\|_\infty$ and $\|c\|_\infty$; the smaller the norms are, the better the solution accuracy.

The interior-point method as implemented by **MOSEK** will converge toward optimality and primal and dual feasibility at the same rate *[And09]*. This means that if the optimizer is stopped prematurely then it is very unlikely that either the primal or dual solution is feasible. Another consequence is that in most cases all the tolerances, ε_p, ε_d, ε_g and ε_i, have to be relaxed together to achieve an effect.

In some cases the interior-point method terminates having found a solution not too far from meeting the optimality condition (8.11). A solution is defined as *near optimal* if scaling the termination tolerances ε_p, ε_d, ε_g and ε_g by the same factor $\varepsilon_n \in [1.0, +\infty]$ makes the condition (8.11) satisfied. A near optimal solution is therefore of lower quality but still potentially valuable. If for instance the solver stalls, i.e. it can make no more significant progress towards the optimal solution, a near optimal solution could be available and be good enough for the user. Near infeasibility certificates are defined similarly. The value of ε_n can be adjusted with the parameter *MSK_DPAR_INTPNT_CO_TOL_NEAR_REL*.

To conclude the discussion in this section, relaxing the termination criterion is usually not worthwhile.

The Interior-point Log

Below is a typical log output from the interior-point optimizer:

```
Optimizer  - threads                : 20
Optimizer  - solved problem         : the primal
Optimizer  - Constraints            : 1
Optimizer  - Cones                  : 2
```

```
Optimizer  - Scalar variables       : 6                 conic                  : 6
Optimizer  - Semi-definite variables: 0                 scalarized             : 0
Factor     - setup time             : 0.00              dense det. time        : 0.00
Factor     - ML order time          : 0.00              GP order time          : 0.00
Factor     - nonzeros before factor : 1                 after factor           : 1
Factor     - dense dim.             : 0                 flops                  : 1.70e+01
ITE PFEAS    DFEAS    GFEAS    PRSTATUS   POBJ              DOBJ              MU       TIME
0   1.0e+00  2.9e-01  3.4e+00  0.00e+00   2.414213562e+00   0.000000000e+00   1.0e+00  0.01
1   2.7e-01  7.9e-02  2.2e+00  8.83e-01   6.969257574e-01   -9.685901771e-03  2.7e-01  0.01
2   6.5e-02  1.9e-02  1.2e+00  1.16e+00   7.606090061e-01   6.046141322e-01   6.5e-02  0.01
3   1.7e-03  5.0e-04  2.2e-01  1.12e+00   7.084385672e-01   7.045122560e-01   1.7e-03  0.01
4   1.4e-08  4.2e-09  4.9e-08  1.00e+00   7.071067941e-01   7.071067599e-01   1.4e-08  0.01
```

The first line displays the number of threads used by the optimizer and the second line tells that the optimizer chose to solve the dual problem rather than the primal problem. The next line displays the problem dimensions as seen by the optimizer, and the `Factor...` lines show various statistics. This is followed by the iteration log.

Using the same notation as in Section *8.4.1* the columns of the iteration log have the following meaning:

- `ITE`: Iteration index k.
- `PFEAS`: $\left\|Ax^k - b\tau^k\right\|_\infty$. The numbers in this column should converge monotonically towards zero but may stall at low level due to rounding errors.
- `DFEAS`: $\left\|A^T y^k + s^k - c\tau^k\right\|_\infty$. The numbers in this column should converge monotonically towards zero but may stall at low level due to rounding errors.
- `GFEAS`: $|-c^T x^k + b^T y^k - \kappa^k|$. The numbers in this column should converge monotonically towards zero but may stall at low level due to rounding errors.
- `PRSTATUS`: This number converges to 1 if the problem has an optimal solution whereas it converges to -1 if that is not the case.
- `POBJ`: $c^T x^k/\tau^k$. An estimate for the primal objective value.
- `DOBJ`: $b^T y^k/\tau^k$. An estimate for the dual objective value.
- `MU`: $\frac{(x^k)^T s^k + \tau^k \kappa^k}{n+1}$. The numbers in this column should always converge to zero.
- `TIME`: Time spent since the optimization started (in seconds).

8.5 Nonlinear Convex Optimization

8.5.1 The Interior-point Optimizer

For quadratic, quadratically constrained, and general convex optimization problems an interior-point type optimizer is available. The interior-point optimizer is an implementation of the homogeneous and self-dual algorithm. For a detailed description of the algorithm, please see *[AY98]*, *[AY99]*.

The Convexity Requirement

Continuous nonlinear problems are required to be convex. For quadratic problems **MOSEK** test this requirement before optimizing. Specifying a non-convex problem results in an error message.

The following parameters are available to control the convexity check:

- *MSK_IPAR_CHECK_CONVEXITY*: Turn convexity check on/off.
- *MSK_DPAR_CHECK_CONVEXITY_REL_TOL*: Tolerance for convexity check.
- *MSK_IPAR_LOG_CHECK_CONVEXITY*: Turn on more log information for debugging.

The Differentiabilty Requirement

The nonlinear optimizer in **MOSEK** requires both first order and second order derivatives. This of course implies care should be taken when solving problems involving non-differentiable functions.

For instance, the function

$$f(x) = x^2$$

is differentiable everywhere whereas the function

$$f(x) = \sqrt{x}$$

is only differentiable for $x > 0$. In order to make sure that **MOSEK** evaluates the functions at points where they are differentiable, the function domains must be defined by setting appropriate variable bounds.

In general, if a variable is not ranged **MOSEK** will only evaluate that variable at points strictly within the bounds. Hence, imposing the bound

$$x \geq 0$$

in the case of $\sqrt{x}$ is sufficient to guarantee that the function will only be evaluated in points where it is differentiable.

However, if a function is differentiable on a closed range, specifying the variable bounds is not sufficient. Consider the function

$$f(x) = \frac{1}{x} + \frac{1}{1-x}. \tag{8.12}$$

In this case the bounds

$$0 \leq x \leq 1$$

will not guarantee that **MOSEK** only evaluates the function for x between 0 and 1 . To force **MOSEK** to strictly satisfy both bounds on ranged variables set the parameter *MSK_IPAR_INTPNT_STARTING_POINT* to *MSK_STARTING_POINT_SATISFY_BOUNDS* .

For efficiency reasons it may be better to reformulate the problem than to force **MOSEK** to observe ranged bounds strictly. For instance, (8.12) can be reformulated as follows

$$\begin{array}{rcl} f(x) & = & \frac{1}{x} + \frac{1}{y} \\ 0 & = & 1 - x - y \\ 0 & \leq & x \\ 0 & \leq & y. \end{array}$$

Interior-point Termination Criteria

The parameters controlling when the general convex interior-point optimizer terminates are shown in Table 8.3.

Table 8.3: Parameters employed in termination criteria.

Parameter name	Purpose
MSK_DPAR_INTPNT_NL_TOL_PFEAS	Controls primal feasibility
MSK_DPAR_INTPNT_NL_TOL_DFEAS	Controls dual feasibility
MSK_DPAR_INTPNT_NL_TOL_REL_GAP	Controls relative gap
MSK_DPAR_INTPNT_TOL_INFEAS	Controls when the problem is declared infeasible
MSK_DPAR_INTPNT_NL_TOL_MU_RED	Controls when the complementarity is reduced enough

CHAPTER

NINE

THE OPTIMIZER FOR MIXED-INTEGER PROBLEMS

A problem is a mixed-integer optimization problem when one or more of the variables are constrained to be integer valued. Readers unfamiliar with integer optimization are recommended to consult some relevant literature, e.g. the book *[Wol98]* by Wolsey.

9.1 The Mixed-integer Optimizer Overview

MOSEK can solve mixed-integer

- linear,
- quadratic and quadratically constrained, and
- conic quadratic

problems, at least as long as they do not contain both quadratic objective or constraints and conic constraints at the same time. The mixed-integer optimizer is specialized for solving linear and conic optimization problems. Pure quadratic and quadratically constrained problems are automatically converted to conic form.

By default the mixed-integer optimizer is run-to-run deterministic. This means that if a problem is solved twice on the same computer with identical parameter settings and no time limit then the obtained solutions will be identical. If a time limit is set then this may not be case since the time taken to solve a problem is not deterministic. The mixed-integer optimizer is parallelized i.e. it can exploit multiple cores during the optimization.

The solution process can be split into these phases:

1. **Presolve:** See Section *8.1*.
2. **Cut generation:** Valid inequalities (cuts) are added to improve the lower bound.
3. **Heuristic:** Using heuristics the optimizer tries to guess a good feasible solution. Heuristics can be controlled by the parameter *MSK_IPAR_MIO_HEURISTIC_LEVEL*.
4. **Search:** The optimal solution is located by branching on integer variables.

9.2 Relaxations and bounds

It is important to understand that, in a worst-case scenario, the time required to solve integer optimization problems grows exponentially with the size of the problem (solving mixed-integer problems is NP-hard). For instance, a problem with n binary variables, may require time proportional to 2^n . The value of 2^n is huge even for moderate values of n.

In practice this implies that the focus should be on computing a near-optimal solution quickly rather than on locating an optimal solution. Even if the problem is only solved approximately, it is important to know how far the approximate solution is from an optimal one. In order to say something about the quality of an approximate solution the concept of *relaxation* is important.

Consider for example a mixed-integer optimization problem

$$\begin{array}{rcllll} z^* & = & \text{minimize} & c^T x & & \\ & & \text{subject to} & Ax & = & b, \\ & & & x \geq 0 & & \\ & & & x_j \in \mathbb{Z}, & & \forall j \in \mathcal{J}. \end{array} \tag{9.1}$$

It has the continuous relaxation

$$\begin{array}{rcllll} \underline{z} & = & \text{minimize} & c^T x & & \\ & & \text{subject to} & Ax & = & b, \\ & & & x \geq 0 & & \end{array} \tag{9.2}$$

obtained simply by ignoring the integrality restrictions. The relaxation is a continuous problem, and therefore much faster to solve to optimality with a linear (or, in the general case, conic) optimizer. We call the optimal value $\underline{z}$ the *objective bound*. The objective bound $\underline{z}$ normally increases during the solution search process when the continuous relaxation is gradually refined.

Moreover, if $\hat{x}$ is any feasible solution to (9.1) and

$$\bar{z} := c^T \hat{x}$$

then

$$\underline{z} \leq z^* \leq \bar{z}.$$

These two inequalities allow us to estimate the quality of the integer solution: it is no further away from the optimum than $\bar{z} - \underline{z}$ in terms of the objective value. Whenever a mixed-integer problem is solved **MOSEK** reports this lower bound so that the quality of the reported solution can be evaluated.

9.3 Termination Criterion

In general, it is time consuming to find an exact feasible and optimal solution to an integer optimization problem, though in many practical cases it may be possible to find a sufficiently good solution. The issue of terminating the mixed-integer optimizer is rather delicate and the user has numerous possibilities of influencing it with various parameters. The mixed-integer optimizer employs a relaxed feasibility and optimality criterion to determine when a satisfactory solution is located.

A candidate solution that is feasible for the continuous relaxation is said to be an *integer feasible solution* if the criterion

$$\min(x_j - \lfloor x_j \rfloor, \lceil x_j \rceil - x_j) \leq \delta_1 \quad \forall j \in \mathcal{J}$$

is satisfied, meaning that x_j is at most δ_1 from the nearest integer.

Whenever the integer optimizer locates an integer feasible solution it will check if the criterion

$$\bar{z} - \underline{z} \leq \max(\delta_2, \delta_3 \max(10^{-10}, |\bar{z}|))$$

is satisfied. If this is the case, the integer optimizer terminates and reports the integer feasible solution as an optimal solution. If an optimal solution cannot be located after the time specified by the parameter *MSK_DPAR_MIO_DISABLE_TERM_TIME* (in seconds), it may be advantageous to relax the termination criteria, and they become replaced with

$$\bar{z} - \underline{z} \leq \max(\delta_4, \delta_5 \max(10^{-10}, |\bar{z}|)).$$

Any solution satisfying those will now be reported as **near optimal** and the solver will be terminated (note that since this criterion depends on timing, the optimizer will not be run to run deterministic).

All the δ tolerances discussed above can be adjusted using suitable parameters — see Table 9.1.

Table 9.1: Tolerances for the mixed-integer optimizer.

Tolerance	Parameter name
δ_1	*MSK_DPAR_MIO_TOL_ABS_RELAX_INT*
δ_2	*MSK_DPAR_MIO_TOL_ABS_GAP*
δ_3	*MSK_DPAR_MIO_TOL_REL_GAP*
δ_4	*MSK_DPAR_MIO_NEAR_TOL_ABS_GAP*
δ_5	*MSK_DPAR_MIO_NEAR_TOL_REL_GAP*

In Table 9.2 some other common parameters affecting the integer optimizer termination criterion are shown. Please note that if the effect of a parameter is delayed, the associated termination criterion is applied only after some time, specified by the *MSK_DPAR_MIO_DISABLE_TERM_TIME* parameter.

Table 9.2: Other parameters affecting the integer optimizer termination criterion.

Parameter name	Delayed	Explanation
MSK_IPAR_MIO_MAX_NUM_BRANCHES	Yes	Maximum number of branches allowed.
MSK_IPAR_MIO_MAX_NUM_RELAXS	Yes	Maximum number of relaxations allowed.
MSK_IPAR_MIO_MAX_NUM_SOLUTIONS	Yes	Maximum number of feasible integer solutions allowed.

9.4 Speeding Up the Solution Process

As mentioned previously, in many cases it is not possible to find an optimal solution to an integer optimization problem in a reasonable amount of time. Some suggestions to reduce the solution time are:

- Relax the termination criterion: In case the run time is not acceptable, the first thing to do is to relax the termination criterion — see Section *9.3* for details.
- Specify a good initial solution: In many cases a good feasible solution is either known or easily computed using problem-specific knowledge. If a good feasible solution is known, it is usually worthwhile to use this as a starting point for the integer optimizer.
- Improve the formulation: A mixed-integer optimization problem may be impossible to solve in one form and quite easy in another form. However, it is beyond the scope of this manual to discuss good formulations for mixed-integer problems. For discussions on this topic see for example *[Wol98]*.

9.5 Understanding Solution Quality

To determine the quality of the solution one should check the following:

- The problem status and solution status returned by **MOSEK**, as well as constraint violations in case of suboptimal solutions.
- The *optimality gap* defined as

$$\epsilon = |(\text{objective value of feasible solution}) - (\text{objective bound})| = |\bar{z} - \underline{z}|.$$

  which measures how much the located solution can deviate from the optimal solution to the problem. The optimality gap can be retrieved through the information item *MSK_DINF_MIO_OBJ_ABS_GAP*. Often it is more meaningful to look at the relative optimality gap normalized against the magnitude of the solution.

$$\epsilon_{\text{rel}} = \frac{|\bar{z} - \underline{z}|}{\max(10^{-10}, |\bar{z}|)}.$$

  The relative optimality gap is available in *MSK_DINF_MIO_OBJ_REL_GAP*.

9.6 The Optimizer Log

Below is a typical log output from the mixed-integer optimizer:

```
Presolved problem: 6573 variables, 35728 constraints, 101258 non-zeros
Presolved problem: 0 general integer, 4294 binary, 2279 continuous
Clique table size: 1636
BRANCHES RELAXS   ACT_NDS  DEPTH    BEST_INT_OBJ         BEST_RELAX_OBJ       REL_GAP(%)  TIME
0        1        0        0        NA                   1.8218819866e+07     NA          1.6
0        1        0        0        1.8331557950e+07     1.8218819866e+07     0.61        3.5
0        1        0        0        1.8300507546e+07     1.8218819866e+07     0.45        4.3
Cut generation started.
0        2        0        0        1.8300507546e+07     1.8218819866e+07     0.45        5.3
Cut generation terminated. Time = 1.43
0        3        0        0        1.8286893047e+07     1.8231580587e+07     0.30        7.5
15       18       1        0        1.8286893047e+07     1.8231580587e+07     0.30        10.5
31       34       1        0        1.8286893047e+07     1.8231580587e+07     0.30        11.1
51       54       1        0        1.8286893047e+07     1.8231580587e+07     0.30        11.6
91       94       1        0        1.8286893047e+07     1.8231580587e+07     0.30        12.4
171      174      1        0        1.8286893047e+07     1.8231580587e+07     0.30        14.3
331      334      1        0        1.8286893047e+07     1.8231580587e+07     0.30        17.9

[ ... ]

Objective of best integer solution : 1.825846762609e+07
Best objective bound               : 1.823311032986e+07
Construct solution objective       : Not employed
Construct solution # roundings     : 0
User objective cut value           : 0
Number of cuts generated           : 117
  Number of Gomory cuts            : 108
  Number of CMIR cuts              : 9
Number of branches                 : 4425
Number of relaxations solved       : 4410
Number of interior point iterations: 25
Number of simplex iterations       : 221131
```

The first lines contain a summary of the problem as seen by the optimizer. This is followed by the iteration log. The columns have the following meaning:

- `BRANCHES`: Number of branches generated.
- `RELAXS`: Number of relaxations solved.
- `ACT_NDS`: Number of active branch bound nodes.
- `DEPTH`: Depth of the recently solved node.
- `BEST_INT_OBJ`: The best integer objective value, $\bar{z}$.
- `BEST_RELAX_OBJ`: The best objective bound, $\underline{z}$.
- `REL_GAP(%)`: Relative optimality gap, $100\% \cdot \epsilon_{\text{rel}}$
- `TIME`: Time (in seconds) from the start of optimization.

Following that a summary of the optimization process is printed.

CHAPTER

TEN

PROBLEM ANALYZER

The problem analyzer prints a detailed survey of the

- linear constraints and objective
- quadratic constraints
- conic constraints
- variables

of the model.

In the initial stages of model formulation the problem analyzer may be used as a quick way of verifying that the model has been built or imported correctly. In later stages it can help revealing special structures within the model that may be used to tune the optimizer's performance or to identify the causes of numerical difficulties.

The problem analyzer is run from the command line using the *-anapro* argument and produces something similar to the following (this is the problem analyzer's survey of the `aflow30a` problem from the MIPLIB 2003 collection.)

```
Analyzing the problem

Constraints               Bounds                    Variables
 upper bd:       421       ranged  : all             cont:       421
 fixed   :        58                                 bin :       421

--------------------------------------------------------------------------------

Objective, min cx
   range: min |c|: 0.00000   min |c|>0: 11.0000     max |c|: 500.000
 distrib:        |c|        vars
                   0         421
           [11, 100)         150
          [100, 500]         271

--------------------------------------------------------------------------------

Constraint matrix A has
       479 rows (constraints)
       842 columns (variables)
      2091 (0.518449%) nonzero entries (coefficients)

Row nonzeros, A_i
   range: min A_i: 2 (0.23753%)    max A_i: 34 (4.038%)
 distrib:        A_i        rows       rows%        acc%
                   2         421       87.89       87.89
             [8, 15]          20        4.18       92.07
            [16, 31]          30        6.26       98.33
            [32, 34]           8        1.67      100.00
```

```
Column nonzeros, A|j
   range: min A|j: 2 (0.417537%)    max A|j: 3 (0.626305%)
 distrib:        A|j        cols        cols%        acc%
                   2         435        51.66       51.66
                   3         407        48.34      100.00

A nonzeros, A(ij)
   range: min |A(ij)|: 1.00000     max |A(ij)|: 100.000
 distrib:      A(ij)      coeffs
             [1, 10)        1670
           [10, 100]         421

--------------------------------------------------------------------------------

Constraint bounds, lb <= Ax <= ub
 distrib:        |b|             lbs             ubs
                   0                             421
             [1, 10]              58              58

Variable bounds, lb <= x <= ub
 distrib:        |b|             lbs             ubs
                   0             842
             [1, 10)                             421
           [10, 100]                             421

--------------------------------------------------------------------------------
```

The survey is divided into six different sections, each described below. To keep the presentation short with focus on key elements the analyzer generally attempts to display information on issues relevant for the current model only: E.g., if the model does not have any conic constraints (this is the case in the example above) or any integer variables, those parts of the analysis will not appear.

10.1 General Characteristics

The first part of the survey consists of a brief summary of the model's linear and quadratic constraints (indexed by i) and variables (indexed by j). The summary is divided into three subsections:

Constraints

- `upper bd` The number of upper bounded constraints, $\sum_{j=0}^{n-1} a_{ij}x_j \leq u_i^c$
- `lower bd` The number of lower bounded constraints, $l_i^c \leq \sum_{j=0}^{n-1} a_{ij}x_j$
- `ranged` The number of ranged constraints, $l_i^c \leq \sum_{j=0}^{n-1} a_{ij}x_j \leq u_i^c$
- `fixed` The number of fixed constraints, $l_i^c = \sum_{j=0}^{n-1} a_{ij}x_j = u_i^c$
- `free` The number of free constraints

Bounds

- `upper bd` The number of upper bounded variables, $x_j \leq u_j^x$
- `lower bd` The number of lower bounded variables, $l_k^x \leq x_j$
- `ranged` The number of ranged variables, $l_k^x \leq x_j \leq u_j^x$
- `fixed` The number of fixed variables, $l_k^x = x_j = u_j^x$

- `free` The number of free variables

`Variables`

- `cont` The number of continuous variables, $x_j \in \mathbb{R}$
- `bin` The number of binary variables, $x_j \in \{0, 1\}$
- `int` The number of general integer variables, $x_j \in \mathbb{Z}$

Only constraints, bounds and domains actually in the model will be reported on; if all entities in a section turn out to be of the same kind, the number will be replaced by `all` for brevity.

10.2 Objective

The second part of the survey focuses on (the linear part of) the objective, summarizing the optimization sense and the coefficients' absolute value range and distribution. The number of 0 (zero) coefficients is singled out (if any such variables are in the problem).

The range is displayed using three terms:

- `min |c|` The minimum absolute value among all coeffecients
- `min |c|>0` The minimum absolute value among the nonzero coefficients
- `max |c|` The maximum absolute value among the coefficients

If some of these extrema turn out to be equal, the display is shortened accordingly:

- If `min |c|` is greater than zero, the `min |c|>0` term is obsolete and will not be displayed
- If only one or two different coefficients occur this will be displayed using `all` and an explicit listing of the coefficients

The absolute value distribution is displayed as a table summarizing the numbers by orders of magnitude (with a ratio of 10). Again, the number of variables with a coefficient of 0 (if any) is singled out. Each line of the table is headed by an interval (half-open intervals including their lower bounds), and is followed by the number of variables with their objective coefficient in this interval. Intervals with no elements are skipped.

10.3 Linear Constraints

The third part of the survey displays information on the nonzero coefficients of the linear constraint matrix.

Following a brief summary of the matrix dimensions and the number of nonzero coefficients in total, three sections provide further details on how the nonzero coefficients are distributed by row-wise count (`A_i`), by column-wise count (`A|j`), and by absolute value (`|A(ij)|`). Each section is headed by a brief display of the distribution's range (`min` and `max`), and for the row/column-wise counts the corresponding densities are displayed too (in parentheses).

The distribution tables single out three particularly interesting counts: zero, one, and two nonzeros per row/column; the remaining row/column nonzeros are displayed by orders of magnitude (ratio 2). For each interval the relative and accumulated relative counts are also displayed.

Note that constraints may have both linear and quadratic terms, but the empty rows and columns reported in this part of the survey relate to the linear terms only. If empty rows and/or columns are found in the linear constraint matrix, the problem is analyzed further in order to determine if the corresponding constraints have any quadratic terms or the corresponding variables are used in conic or quadratic constraints.

The distribution of the absolute values, `|A(ij)|`, is displayed just as for the objective coefficients described above.

10.4 Constraint and Variable Bounds

The fourth part of the survey displays distributions for the absolute values of the finite lower and upper bounds for both constraints and variables. The number of bounds at 0 is singled out and, otherwise, displayed by orders of magnitude (with a ratio of 10).

10.5 Quadratic Constraints

The fifth part of the survey displays distributions for the nonzero elements in the gradient of the quadratic constraints, i.e. the nonzero row counts for the column vectors Qx . The table is similar to the tables for the linear constraints' nonzero row and column counts described in the survey's third part.

Note: Quadratic constraints may also have a linear part, but that will be included in the linear constraints survey; this means that if a problem has one or more pure quadratic constraints, part three of the survey will report anleq al number of linear constraint rows with 0 (zero) nonzeros. Likewise, variables that appear in quadratic terms only will be reported as empty columns (0 nonzeros) in the linear constraint report.

10.6 Conic Constraints

The last part of the survey summarizes the model's conic constraints. For each of the two types of cones, quadratic and rotated quadratic, the total number of cones are reported, and the distribution of the cones' dimensions are displayed using intervals. Cone dimensions of 2, 3, and 4 are singled out.

CHAPTER

ELEVEN

ANALYZING INFEASIBLE PROBLEMS

When developing and implementing a new optimization model, the first attempts will often be either infeasible, due to specification of inconsistent constraints, or unbounded, if important constraints have been left out.

In this section we will

- go over an example demonstrating how to locate infeasible constraints using the **MOSEK** infeasibility report tool,
- discuss in more general terms which properties may cause infeasibilities, and
- present the more formal theory of infeasible and unbounded problems.

11.1 Example: Primal Infeasibility

A problem is said to be *primal infeasible* if no solution exists that satisfies all the constraints of the problem.

As an example of a primal infeasible problem consider the problem of minimizing the cost of transportation between a number of production plants and stores: Each plant produces a fixed number of goods, and each store has a fixed demand that must be met. Supply, demand and cost of transportation per unit are given in Fig. 11.1.

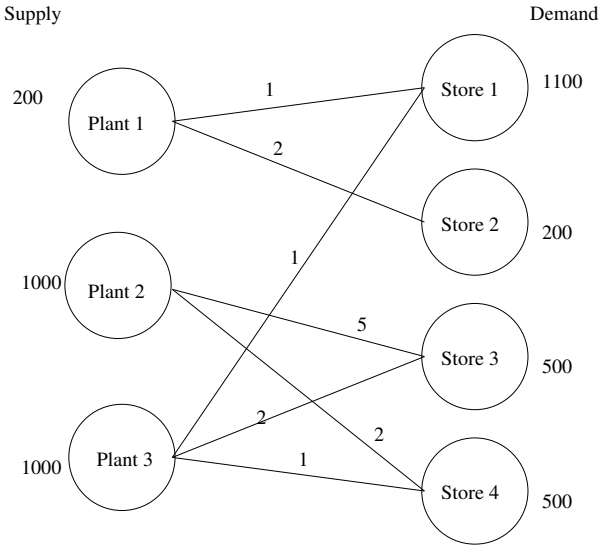

Fig. 11.1: Supply, demand and cost of transportation.

The problem represented in Fig. 11.1 is infeasible, since the total demand

$$2300 = 1100 + 200 + 500 + 500$$

exceeds the total supply

$$2200 = 200 + 1000 + 1000$$

If we denote the number of transported goods from plant i to store j by x_{ij} , the problem can be formulated as the LP:

$$\begin{array}{lrcrcrcrcrcrcrcl}
\text{minimize} & x_{11} & + & 2x_{12} & + & 5x_{23} & + & 2x_{24} & + & x_{31} & + & 2x_{33} & + & x_{34} & & \\
\text{subject to} & x_{11} & + & x_{12} & & & & & & & & & & & \leq & 200, \\
 & & & & & x_{23} & + & x_{24} & & & & & & & \leq & 1000, \\
 & & & & & & & & & x_{31} & + & x_{33} & + & x_{34} & \leq & 1000, \\
 & x_{11} & & & & & & & + & x_{31} & & & & & = & 1100, \\
 & & & x_{12} & & & & & & & & & & & = & 200, \\
 & & & & & x_{23} & + & & & & & x_{33} & & & = & 500, \\
 & & & & & & & x_{24} & + & & & & & x_{34} & = & 500, \\
x_{ij} \geq 0. & & & & & & & & & & & & & & &
\end{array} \tag{11.1}$$

Solving problem (11.1) using **MOSEK** will result in a solution, a solution status and a problem status. Among the log output from the execution of **MOSEK** on the above problem are the lines:

```
Basic solution
Problem status  : PRIMAL_INFEASIBLE
Solution status : PRIMAL_INFEASIBLE_CER
```

The first line indicates that the problem status is primal infeasible. The second line says that a *certificate of the infeasibility* was found. The certificate is returned in place of the solution to the problem.

11.2 Locating the cause of Primal Infeasibility

Usually a primal infeasible problem status is caused by a mistake in formulating the problem and therefore the question arises: *What is the cause of the infeasible status?* When trying to answer this question, it is often advantageous to follow these steps:

- Remove the objective function. This does not change the infeasibility status but simplifies the problem, eliminating any possibility of issues related to the objective function.
- Consider whether your problem has some necessary conditions for feasibility and examine if these are satisfied, e.g. total supply should be greater than or equal to total demand.
- Verify that coefficients and bounds are reasonably sized in your problem.

If the problem is still primal infeasible, some of the constraints must be relaxed or removed completely. The **MOSEK** infeasibility report (Section *11.4*) may assist you in finding the constraints causing the infeasibility.

Possible ways of relaxing your problem nclude:

- Increasing (decreasing) upper (lower) bounds on variables and constraints.
- Removing suspected constraints from the problem.

Returning to the transportation example, we discover that removing the fifth constraint

$$x_{12} = 200$$

makes the problem feasible.

11.3 Locating the Cause of Dual Infeasibility

A problem may also be *dual infeasible*. In this case the primal problem is often unbounded, meaning that feasbile solutions exists such that the objective tends towards infinity. An example of a dual infeasible and primal unbounded problem is:

$$\begin{array}{ll} \text{minimize} & x_1 \\ \text{subject to} & x_1 \leq 5. \end{array}$$

To resolve a dual infeasibility the primal problem must be made more restricted by

- Adding upper or lower bounds on variables or constraints.
- Removing variables.
- Changing the objective.

11.3.1 A cautionary note

The problem

$$\begin{array}{ll} \text{minimize} & 0 \\ \text{subject to} & 0 \leq x_1, \\ & x_j \leq x_{j+1}, \quad j = 1, \ldots, n-1, \\ & x_n \leq -1 \end{array}$$

is clearly infeasible. Moreover, if any one of the constraints is dropped, then the problem becomes feasible.

This illustrates the worst case scenario where all, or at least a significant portion of the constraints are involved in causing infeasibility. Hence, it may not always be easy or possible to pinpoint a few constraints responsible for infeasibility.

11.4 The Infeasibility Report

MOSEK includes functionality for diagnosing the cause of a primal or a dual infeasibility. It can be turned on by setting the *MSK_IPAR_INFEAS_REPORT_AUTO* to *MSK_ON*. This causes **MOSEK** to print a report on variables and constraints involved in the infeasibility.

The *MSK_IPAR_INFEAS_REPORT_LEVEL* parameter controls the amount of information presented in the infeasibility report. The default value is 1.

11.4.1 Example: Primal Infeasibility

We will keep working with the problem (11.1) written in LP format:

Listing 11.1: The code for problem (11.1).

```
\
\ An example of an infeasible linear problem.
\
minimize
 obj: + 1 x11 + 2 x12
      + 5 x23 + 2 x24
      + 1 x31 + 2 x33 + 1 x34
st
  s0: + x11 + x12       <= 200
  s1: + x23 + x24       <= 1000
  s2: + x31 + x33 + x34 <= 1000
```

```
  d1: + x11 + x31        = 1100
  d2: + x12              = 200
  d3: + x23 + x33        = 500
  d4: + x24 + x34        = 500
bounds
end
```

Using the command line (please remeber it accepts options following the C API format)

```
mosek -d MSK_IPAR_INFEAS_REPORT_AUTO MSK_ON infeas.lp
```

MOSEK produces the following infeasibility report:

```
MOSEK PRIMAL INFEASIBILITY REPORT.

Problem status: The problem is primal infeasible

The following constraints are involved in the primal infeasibility.

Index    Name      Lower bound      Upper bound      Dual lower       Dual upper
0        s0        NONE             2.000000e+002    0.000000e+000    1.000000e+000
2        s2        NONE             1.000000e+003    0.000000e+000    1.000000e+000
3        d1        1.100000e+003    1.100000e+003    1.000000e+000    0.000000e+000
4        d2        2.000000e+002    2.000000e+002    1.000000e+000    0.000000e+000

The following bound constraints are involved in the infeasibility.

Index    Name      Lower bound      Upper bound      Dual lower       Dual upper
8        x33       0.000000e+000    NONE             1.000000e+000    0.000000e+000
10       x34       0.000000e+000    NONE             1.000000e+000    0.000000e+000
```

The infeasibility report is divided into two sections corresponding to constraints and variables. It is a selection of those lines from the problem solution (in this case the file `infeas.sol`), which are important in understanding primal infeasibility. In this case the constraints `s0`, `s2`, `d1`, `d2` and variables `x33`, `x34` are of importance.

The columns `Dual lower` and `Dual upper` contain the values of dual variables s_l^c, s_u^c, s_l^x and s_u^x in the primal infeasibility certificate (see Section *7.1.2.1*). Only the non-zero ones, which contribute to the optimization objective and thus are important for infeasibility, are shown.

It is also possible to obtain the infeasible subproblem. The command line

```
mosek -d MSK_IPAR_INFEAS_REPORT_AUTO MSK_ON infeas.lp -info rinfeas.lp
```

produces the files `rinfeas.bas.inf.lp`. In this case the content of the file `rinfeas.bas.inf.lp` is

```
minimize
obj:  + 0 x11 + 0 x12 + 0 x13 + 0 x21 + 0 x22 + 0 x23
      + 0 x31 + 0 x32 + 0 x33 + 0 x24 + 0 x34
subject to
s0:  + x11 + x12 <= 2e+02
s2:  + x31 + x33 + x34 <= 1e+03
d1:  + x11 + x31 = 1.1e+03
d2:  + x12 = 2e+02
bounds
x11 free
x12 free
x13 free
x21 free
x22 free
x23 free
x31 free
```

```
x32 free
0 <= x33 <= +infinity
x24 free
0 <= x34 <= +infinity
end
```

which is an optimization problem. This problem is identical to (11.1), except that the objective and some of the constraints and bounds have been removed. Executing the command

```
mosek -d MSK_IPAR_INFEAS_REPORT_AUTO MSK_ON rinfeas.bas.inf.lp
```

demonstrates that the reduced problem is **primal infeasible**. Since the reduced problem is usually smaller than original problem, it should be easier to locate the cause of infeasibility in this rather than in the original (11.1).

11.4.2 Example: Dual Infeasibility

The following problem is dual to (11.1) and therefore it is dual infeasible.

Listing 11.2: The dual of problem (11.1).

```
maximize + 200 y1 + 1000 y2 + 1000 y3 + 1100 y4 + 200 y5 + 500 y6 + 500 y7
subject to
   x11: y1+y4 < 1
   x12: y1+y5 < 2
   x23: y2+y6 < 5
   x24: y2+y7 < 2
   x31: y3+y4 < 1
   x33: y3+y6 < 2
   x34: y3+y7 < 1
bounds
   -inf <= y1 < 0
   -inf <= y2 < 0
   -inf <= y3 < 0
   y4 free
   y5 free
   y6 free
   y7 free
end
```

This can be verified by proving that

$$(y_1, \ldots, y_7) = (-1, 0, -1, 1, 1, 0, 0)$$

is a certificate of dual infeasibility (see Section *7.1.2.2*) as we can see from this report:

```
MOSEK DUAL INFEASIBILITY REPORT.

Problem status: The problem is dual infeasible

The following constraints are involved in the infeasibility.

Index    Name             Activity         Objective        Lower bound      Upper bound
5        x33              -1.000000e+00                     NONE             2.000000e+00
6        x34              -1.000000e+00                     NONE             1.000000e+00

The following variables are involved in the infeasibility.

Index    Name             Activity         Objective        Lower bound      Upper bound
0        y1               -1.000000e+00    2.000000e+02     NONE             0.000000e+00
2        y3               -1.000000e+00    1.000000e+03     NONE             0.000000e+00
```

```
3        y4                1.000000e+00      1.100000e+03      NONE              NONE
4        y5                1.000000e+00      2.000000e+02      NONE              NONE

Interior-point solution summary
  Problem status  : DUAL_INFEASIBLE
  Solution status : DUAL_INFEASIBLE_CER
  Primal.  obj: 1.0000000000e+02    nrm: 1e+00    Viol.  con: 0e+00    var: 0e+00
```

Let y^* denote the reported primal solution. **MOSEK** states

- that the problem is *dual infeasible*,
- that the reported solution is a certificate of dual infeasibility, and
- that the infeasibility measure for y^* is approximately zero.

Since the original objective was maximization, we have that $c^T y^* > 0$. See Section *7.1.2* for how to interpret the parameter values in the infeasibility report for a linear program. We see that the variables `y1`, `y3`, `y4`, `y5` and the constraints `x33` and `x34` contribute to infeasibility with non-zero values in the `Activity` column.

One possible strategy to *fix* the infeasibility is to modify the problem so that the certificate of infeasibility becomes invalid. In this case we could do one the following things:

- Add a lower bound on `y3`. This will directly invalidate the certificate of dual infeasibility.
- Increase the object coefficient of `y3`. Changing the coefficients sufficiently will invalidate the inequality $c^T y^* > 0$ and thus the certificate.
- Add lower bounds on `x11` or `x31`. This will directly invalidate the certificate of infeasibility.

Please note that modifying the problem to invalidate the reported certificate does *not* imply that the problem becomes dual feasible — the reason for infeasibility may simply *move*, resulting a problem that is still infeasible, but for a different reason.

More often, the reported certificate can be used to give a hint about errors or inconsistencies in the model that produced the problem.

11.5 Theory Concerning Infeasible Problems

This section discusses the theory of infeasibility certificates and how **MOSEK** uses a certificate to produce an infeasibility report. In general, **MOSEK** solves the problem

$$\begin{array}{lccccc} \text{minimize} & & & c^T x + c^f & & \\ \text{subject to} & l^c & \leq & Ax & \leq & u^c, \\ & l^x & \leq & x & \leq & u^x \end{array} \tag{11.2}$$

where the corresponding dual problem is

$$\begin{array}{lcl} \text{maximize} & (l^c)^T s_l^c - (u^c)^T s_u^c & \\ & +(l^x)^T s_l^x - (u^x)^T s_u^x + c^f & \\ \text{subject to} & A^T y + s_l^x - s_u^x = c, & \\ & -y + s_l^c - s_u^c = 0, & \\ & s_l^c, s_u^c, s_l^x, s_u^x \leq 0. & \end{array} \tag{11.3}$$

We use the convension that for any bound that is not finite, the corresponding dual variable is fixed at zero (and thus will have no influence on the dual problem). For example

$$l_j^x = -\infty \quad \Rightarrow \quad (s_l^x)_j = 0$$

11.6 The Certificate of Primal Infeasibility

A certificate of primal infeasibility is *any* solution to the homogenized dual problem

$$\begin{array}{lll} \text{maximize} & (l^c)^T s_l^c - (u^c)^T s_u^c & \\ & +(l^x)^T s_l^x - (u^x)^T s_u^x & \\ \text{subject to} & A^T y + s_l^x - s_u^x & = 0, \\ & -y + s_l^c - s_u^c & = 0, \\ & s_l^c, s_u^c, s_l^x, s_u^x \leq 0. & \end{array}$$

with a positive objective value. That is, $(s_l^{c*}, s_u^{c*}, s_l^{x*}, s_u^{x*})$ is a certificate of primal infeasibility if

$$(l^c)^T s_l^{c*} - (u^c)^T s_u^{c*} + (l^x)^T s_l^{x*} - (u^x)^T s_u^{x*} > 0$$

and

$$\begin{array}{lll} A^T y + s_l^{x*} - s_u^{x*} & = & 0, \\ -y + s_l^{c*} - s_u^{c*} & = & 0, \\ s_l^{c*}, s_u^{c*}, s_l^{x*}, s_u^{x*} \leq 0. & & \end{array}$$

The well-known *Farkas Lemma* tells us that (11.2) is infeasible if and only if a certificate of primal infeasibility exists.

Let $(s_l^{c*}, s_u^{c*}, s_l^{x*}, s_u^{x*})$ be a certificate of primal infeasibility then

$$(s_l^{c*})_i > 0((s_u^{c*})_i > 0)$$

implies that the lower (upper) bound on the i th constraint is important for the infeasibility. Furthermore,

$$(s_l^{x*})_j > 0((s_u^{x*})_i > 0)$$

implies that the lower (upper) bound on the j th variable is important for the infeasibility.

11.7 The certificate of dual infeasibility

A certificate of dual infeasibility is *any* solution to the problem

$$\begin{array}{lllll} \text{minimize} & & c^T x & & \\ \text{subject to} & \bar{l}^c & \leq Ax & \leq & \bar{u}^c, \\ & \bar{l}^x & \leq x & \leq & \bar{u}^x \end{array}$$

with negative objective value, where we use the definitions

$$\bar{l}_i^c := \left\{ \begin{array}{ll} 0, & l_i^c > -\infty, \\ -\infty, & \text{otherwise}, \end{array} \right\}, \; \bar{u}_i^c := \left\{ \begin{array}{ll} 0, & u_i^c < \infty, \\ \infty, & \text{otherwise}, \end{array} \right\}$$

and

$$\bar{l}_i^x := \left\{ \begin{array}{ll} 0, & l_i^x > -\infty, \\ -\infty, & \text{otherwise}, \end{array} \right\} \quad \text{and} \quad \bar{u}_i^x := \left\{ \begin{array}{ll} 0, & u_i^x < \infty, \\ \infty, & \text{otherwise}. \end{array} \right\}$$

Stated differently, a certificate of dual infeasibility is any x^* such that

$$\begin{array}{lllll} & & c^T x^* & < & 0, \\ \bar{l}^c & \leq & Ax^* & \leq & \bar{u}^c, \\ \bar{l}^x & \leq & x^* & \leq & \bar{u}^x \end{array} \tag{11.4}$$

The well-known Farkas Lemma tells us that (11.3) is infeasible if and only if a certificate of dual infeasibility exists.

Note that if x^* is a certificate of dual infeasibility then for any j such that

$$x_j^* \leq 0,$$

variable j is involved in the dual infeasibility.

Given the assumption that all weights are 1 then the command

```
mosek -primalrepair -d MSK_IPAR_LOG_FEAS_REPAIR 3 feasrepair.lp
```

will form the repaired problem and solve it. The parameter *MSK_IPAR_LOG_FEAS_REPAIR* controls the amount of log output from the repair. A value of 2 causes the optimal repair to printed out.

The output from running the above command is:

```
Copyright (c) MOSEK ApS, Denmark. WWW: mosek.com

Open file 'feasrepair.lp'

Read summary
Type             : LO (linear optimization problem)
Objective sense  : min
Constraints      : 4
Scalar variables : 2
Matrix variables : 0
Time             : 0.0

Computer
Platform               : Windows/64-X86
Cores                  : 4

Problem
Name                   :
Objective sense        : min
Type                   : LO (linear optimization problem)
Constraints            : 4
Cones                  : 0
Scalar variables       : 2
Matrix variables       : 0
Integer variables      : 0

Primal feasibility repair started.
Optimizer started.
Interior-point optimizer started.
Presolve started.
Linear dependency checker started.
Linear dependency checker terminated.
Eliminator started.
Total number of eliminations : 2
Eliminator terminated.
Eliminator - tries                  : 1                 time                   : 0.00
Eliminator - elim's                 : 2
Lin. dep.  - tries                  : 1                 time                   : 0.00
Lin. dep.  - number                 : 0
Presolve terminated. Time: 0.00
Optimizer  - threads                : 1
Optimizer  - solved problem         : the primal
Optimizer  - Constraints            : 2
Optimizer  - Cones                  : 0
Optimizer  - Scalar variables       : 6                 conic                  : 0
Optimizer  - Semi-definite variables: 0                 scalarized             : 0
Factor     - setup time             : 0.00              dense det. time        : 0.00
Factor     - ML order time          : 0.00              GP order time          : 0.00
Factor     - nonzeros before factor : 3                 after factor           : 3
Factor     - dense dim.             : 0                 flops                  : 5.40e+001
ITE PFEAS    DFEAS    GFEAS    PRSTATUS   POBJ              DOBJ              MU       TIME
0   2.7e+001 1.0e+000 4.8e+000 1.00e+000  4.195228609e+000  0.000000000e+000  1.0e+000 0.00
1   2.4e+001 8.6e-001 1.5e+000 0.00e+000  1.227497414e+001  1.504971820e+001  2.6e+000 0.00
2   2.6e+000 9.7e-002 1.7e-001 -6.19e-001 4.363064729e+001  4.648523094e+001  3.0e-001 0.00
3   4.7e-001 1.7e-002 3.1e-002 1.24e+000  4.256803136e+001  4.298540657e+001  5.2e-002 0.00
4   8.7e-004 3.2e-005 5.7e-005 1.08e+000  4.249989892e+001  4.250078747e+001  9.7e-005 0.00
```

```
5   8.7e-008 3.2e-009 5.7e-009 1.00e+000  4.249999999e+001  4.250000008e+001  9.7e-009 0.00
6   8.7e-012 3.2e-013 5.7e-013 1.00e+000  4.250000000e+001  4.250000000e+001  9.7e-013 0.00
Basis identification started.
Primal basis identification phase started.
ITER      TIME
0         0.00
Primal basis identification phase terminated. Time: 0.00
Dual basis identification phase started.
ITER      TIME
0         0.00
Dual basis identification phase terminated. Time: 0.00
Basis identification terminated. Time: 0.00
Interior-point optimizer terminated. Time: 0.00.

Optimizer terminated. Time: 0.03
Basic solution summary
Problem status  : PRIMAL_AND_DUAL_FEASIBLE
Solution status : OPTIMAL
Primal.  obj: 4.2500000000e+001   Viol.  con: 1e-013   var: 0e+000
Dual.    obj: 4.2500000000e+001   Viol.  con: 0e+000   var: 5e-013
Optimal objective value of the penalty problem: 4.250000000000e+001

Repairing bounds.
Increasing the upper bound -2.25e+001 on constraint 'c4' (3) with 1.35e+002.
Decreasing the lower bound 6.50e+002 on variable 'x2' (4) with 2.00e+001.
Primal feasibility repair terminated.
Optimizer started.
Interior-point optimizer started.
Presolve started.
Presolve terminated. Time: 0.00
Interior-point optimizer terminated. Time: 0.00.

Optimizer terminated. Time: 0.00

Interior-point solution summary
Problem status  : PRIMAL_AND_DUAL_FEASIBLE
Solution status : OPTIMAL
Primal.  obj: -5.6700000000e+003  Viol.  con: 0e+000   var: 0e+000
Dual.    obj: -5.6700000000e+003  Viol.  con: 0e+000   var: 0e+000

Basic solution summary
Problem status  : PRIMAL_AND_DUAL_FEASIBLE
Solution status : OPTIMAL
Primal.  obj: -5.6700000000e+003  Viol.  con: 0e+000   var: 0e+000
Dual.    obj: -5.6700000000e+003  Viol.  con: 0e+000   var: 0e+000

Optimizer summary
Optimizer                 -                        time: 0.00
Interior-point          - iterations : 0         time: 0.00
Basis identification    -                        time: 0.00
Primal              - iterations : 0         time: 0.00
Dual                - iterations : 0         time: 0.00
Clean primal        - iterations : 0         time: 0.00
Clean dual          - iterations : 0         time: 0.00
Clean primal-dual   - iterations : 0         time: 0.00
Simplex                 -                        time: 0.00
Primal simplex        - iterations : 0         time: 0.00
Dual simplex          - iterations : 0         time: 0.00
Primal-dual simplex   - iterations : 0         time: 0.00
Mixed integer           - relaxations: 0         time: 0.00
```

reports the optimal repair. In this case it is to increase the upper bound on constraint `c4` by 1.35e2 and

decrease the lower bound on variable `x2` by 20.

CHAPTER

TWELVE

SENSITIVITY ANALYSIS

Given an optimization problem it is often useful to obtain information about how the optimal objective value changes when the problem parameters are perturbed. E.g, assume that a bound represents the capacity of a machine. Now, it may be possible to expand the capacity for a certain cost and hence it is worthwhile knowing what the value of additional capacity is. This is precisely the type of questions the sensitivity analysis deals with.

Analyzing how the optimal objective value changes when the problem data is changed is called *sensitivity analysis*.

References

The book *[Chv83]* discusses the classical sensitivity analysis in Chapter 10 whereas the book *[RTV97]* presents a modern introduction to sensitivity analysis. Finally, it is recommended to read the short paper *[Wal00]* to avoid some of the pitfalls associated with sensitivity analysis.

Warning: Currently, sensitivity analysis is only available for continuous linear optimization problems. Moreover, **MOSEK** can only deal with perturbations of bounds and objective function coefficients.

12.1 Sensitivity Analysis for Linear Problems

12.1.1 The Optimal Objective Value Function

Assume that we are given the problem

$$\begin{array}{rcllcll} z(l^c,u^c,l^x,u^x,c) & = & \text{minimize} & & & c^Tx & & \\ & & \text{subject to} & l^c & \leq & Ax & \leq & u^c, \\ & & & l^x & \leq & x & \leq & u^x, \end{array} \tag{12.1}$$

and we want to know how the optimal objective value changes as l_i^c is perturbed. To answer this question we define the perturbed problem for l_i^c as follows

$$\begin{array}{rcllcll} f_{l_i^c}(\beta) & = & \text{minimize} & & & c^Tx & & \\ & & \text{subject to} & l^c+\beta e_i & \leq & Ax & \leq u^c, \\ & & & l^x & \leq & x \leq & u^x, \end{array}$$

where e_i is the i-th column of the identity matrix. The function

$$f_{l_i^c}(\beta) \tag{12.2}$$

shows the optimal objective value as a function of β. Please note that a change in β corresponds to a perturbation in l_i^c and hence (12.2) shows the optimal objective value as a function of varying l_i^c with the other bounds fixed.

It is possible to prove that the function (12.2) is a piecewise linear and convex function, i.e. its graph may look like in Fig. 12.1 and Fig. 12.2.

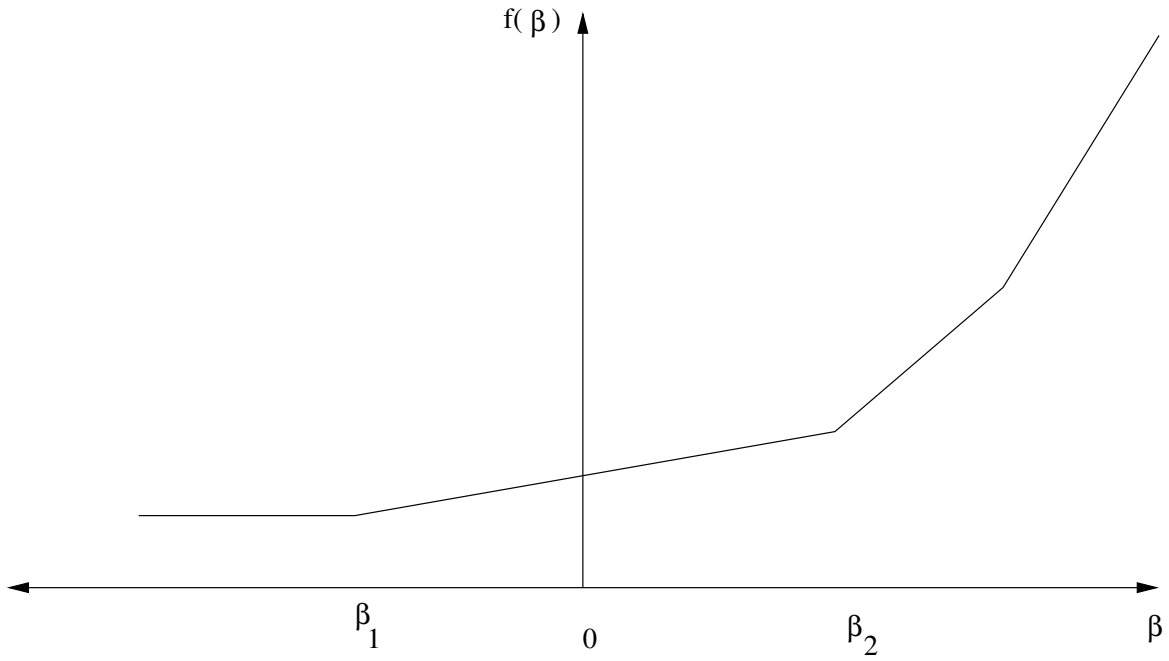

Fig. 12.1: $\beta = 0$ is in the interior of linearity interval.

Clearly, if the function $f_{l_i^c}(\beta)$ does not change much when β is changed, then we can conclude that the optimal objective value is insensitive to changes in l_i^c. Therefore, we are interested in the rate of change in $f_{l_i^c}(\beta)$ for small changes in β — specifically the gradient

$$f'_{l_i^c}(0),$$

which is called the *shadow price* related to l_i^c. The shadow price specifies how the objective value changes for small changes of β around zero. Moreover, we are interested in the *linearity interval*

$$\beta \in [\beta_1, \beta_2]$$

for which

$$f'_{l_i^c}(\beta) = f'_{l_i^c}(0).$$

Since $f_{l_i^c}$ is not a smooth function $f'_{l_i^c}$ may not be defined at 0, as illustrated in Fig. 12.2. In this case we can define a left and a right shadow price and a left and a right linearity interval.

The function $f_{l_i^c}$ considered only changes in l_i^c. We can define similar functions for the remaining parameters of the z defined in (12.1) as well:

$$\begin{array}{rcll}
f_{l_i^c}(\beta) & = & z(l^c + \beta e_i, u^c, l^x, u^x, c), & i = 1, \ldots, m, \\
f_{u_i^c}(\beta) & = & z(l^c, u^c + \beta e_i, l^x, u^x, c), & i = 1, \ldots, m, \\
f_{l_j^x}(\beta) & = & z(l^c, u^c, l^x + \beta e_j, u^x, c), & j = 1, \ldots, n, \\
f_{u_j^x}(\beta) & = & z(l^c, u^c, l^x, u^x + \beta e_j, c), & j = 1, \ldots, n, \\
f_{c_j}(\beta) & = & z(l^c, u^c, l^x, u^x, c + \beta e_j), & j = 1, \ldots, n.
\end{array}$$

Given these definitions it should be clear how linearity intervals and shadow prices are defined for the parameters u_i^c etc.

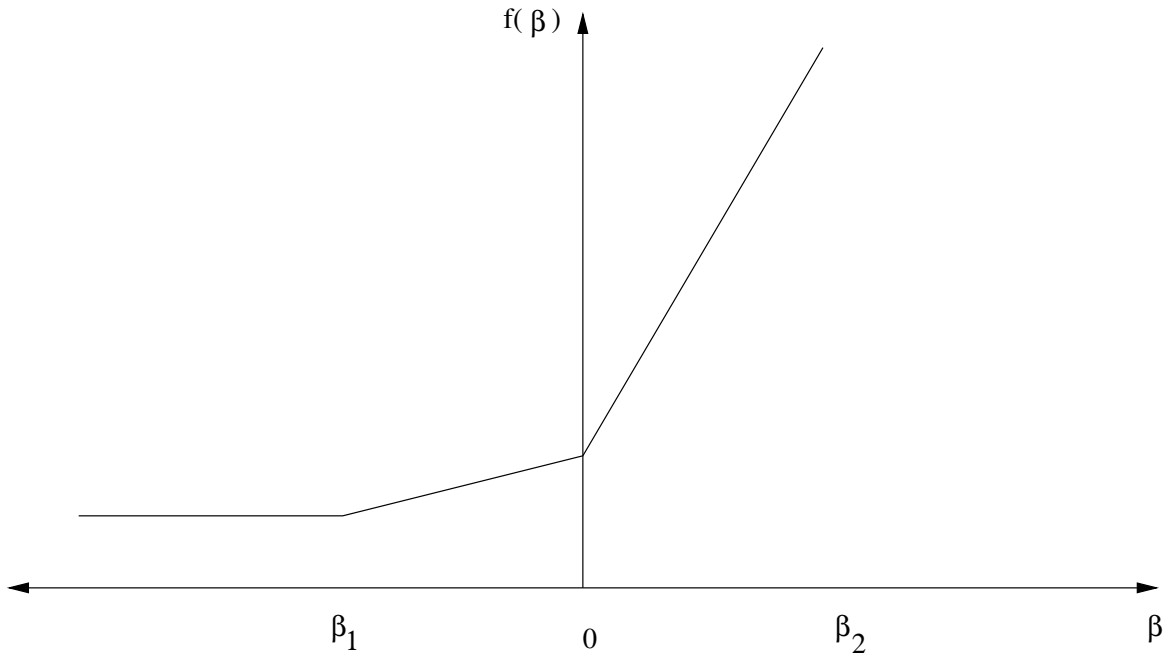

Fig. 12.2: $\beta = 0$ is a breakpoint.

Equality Constraints

In **MOSEK** a constraint can be specified as either an equality constraint or a ranged constraint. If some constraint e_i^c is an equality constraint, we define the optimal value function for this constraint as

$$f_{e_i^c}(\beta) = z(l^c + \beta e_i, u^c + \beta e_i, l^x, u^x, c)$$

Thus for an equality constraint the upper and the lower bounds (which are equal) are perturbed simultaneously. Therefore, **MOSEK** will handle sensitivity analysis differently for a ranged constraint with $l_i^c = u_i^c$ and for an equality constraint.

12.1.2 The Basis Type Sensitivity Analysis

The classical sensitivity analysis discussed in most textbooks about linear optimization, e.g. *[Chv83]*, is based on an optimal basic solution or, equivalently, on an optimal basis. This method may produce misleading results *[RTV97]* but is **computationally cheap**. Therefore, and for historical reasons, this method is available in **MOSEK**.

We will now briefly discuss the basis type sensitivity analysis. Given an optimal basic solution which provides a partition of variables into basic and non-basic variables, the basis type sensitivity analysis computes the linearity interval $[\beta_1, \beta_2]$ so that the basis remains optimal for the perturbed problem. A shadow price associated with the linearity interval is also computed. However, it is well-known that an optimal basic solution may not be unique and therefore the result depends on the optimal basic solution employed in the sensitivity analysis. This implies that the computed interval is only a subset of the largest interval for which the shadow price is constant. Furthermore, the optimal objective value function might have a breakpoint for $\beta = 0$. In this case the basis type sensitivity method will only provide a subset of either the left or the right linearity interval.

In summary, the basis type sensitivity analysis is computationally cheap but does not provide complete information. Hence, the results of the basis type sensitivity analysis should be used with care.

12.1.3 The Optimal Partition Type Sensitivity Analysis

Another method for computing the complete linearity interval is called the *optimal partition type sensitivity analysis*. The main drawback of the optimal partition type sensitivity analysis is that it is computationally expensive compared to the basis type analysis. This type of sensitivity analysis is currently provided as an experimental feature in **MOSEK**.

Given the optimal primal and dual solutions to (12.1), i.e. x^* and $((s_l^c)^*, (s_u^c)^*, (s_l^x)^*, (s_u^x)^*)$ the optimal objective value is given by

$$z^* := c^T x^*.$$

The left and right shadow prices σ_1 and σ_2 for l_i^c are given by this pair of optimization problems:

$$\begin{array}{rcll} \sigma_1 & = & \text{minimize} & e_i^T s_l^c \\ & & \text{subject to} & A^T(s_l^c - s_u^c) + s_l^x - s_u^x = c, \\ & & & (l^c)^T(s_l^c) - (u^c)^T(s_u^c) + (l^x)^T(s_l^x) - (u^x)^T(s_u^x) = z^*, \\ & & & s_l^c, s_u^c, s_l^c, s_u^x \geq 0 \end{array}$$

and

$$\begin{array}{rcll} \sigma_2 & = & \text{maximize} & e_i^T s_l^c \\ & & \text{subject to} & A^T(s_l^c - s_u^c) + s_l^x - s_u^x = c, \\ & & & (l^c)^T(s_l^c) - (u^c)^T(s_u^c) + (l^x)^T(s_l^x) - (u^x)^T(s_u^x) = z^*, \\ & & & s_l^c, s_u^c, s_l^c, s_u^x \geq 0. \end{array}$$

These two optimization problems make it easy to interpret the shadow price. Indeed, if $((s_l^c)^*, (s_u^c)^*, (s_l^x)^*, (s_u^x)^*)$ is an arbitrary optimal solution then

$$(s_l^c)_i^* \in [\sigma_1, \sigma_2].$$

Next, the linearity interval $[\beta_1, \beta_2]$ for l_i^c is computed by solving the two optimization problems

$$\begin{array}{rcllcll} \beta_1 & = & \text{minimize} & & & \beta & \\ & & \text{subject to} & l^c + \beta e_i & \leq & Ax & \leq u^c, \\ & & & & & c^T x - \sigma_1 \beta & = z^*, \\ & & & l^x & \leq & x & \leq u^x, \end{array}$$

and

$$\begin{array}{rcllcll} \beta_2 & = & \text{maximize} & & & \beta & \\ & & \text{subject to} & l^c + \beta e_i & \leq & Ax & \leq u^c, \\ & & & & & c^T x - \sigma_2 \beta & = z^*, \\ & & & l^x & \leq & x & \leq u^x. \end{array}$$

The linearity intervals and shadow prices for u_i^c, l_j^x, and u_j^x are computed similarly to l_i^c.

The left and right shadow prices for c_j denoted σ_1 and σ_2 respectively are computed as follows:

$$\begin{array}{rcllcll} \sigma_1 & = & \text{minimize} & & & e_j^T x & \\ & & \text{subject to} & l^c + \beta e_i & \leq & Ax & \leq u^c, \\ & & & & & c^T x & = z^*, \\ & & & l^x & \leq & x & \leq u^x, \end{array}$$

and

$$\begin{array}{rcllcll} \sigma_2 & = & \text{maximize} & & & e_j^T x & \\ & & \text{subject to} & l^c + \beta e_i & \leq & Ax & \leq u^c, \\ & & & & & c^T x & = z^*, \\ & & & l^x & \leq & x & \leq u^x. \end{array}$$

Once again the above two optimization problems make it easy to interpret the shadow prices. Indeed, if x^* is an arbitrary primal optimal solution, then

$$x_j^* \in [\sigma_1, \sigma_2].$$

The linearity interval $[\beta_1, \beta_2]$ for a c_j is computed as follows:

$$\begin{array}{rcll} \beta_1 & = & \text{minimize} & \beta \\ & & \text{subject to} & A^T(s_l^c - s_u^c) + s_l^x - s_u^x = c + \beta e_j, \\ & & & (l^c)^T(s_l^c) - (u^c)^T(s_u^c) + (l^x)^T(s_l^x) - (u^x)^T(s_u^x) - \sigma_1\beta \leq z^*, \\ & & & s_l^c, s_u^c, s_l^c, s_u^x \geq 0 \end{array}$$

and

$$\begin{array}{rcll} \beta_2 & = & \text{maximize} & \beta \\ & & \text{subject to} & A^T(s_l^c - s_u^c) + s_l^x - s_u^x = c + \beta e_j, \\ & & & (l^c)^T(s_l^c) - (u^c)^T(s_u^c) + (l^x)^T(s_l^x) - (u^x)^T(s_u^x) - \sigma_2\beta \leq z^*, \\ & & & s_l^c, s_u^c, s_l^c, s_u^x \geq 0. \end{array}$$

12.1.4 Example: Sensitivity Analysis

As an example we will use the following transportation problem. Consider the problem of minimizing the transportation cost between a number of production plants and stores. Each plant supplies a number of goods and each store has a given demand that must be met. Supply, demand and cost of transportation per unit are shown in Fig. 12.3.

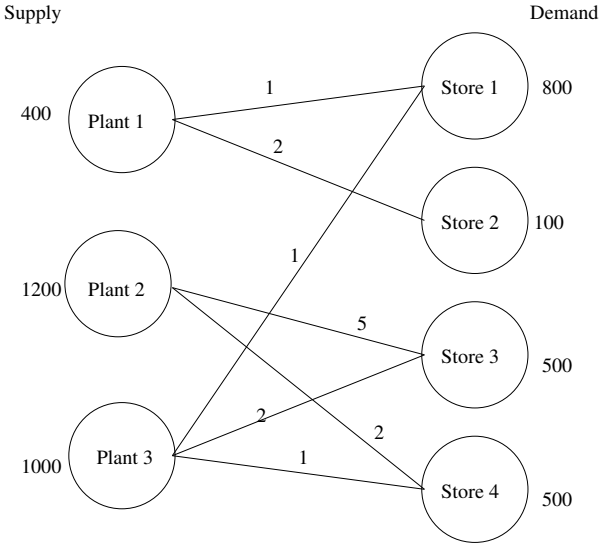

Fig. 12.3: Supply, demand and cost of transportation.

If we denote the number of transported goods from location i to location j by x_{ij}, problem can be formulated as the linear optimization problem of minimizing

$$1x_{11} + 2x_{12} + 5x_{23} + 2x_{24} + 1x_{31} + 2x_{33} + 1x_{34}$$

subject to

$$\begin{array}{rrrrrrrrrrrrr} x_{11} & + & x_{12} & & & & & & & & & \leq & 400, \\ & & & x_{23} & + & x_{24} & & & & & & \leq & 1200, \\ & & & & & & x_{31} & + & x_{33} & + & x_{34} & \leq & 1000, \\ x_{11} & & & & & & + & x_{31} & & & & = & 800, \\ & & x_{12} & & & & & & & & & = & 100, \\ & & & x_{23} & + & & & & x_{33} & & & = & 500, \\ & & & & & x_{24} & + & & & & x_{34} & = & 500, \\ x_{11}, & & x_{12}, & & x_{23}, & & x_{24}, & & x_{31}, & & x_{33}, & & x_{34} \geq 0. \end{array} \tag{12.3}$$

The sensitivity parameters are shown in Table 12.1 and Table 12.2 for the basis type analysis and in Table 12.3 and Table 12.4 for the optimal partition type analysis.

Table 12.1: Ranges and shadow prices related to bounds on constraints and variables: results for the basis type sensitivity analysis.

Con.	β_1	β_2	σ_1	σ_2
1	-300.00	0.00	3.00	3.00
2	-700.00	$+\infty$	0.00	0.00
3	-500.00	0.00	3.00	3.00
4	-0.00	500.00	4.00	4.00
5	-0.00	300.00	5.00	5.00
6	-0.00	700.00	5.00	5.00
7	-500.00	700.00	2.00	2.00
Var.	β_1	β_2	σ_1	σ_2
x_{11}	$-\infty$	300.00	0.00	0.00
x_{12}	$-\infty$	100.00	0.00	0.00
x_{23}	$-\infty$	0.00	0.00	0.00
x_{24}	$-\infty$	500.00	0.00	0.00
x_{31}	$-\infty$	500.00	0.00	0.00
x_{33}	$-\infty$	500.00	0.00	0.00
x_{34}	-0.000000	500.00	2.00	2.00

Table 12.2: Ranges and shadow prices related to bounds on constraints and variables: results for the optimal partition type sensitivity analysis.

Con.	β_1	β_2	σ_1	σ_2
1	-300.00	500.00	3.00	1.00
2	-700.00	$+\infty$	-0.00	-0.00
3	-500.00	500.00	3.00	1.00
4	-500.00	500.00	2.00	4.00
5	-100.00	300.00	3.00	5.00
6	-500.00	700.00	3.00	5.00
7	-500.00	700.00	2.00	2.00
Var.	β_1	β_2	σ_1	σ_2
x_{11}	$-\infty$	300.00	0.00	0.00
x_{12}	$-\infty$	100.00	0.00	0.00
x_{23}	$-\infty$	500.00	0.00	2.00
x_{24}	$-\infty$	500.00	0.00	0.00
x_{31}	$-\infty$	500.00	0.00	0.00
x_{33}	$-\infty$	500.00	0.00	0.00
x_{34}	$-\infty$	500.00	0.00	2.00

Table 12.3: Ranges and shadow prices related to the objective coefficients: results for the basis type sensitivity analysis.

Var.	β_1	β_2	σ_1	σ_2
c_1	$-\infty$	3.00	300.00	300.00
c_2	$-\infty$	∞	100.00	100.00
c_3	-2.00	∞	0.00	0.00
c_4	$-\infty$	2.00	500.00	500.00
c_5	-3.00	∞	500.00	500.00
c_6	$-\infty$	2.00	500.00	500.00
c_7	-2.00	∞	0.00	0.00

Table 12.4: Ranges and shadow prices related to the objective coefficients: results for the optimal partition type sensitivity analysis.

Var.	β_1	β_2	σ_1	σ_2
c_1	$-\infty$	3.00	300.00	300.00
c_2	$-\infty$	∞	100.00	100.00
c_3	-2.00	∞	0.00	0.00
c_4	$-\infty$	2.00	500.00	500.00
c_5	-3.00	∞	500.00	500.00
c_6	$-\infty$	2.00	500.00	500.00
c_7	-2.00	∞	0.00	0.00

Examining the results from the optimal partition type sensitivity analysis we see that for constraint number 1 we have $\sigma_1 = 3,\ \sigma_2 = 1$ and $\beta_1 = -300,\ \beta_2 = 500$. Therefore, we have a left linearity interval of $[-300, 0]$ and a right interval of $[0, 500]$. The corresponding left and right shadow prices are 3 and 1 respectively. This implies that if the upper bound on constraint 1 increases by

$$\beta \in [0, \beta_1] = [0, 500]$$

then the optimal objective value will decrease by the value

$$\sigma_2 \beta = 1\beta.$$

Correspondingly, if the upper bound on constraint 1 is decreased by

$$\beta \in [0, 300]$$

then the optimal objective value will increase by the value

$$\sigma_1 \beta = 3\beta.$$

12.2 Sensitivity Analysis with MOSEK

A sensitivity analysis can be performed with the **MOSEK** command line tool specifying the option `-sen`, e.g.

```
mosek myproblem.mps -sen sensitivity.ssp
```

where `sensitivity.ssp` is a file in the format described in the next section. The `ssp` file describes which parts of the problem the sensitivity analysis should be performed on, see Section *12.2.1*.

By default results are written to a file named `myproblem.sen`. If necessary, this filename can be changed by setting the *MSK_SPAR_SENSITIVITY_RES_FILE_NAME* parameter. By default a basis type sensitivity analysis is performed. However, the type of sensitivity analysis (basis or optimal partition) can be changed by setting the parameter *MSK_IPAR_SENSITIVITY_TYPE* appropriately. Following values are accepted for this parameter:

- *MSK_SENSITIVITY_TYPE_BASIS*
- *MSK_SENSITIVITY_TYPE_OPTIMAL_PARTITION*

12.2.1 Sensitivity Analysis Specification File

MOSEK employs an MPS-like file format to specify on which model parameters the sensitivity analysis should be performed. As the optimal partition type sensitivity analysis can be computationally expensive it is important to limit the sensitivity analysis.

The format of the sensitivity specification file is shown in Listing 12.1, where capitalized names are keywords, and names in brackets are names of the constraints and variables to be included in the analysis.

Listing 12.1: Sensitivity analysis file specification.

```
BOUNDS CONSTRAINTS
U|L|LU [cname1]
U|L|LU [cname2]-[cname3]
BOUNDS VARIABLES
U|L|LU [vname1]
U|L|LU [vname2]-[vname3]
OBJECTIVE VARIABLES
[vname1]
[vname2]-[vname3]
```

The sensitivity specification file has three sections, i.e.

- `BOUNDS CONSTRAINTS`: Specifies on which bounds on constraints the sensitivity analysis should be performed.
- `BOUNDS VARIABLES`: Specifies on which bounds on variables the sensitivity analysis should be performed.
- `OBJECTIVE VARIABLES`: Specifies on which objective coefficients the sensitivity analysis should be performed.

A line in the body of a section must begin with a whitespace. In the `BOUNDS` sections one of the keys `L`, `U`, and `LU` must appear next. These keys specify whether the sensitivity analysis is performed on the lower bound, on the upper bound, or on both the lower and the upper bound respectively. Next, a single constraint (variable) or range of constraints (variables) is specified.

Recall from Section *12.1.1.1* that equality constraints are handled in a special way. Sensitivity analysis of an equality constraint can be specified with either `L`, `U`, or `LU`, all indicating the same, namely that upper and lower bounds (which are equal) are perturbed simultaneously.

As an example consider

```
BOUNDS CONSTRAINTS
L  "cons1"
U  "cons2"
LU "cons3"-"cons6"
```

which requests that sensitivity analysis is performed on the lower bound of the constraint named `cons1`, on the upper bound of the constraint named `cons2`, and on both lower and upper bound on the constraints named `cons3` to `cons6`.

It is allowed to use indexes instead of names, for instance

```
BOUNDS CONSTRAINTS
L  "cons1"
U  2
LU 3 - 6
```

The character * indicates that the line contains a comment and is ignored.

12.2.2 Example: Sensitivity Analysis from Command Line

As an example consider problem (12.3): the sensitivity file shown below (included in the distribution among the examples).

Listing 12.2: Sensitivity file for problem (12.3).

```
* Comment 1

BOUNDS CONSTRAINTS
 U "c1"          * Analyze upper bound for constraints named c1
 U 2             * Analyze upper bound for constraints with index 2
 U 3-5           * Analyze upper bound for constraint with index in interval [3:5]

VARIABLES CONSTRAINTS
 L 2-4           * This section specifies which bounds on variables should be analyzed.
 L "x11"
OBJECTIVE CONSTRAINTS
 "x11"           * This section specifies which objective coeficients should be analysed.
 2
```

The command

```
mosek transport.lp -sen sensitivity.ssp  -d MSK_IPAR_SENSITIVITY_TYPE sensitivitytype.basis
```

produces the output file as follow

```
BOUNDS CONSTRAINTS
INDEX    NAME            BOUND    LEFTRANGE        RIGHTRANGE       LEFTPRICE       ␣
 ↪RIGHTPRICE
0        c1              UP       -6.574875e-18    5.000000e+02     1.000000e+00     1.
 ↪000000e+00
2        c3              UP       -6.574875e-18    5.000000e+02     1.000000e+00     1.
 ↪000000e+00
3        c4              FIX      -5.000000e+02    6.574875e-18     2.000000e+00     2.
 ↪000000e+00
4        c5              FIX      -1.000000e+02    6.574875e-18     3.000000e+00     3.
 ↪000000e+00
5        c6              FIX      -5.000000e+02    6.574875e-18     3.000000e+00     3.
 ↪000000e+00

BOUNDS VARIABLES
INDEX    NAME            BOUND    LEFTRANGE        RIGHTRANGE       LEFTPRICE       ␣
 ↪RIGHTPRICE
2        x23             LO       -6.574875e-18    5.000000e+02     2.000000e+00     2.
 ↪000000e+00
3        x24             LO       -inf             5.000000e+02     0.000000e+00     0.
 ↪000000e+00
4        x31             LO       -inf             5.000000e+02     0.000000e+00     0.
 ↪000000e+00
```

```
0        x11             LO       -inf             3.000000e+02     0.000000e+00     0.
↪000000e+00

OBJECTIVE VARIABLES
INDEX    NAME                     LEFTRANGE        RIGHTRANGE       LEFTPRICE        ␣
↪RIGHTPRICE
0        x11                      -inf             1.000000e+00     3.000000e+02     3.
↪000000e+02
2        x23                      -2.000000e+00    +inf             0.000000e+00     0.
↪000000e+00
```

12.2.3 Controlling Log Output

Setting the parameter *MSK_IPAR_LOG_SENSITIVITY* to 1 or 0 (default) controls whether or not the results from sensitivity calculations are printed to the message stream.

The parameter *MSK_IPAR_LOG_SENSITIVITY_OPT* controls the amount of debug information on internal calculations from the sensitivity analysis.

CHAPTER

THIRTEEN

API REFERENCE

13.1 Parameters grouped by topic

Analysis

- *MSK_DPAR_ANA_SOL_INFEAS_TOL*
- *MSK_IPAR_ANA_SOL_BASIS*
- *MSK_IPAR_ANA_SOL_PRINT_VIOLATED*
- *MSK_IPAR_LOG_ANA_PRO*

Basis identification

- *MSK_DPAR_SIM_LU_TOL_REL_PIV*
- *MSK_IPAR_BI_CLEAN_OPTIMIZER*
- *MSK_IPAR_BI_IGNORE_MAX_ITER*
- *MSK_IPAR_BI_IGNORE_NUM_ERROR*
- *MSK_IPAR_BI_MAX_ITERATIONS*
- *MSK_IPAR_INTPNT_BASIS*
- *MSK_IPAR_LOG_BI*
- *MSK_IPAR_LOG_BI_FREQ*

Conic interior-point method

- *MSK_DPAR_INTPNT_CO_TOL_DFEAS*
- *MSK_DPAR_INTPNT_CO_TOL_INFEAS*
- *MSK_DPAR_INTPNT_CO_TOL_MU_RED*
- *MSK_DPAR_INTPNT_CO_TOL_NEAR_REL*
- *MSK_DPAR_INTPNT_CO_TOL_PFEAS*
- *MSK_DPAR_INTPNT_CO_TOL_REL_GAP*

Data check

- *MSK_DPAR_DATA_SYM_MAT_TOL*
- *MSK_DPAR_DATA_SYM_MAT_TOL_HUGE*
- *MSK_DPAR_DATA_SYM_MAT_TOL_LARGE*
- *MSK_DPAR_DATA_TOL_AIJ*
- *MSK_DPAR_DATA_TOL_AIJ_HUGE*
- *MSK_DPAR_DATA_TOL_AIJ_LARGE*
- *MSK_DPAR_DATA_TOL_BOUND_INF*
- *MSK_DPAR_DATA_TOL_BOUND_WRN*
- *MSK_DPAR_DATA_TOL_C_HUGE*
- *MSK_DPAR_DATA_TOL_CJ_LARGE*
- *MSK_DPAR_DATA_TOL_QIJ*
- *MSK_DPAR_DATA_TOL_X*
- *MSK_DPAR_SEMIDEFINITE_TOL_APPROX*
- *MSK_IPAR_CHECK_CONVEXITY*
- *MSK_IPAR_LOG_CHECK_CONVEXITY*

Data input/output

- *MSK_IPAR_INFEAS_REPORT_AUTO*
- *MSK_IPAR_LOG_FILE*
- *MSK_IPAR_OPF_MAX_TERMS_PER_LINE*
- *MSK_IPAR_OPF_WRITE_HEADER*
- *MSK_IPAR_OPF_WRITE_HINTS*
- *MSK_IPAR_OPF_WRITE_PARAMETERS*
- *MSK_IPAR_OPF_WRITE_PROBLEM*
- *MSK_IPAR_OPF_WRITE_SOL_BAS*
- *MSK_IPAR_OPF_WRITE_SOL_ITG*
- *MSK_IPAR_OPF_WRITE_SOL_ITR*
- *MSK_IPAR_OPF_WRITE_SOLUTIONS*
- *MSK_IPAR_PARAM_READ_CASE_NAME*
- *MSK_IPAR_PARAM_READ_IGN_ERROR*
- *MSK_IPAR_READ_DATA_COMPRESSED*
- *MSK_IPAR_READ_DATA_FORMAT*
- *MSK_IPAR_READ_DEBUG*
- *MSK_IPAR_READ_KEEP_FREE_CON*
- *MSK_IPAR_READ_LP_DROP_NEW_VARS_IN_BOU*
- *MSK_IPAR_READ_LP_QUOTED_NAMES*
- *MSK_IPAR_READ_MPS_FORMAT*

- *MSK_IPAR_READ_MPS_WIDTH*
- *MSK_IPAR_READ_TASK_IGNORE_PARAM*
- *MSK_IPAR_SOL_READ_NAME_WIDTH*
- *MSK_IPAR_SOL_READ_WIDTH*
- *MSK_IPAR_WRITE_BAS_CONSTRAINTS*
- *MSK_IPAR_WRITE_BAS_HEAD*
- *MSK_IPAR_WRITE_BAS_VARIABLES*
- *MSK_IPAR_WRITE_DATA_COMPRESSED*
- *MSK_IPAR_WRITE_DATA_FORMAT*
- *MSK_IPAR_WRITE_DATA_PARAM*
- *MSK_IPAR_WRITE_FREE_CON*
- *MSK_IPAR_WRITE_GENERIC_NAMES*
- *MSK_IPAR_WRITE_GENERIC_NAMES_IO*
- *MSK_IPAR_WRITE_IGNORE_INCOMPATIBLE_ITEMS*
- *MSK_IPAR_WRITE_INT_CONSTRAINTS*
- *MSK_IPAR_WRITE_INT_HEAD*
- *MSK_IPAR_WRITE_INT_VARIABLES*
- *MSK_IPAR_WRITE_LP_FULL_OBJ*
- *MSK_IPAR_WRITE_LP_LINE_WIDTH*
- *MSK_IPAR_WRITE_LP_QUOTED_NAMES*
- *MSK_IPAR_WRITE_LP_STRICT_FORMAT*
- *MSK_IPAR_WRITE_LP_TERMS_PER_LINE*
- *MSK_IPAR_WRITE_MPS_FORMAT*
- *MSK_IPAR_WRITE_MPS_INT*
- *MSK_IPAR_WRITE_PRECISION*
- *MSK_IPAR_WRITE_SOL_BARVARIABLES*
- *MSK_IPAR_WRITE_SOL_CONSTRAINTS*
- *MSK_IPAR_WRITE_SOL_HEAD*
- *MSK_IPAR_WRITE_SOL_IGNORE_INVALID_NAMES*
- *MSK_IPAR_WRITE_SOL_VARIABLES*
- *MSK_IPAR_WRITE_TASK_INC_SOL*
- *MSK_IPAR_WRITE_XML_MODE*
- *MSK_SPAR_BAS_SOL_FILE_NAME*
- *MSK_SPAR_DATA_FILE_NAME*
- *MSK_SPAR_DEBUG_FILE_NAME*
- *MSK_SPAR_INT_SOL_FILE_NAME*
- *MSK_SPAR_ITR_SOL_FILE_NAME*
- *MSK_SPAR_MIO_DEBUG_STRING*
- *MSK_SPAR_PARAM_COMMENT_SIGN*

- *MSK_SPAR_PARAM_READ_FILE_NAME*
- *MSK_SPAR_PARAM_WRITE_FILE_NAME*
- *MSK_SPAR_READ_MPS_BOU_NAME*
- *MSK_SPAR_READ_MPS_OBJ_NAME*
- *MSK_SPAR_READ_MPS_RAN_NAME*
- *MSK_SPAR_READ_MPS_RHS_NAME*
- *MSK_SPAR_SENSITIVITY_FILE_NAME*
- *MSK_SPAR_SENSITIVITY_RES_FILE_NAME*
- *MSK_SPAR_SOL_FILTER_XC_LOW*
- *MSK_SPAR_SOL_FILTER_XC_UPR*
- *MSK_SPAR_SOL_FILTER_XX_LOW*
- *MSK_SPAR_SOL_FILTER_XX_UPR*
- *MSK_SPAR_STAT_FILE_NAME*
- *MSK_SPAR_STAT_KEY*
- *MSK_SPAR_STAT_NAME*
- *MSK_SPAR_WRITE_LP_GEN_VAR_NAME*

Debugging

- *MSK_IPAR_AUTO_SORT_A_BEFORE_OPT*

Dual simplex

- *MSK_IPAR_SIM_DUAL_CRASH*
- *MSK_IPAR_SIM_DUAL_RESTRICT_SELECTION*
- *MSK_IPAR_SIM_DUAL_SELECTION*

Infeasibility report

- *MSK_IPAR_INFEAS_GENERIC_NAMES*
- *MSK_IPAR_INFEAS_REPORT_LEVEL*
- *MSK_IPAR_LOG_INFEAS_ANA*

Interior-point method

- *MSK_DPAR_CHECK_CONVEXITY_REL_TOL*
- *MSK_DPAR_INTPNT_CO_TOL_DFEAS*
- *MSK_DPAR_INTPNT_CO_TOL_INFEAS*
- *MSK_DPAR_INTPNT_CO_TOL_MU_RED*
- *MSK_DPAR_INTPNT_CO_TOL_NEAR_REL*
- *MSK_DPAR_INTPNT_CO_TOL_PFEAS*
- *MSK_DPAR_INTPNT_CO_TOL_REL_GAP*

- *MSK_DPAR_INTPNT_NL_MERIT_BAL*
- *MSK_DPAR_INTPNT_NL_TOL_DFEAS*
- *MSK_DPAR_INTPNT_NL_TOL_MU_RED*
- *MSK_DPAR_INTPNT_NL_TOL_NEAR_REL*
- *MSK_DPAR_INTPNT_NL_TOL_PFEAS*
- *MSK_DPAR_INTPNT_NL_TOL_REL_GAP*
- *MSK_DPAR_INTPNT_NL_TOL_REL_STEP*
- *MSK_DPAR_INTPNT_QO_TOL_DFEAS*
- *MSK_DPAR_INTPNT_QO_TOL_INFEAS*
- *MSK_DPAR_INTPNT_QO_TOL_MU_RED*
- *MSK_DPAR_INTPNT_QO_TOL_NEAR_REL*
- *MSK_DPAR_INTPNT_QO_TOL_PFEAS*
- *MSK_DPAR_INTPNT_QO_TOL_REL_GAP*
- *MSK_DPAR_INTPNT_TOL_DFEAS*
- *MSK_DPAR_INTPNT_TOL_DSAFE*
- *MSK_DPAR_INTPNT_TOL_INFEAS*
- *MSK_DPAR_INTPNT_TOL_MU_RED*
- *MSK_DPAR_INTPNT_TOL_PATH*
- *MSK_DPAR_INTPNT_TOL_PFEAS*
- *MSK_DPAR_INTPNT_TOL_PSAFE*
- *MSK_DPAR_INTPNT_TOL_REL_GAP*
- *MSK_DPAR_INTPNT_TOL_REL_STEP*
- *MSK_DPAR_INTPNT_TOL_STEP_SIZE*
- *MSK_DPAR_QCQO_REFORMULATE_REL_DROP_TOL*
- *MSK_IPAR_BI_IGNORE_MAX_ITER*
- *MSK_IPAR_BI_IGNORE_NUM_ERROR*
- *MSK_IPAR_INTPNT_BASIS*
- *MSK_IPAR_INTPNT_DIFF_STEP*
- *MSK_IPAR_INTPNT_HOTSTART*
- *MSK_IPAR_INTPNT_MAX_ITERATIONS*
- *MSK_IPAR_INTPNT_MAX_NUM_COR*
- *MSK_IPAR_INTPNT_MAX_NUM_REFINEMENT_STEPS*
- *MSK_IPAR_INTPNT_OFF_COL_TRH*
- *MSK_IPAR_INTPNT_ORDER_METHOD*
- *MSK_IPAR_INTPNT_REGULARIZATION_USE*
- *MSK_IPAR_INTPNT_SCALING*
- *MSK_IPAR_INTPNT_SOLVE_FORM*
- *MSK_IPAR_INTPNT_STARTING_POINT*
- *MSK_IPAR_LOG_INTPNT*

License manager

- *MSK_IPAR_CACHE_LICENSE*
- *MSK_IPAR_LICENSE_DEBUG*
- *MSK_IPAR_LICENSE_PAUSE_TIME*
- *MSK_IPAR_LICENSE_SUPPRESS_EXPIRE_WRNS*
- *MSK_IPAR_LICENSE_TRH_EXPIRY_WRN*
- *MSK_IPAR_LICENSE_WAIT*

Logging

- *MSK_IPAR_LOG*
- *MSK_IPAR_LOG_ANA_PRO*
- *MSK_IPAR_LOG_BI*
- *MSK_IPAR_LOG_BI_FREQ*
- *MSK_IPAR_LOG_CUT_SECOND_OPT*
- *MSK_IPAR_LOG_EXPAND*
- *MSK_IPAR_LOG_FEAS_REPAIR*
- *MSK_IPAR_LOG_FILE*
- *MSK_IPAR_LOG_INFEAS_ANA*
- *MSK_IPAR_LOG_INTPNT*
- *MSK_IPAR_LOG_MIO*
- *MSK_IPAR_LOG_MIO_FREQ*
- *MSK_IPAR_LOG_ORDER*
- *MSK_IPAR_LOG_PRESOLVE*
- *MSK_IPAR_LOG_RESPONSE*
- *MSK_IPAR_LOG_SENSITIVITY*
- *MSK_IPAR_LOG_SENSITIVITY_OPT*
- *MSK_IPAR_LOG_SIM*
- *MSK_IPAR_LOG_SIM_FREQ*
- *MSK_IPAR_LOG_STORAGE*

Mixed-integer optimization

- *MSK_DPAR_MIO_DISABLE_TERM_TIME*
- *MSK_DPAR_MIO_MAX_TIME*
- *MSK_DPAR_MIO_NEAR_TOL_ABS_GAP*
- *MSK_DPAR_MIO_NEAR_TOL_REL_GAP*
- *MSK_DPAR_MIO_REL_GAP_CONST*
- *MSK_DPAR_MIO_TOL_ABS_GAP*
- *MSK_DPAR_MIO_TOL_ABS_RELAX_INT*

- *MSK_DPAR_MIO_TOL_FEAS*
- *MSK_DPAR_MIO_TOL_REL_DUAL_BOUND_IMPROVEMENT*
- *MSK_DPAR_MIO_TOL_REL_GAP*
- *MSK_IPAR_LOG_MIO*
- *MSK_IPAR_LOG_MIO_FREQ*
- *MSK_IPAR_MIO_BRANCH_DIR*
- *MSK_IPAR_MIO_CONSTRUCT_SOL*
- *MSK_IPAR_MIO_CUT_CLIQUE*
- *MSK_IPAR_MIO_CUT_CMIR*
- *MSK_IPAR_MIO_CUT_GMI*
- *MSK_IPAR_MIO_CUT_IMPLIED_BOUND*
- *MSK_IPAR_MIO_CUT_KNAPSACK_COVER*
- *MSK_IPAR_MIO_CUT_SELECTION_LEVEL*
- *MSK_IPAR_MIO_HEURISTIC_LEVEL*
- *MSK_IPAR_MIO_MAX_NUM_BRANCHES*
- *MSK_IPAR_MIO_MAX_NUM_RELAXS*
- *MSK_IPAR_MIO_MAX_NUM_SOLUTIONS*
- *MSK_IPAR_MIO_NODE_OPTIMIZER*
- *MSK_IPAR_MIO_NODE_SELECTION*
- *MSK_IPAR_MIO_PERSPECTIVE_REFORMULATE*
- *MSK_IPAR_MIO_PROBING_LEVEL*
- *MSK_IPAR_MIO_RINS_MAX_NODES*
- *MSK_IPAR_MIO_ROOT_OPTIMIZER*
- *MSK_IPAR_MIO_ROOT_REPEAT_PRESOLVE_LEVEL*
- *MSK_IPAR_MIO_VB_DETECTION_LEVEL*

Nonlinear convex method

- *MSK_DPAR_INTPNT_NL_MERIT_BAL*
- *MSK_DPAR_INTPNT_NL_TOL_DFEAS*
- *MSK_DPAR_INTPNT_NL_TOL_MU_RED*
- *MSK_DPAR_INTPNT_NL_TOL_NEAR_REL*
- *MSK_DPAR_INTPNT_NL_TOL_PFEAS*
- *MSK_DPAR_INTPNT_NL_TOL_REL_GAP*
- *MSK_DPAR_INTPNT_NL_TOL_REL_STEP*
- *MSK_DPAR_INTPNT_TOL_INFEAS*
- *MSK_IPAR_CHECK_CONVEXITY*
- *MSK_IPAR_LOG_CHECK_CONVEXITY*

Output information

- *MSK_IPAR_INFEAS_REPORT_LEVEL*
- *MSK_IPAR_LICENSE_SUPPRESS_EXPIRE_WRNS*
- *MSK_IPAR_LICENSE_TRH_EXPIRY_WRN*
- *MSK_IPAR_LOG*
- *MSK_IPAR_LOG_BI*
- *MSK_IPAR_LOG_BI_FREQ*
- *MSK_IPAR_LOG_CUT_SECOND_OPT*
- *MSK_IPAR_LOG_EXPAND*
- *MSK_IPAR_LOG_FEAS_REPAIR*
- *MSK_IPAR_LOG_FILE*
- *MSK_IPAR_LOG_INFEAS_ANA*
- *MSK_IPAR_LOG_INTPNT*
- *MSK_IPAR_LOG_MIO*
- *MSK_IPAR_LOG_MIO_FREQ*
- *MSK_IPAR_LOG_ORDER*
- *MSK_IPAR_LOG_RESPONSE*
- *MSK_IPAR_LOG_SENSITIVITY*
- *MSK_IPAR_LOG_SENSITIVITY_OPT*
- *MSK_IPAR_LOG_SIM*
- *MSK_IPAR_LOG_SIM_FREQ*
- *MSK_IPAR_LOG_SIM_MINOR*
- *MSK_IPAR_LOG_STORAGE*
- *MSK_IPAR_MAX_NUM_WARNINGS*

Overall solver

- *MSK_IPAR_BI_CLEAN_OPTIMIZER*
- *MSK_IPAR_INFEAS_PREFER_PRIMAL*
- *MSK_IPAR_LICENSE_WAIT*
- *MSK_IPAR_MIO_MODE*
- *MSK_IPAR_OPTIMIZER*
- *MSK_IPAR_PRESOLVE_LEVEL*
- *MSK_IPAR_PRESOLVE_MAX_NUM_REDUCTIONS*
- *MSK_IPAR_PRESOLVE_USE*
- *MSK_IPAR_PRIMAL_REPAIR_OPTIMIZER*
- *MSK_IPAR_SENSITIVITY_ALL*
- *MSK_IPAR_SENSITIVITY_OPTIMIZER*
- *MSK_IPAR_SENSITIVITY_TYPE*

- *MSK_IPAR_SOLUTION_CALLBACK*

Overall system

- *MSK_IPAR_AUTO_UPDATE_SOL_INFO*
- *MSK_IPAR_INTPNT_MULTI_THREAD*
- *MSK_IPAR_LICENSE_WAIT*
- *MSK_IPAR_LOG_STORAGE*
- *MSK_IPAR_MIO_MT_USER_CB*
- *MSK_IPAR_MT_SPINCOUNT*
- *MSK_IPAR_NUM_THREADS*
- *MSK_IPAR_REMOVE_UNUSED_SOLUTIONS*
- *MSK_IPAR_TIMING_LEVEL*
- *MSK_SPAR_REMOTE_ACCESS_TOKEN*

Presolve

- *MSK_DPAR_PRESOLVE_TOL_ABS_LINDEP*
- *MSK_DPAR_PRESOLVE_TOL_AIJ*
- *MSK_DPAR_PRESOLVE_TOL_REL_LINDEP*
- *MSK_DPAR_PRESOLVE_TOL_S*
- *MSK_DPAR_PRESOLVE_TOL_X*
- *MSK_IPAR_PRESOLVE_ELIMINATOR_MAX_FILL*
- *MSK_IPAR_PRESOLVE_ELIMINATOR_MAX_NUM_TRIES*
- *MSK_IPAR_PRESOLVE_LEVEL*
- *MSK_IPAR_PRESOLVE_LINDEP_ABS_WORK_TRH*
- *MSK_IPAR_PRESOLVE_LINDEP_REL_WORK_TRH*
- *MSK_IPAR_PRESOLVE_LINDEP_USE*
- *MSK_IPAR_PRESOLVE_MAX_NUM_REDUCTIONS*
- *MSK_IPAR_PRESOLVE_USE*

Primal simplex

- *MSK_IPAR_SIM_PRIMAL_CRASH*
- *MSK_IPAR_SIM_PRIMAL_RESTRICT_SELECTION*
- *MSK_IPAR_SIM_PRIMAL_SELECTION*

Progress callback

- *MSK_IPAR_SOLUTION_CALLBACK*

Simplex optimizer

- *MSK_DPAR_BASIS_REL_TOL_S*
- *MSK_DPAR_BASIS_TOL_S*
- *MSK_DPAR_BASIS_TOL_X*
- *MSK_DPAR_SIM_LU_TOL_REL_PIV*
- *MSK_DPAR_SIMPLEX_ABS_TOL_PIV*
- *MSK_IPAR_BASIS_SOLVE_USE_PLUS_ONE*
- *MSK_IPAR_LOG_SIM*
- *MSK_IPAR_LOG_SIM_FREQ*
- *MSK_IPAR_LOG_SIM_MINOR*
- *MSK_IPAR_SENSITIVITY_OPTIMIZER*
- *MSK_IPAR_SIM_BASIS_FACTOR_USE*
- *MSK_IPAR_SIM_DEGEN*
- *MSK_IPAR_SIM_DUAL_PHASEONE_METHOD*
- *MSK_IPAR_SIM_EXPLOIT_DUPVEC*
- *MSK_IPAR_SIM_HOTSTART*
- *MSK_IPAR_SIM_HOTSTART_LU*
- *MSK_IPAR_SIM_MAX_ITERATIONS*
- *MSK_IPAR_SIM_MAX_NUM_SETBACKS*
- *MSK_IPAR_SIM_NON_SINGULAR*
- *MSK_IPAR_SIM_PRIMAL_PHASEONE_METHOD*
- *MSK_IPAR_SIM_REFACTOR_FREQ*
- *MSK_IPAR_SIM_REFORMULATION*
- *MSK_IPAR_SIM_SAVE_LU*
- *MSK_IPAR_SIM_SCALING*
- *MSK_IPAR_SIM_SCALING_METHOD*
- *MSK_IPAR_SIM_SOLVE_FORM*
- *MSK_IPAR_SIM_STABILITY_PRIORITY*
- *MSK_IPAR_SIM_SWITCH_OPTIMIZER*

Solution input/output

- *MSK_IPAR_INFEAS_REPORT_AUTO*
- *MSK_IPAR_SOL_FILTER_KEEP_BASIC*
- *MSK_IPAR_SOL_FILTER_KEEP_RANGED*
- *MSK_IPAR_SOL_READ_NAME_WIDTH*
- *MSK_IPAR_SOL_READ_WIDTH*
- *MSK_IPAR_WRITE_BAS_CONSTRAINTS*
- *MSK_IPAR_WRITE_BAS_HEAD*

- *MSK_IPAR_WRITE_BAS_VARIABLES*
- *MSK_IPAR_WRITE_INT_CONSTRAINTS*
- *MSK_IPAR_WRITE_INT_HEAD*
- *MSK_IPAR_WRITE_INT_VARIABLES*
- *MSK_IPAR_WRITE_SOL_BARVARIABLES*
- *MSK_IPAR_WRITE_SOL_CONSTRAINTS*
- *MSK_IPAR_WRITE_SOL_HEAD*
- *MSK_IPAR_WRITE_SOL_IGNORE_INVALID_NAMES*
- *MSK_IPAR_WRITE_SOL_VARIABLES*
- *MSK_SPAR_BAS_SOL_FILE_NAME*
- *MSK_SPAR_INT_SOL_FILE_NAME*
- *MSK_SPAR_ITR_SOL_FILE_NAME*
- *MSK_SPAR_SOL_FILTER_XC_LOW*
- *MSK_SPAR_SOL_FILTER_XC_UPR*
- *MSK_SPAR_SOL_FILTER_XX_LOW*
- *MSK_SPAR_SOL_FILTER_XX_UPR*

Termination criteria

- *MSK_DPAR_BASIS_REL_TOL_S*
- *MSK_DPAR_BASIS_TOL_S*
- *MSK_DPAR_BASIS_TOL_X*
- *MSK_DPAR_INTPNT_CO_TOL_DFEAS*
- *MSK_DPAR_INTPNT_CO_TOL_INFEAS*
- *MSK_DPAR_INTPNT_CO_TOL_MU_RED*
- *MSK_DPAR_INTPNT_CO_TOL_NEAR_REL*
- *MSK_DPAR_INTPNT_CO_TOL_PFEAS*
- *MSK_DPAR_INTPNT_CO_TOL_REL_GAP*
- *MSK_DPAR_INTPNT_NL_TOL_DFEAS*
- *MSK_DPAR_INTPNT_NL_TOL_MU_RED*
- *MSK_DPAR_INTPNT_NL_TOL_NEAR_REL*
- *MSK_DPAR_INTPNT_NL_TOL_PFEAS*
- *MSK_DPAR_INTPNT_NL_TOL_REL_GAP*
- *MSK_DPAR_INTPNT_QO_TOL_DFEAS*
- *MSK_DPAR_INTPNT_QO_TOL_INFEAS*
- *MSK_DPAR_INTPNT_QO_TOL_MU_RED*
- *MSK_DPAR_INTPNT_QO_TOL_NEAR_REL*
- *MSK_DPAR_INTPNT_QO_TOL_PFEAS*
- *MSK_DPAR_INTPNT_QO_TOL_REL_GAP*
- *MSK_DPAR_INTPNT_TOL_DFEAS*

- *MSK_DPAR_INTPNT_TOL_INFEAS*
- *MSK_DPAR_INTPNT_TOL_MU_RED*
- *MSK_DPAR_INTPNT_TOL_PFEAS*
- *MSK_DPAR_INTPNT_TOL_REL_GAP*
- *MSK_DPAR_LOWER_OBJ_CUT*
- *MSK_DPAR_LOWER_OBJ_CUT_FINITE_TRH*
- *MSK_DPAR_MIO_DISABLE_TERM_TIME*
- *MSK_DPAR_MIO_MAX_TIME*
- *MSK_DPAR_MIO_NEAR_TOL_REL_GAP*
- *MSK_DPAR_MIO_REL_GAP_CONST*
- *MSK_DPAR_MIO_TOL_REL_GAP*
- *MSK_DPAR_OPTIMIZER_MAX_TIME*
- *MSK_DPAR_UPPER_OBJ_CUT*
- *MSK_DPAR_UPPER_OBJ_CUT_FINITE_TRH*
- *MSK_IPAR_BI_MAX_ITERATIONS*
- *MSK_IPAR_INTPNT_MAX_ITERATIONS*
- *MSK_IPAR_MIO_MAX_NUM_BRANCHES*
- *MSK_IPAR_MIO_MAX_NUM_SOLUTIONS*
- *MSK_IPAR_SIM_MAX_ITERATIONS*

Other

- *MSK_IPAR_COMPRESS_STATFILE*

13.2 Parameters (alphabetical list sorted by type)

- *Double parameters*
- *Integer parameters*
- *String parameters*

13.2.1 Double parameters

MSK_DPAR_ANA_SOL_INFEAS_TOL
: If a constraint violates its bound with an amount larger than this value, the constraint name, index and violation will be printed by the solution analyzer.

  Default 1e-6

  Accepted [0.0; +inf]

  Groups *Analysis*

MSK_DPAR_BASIS_REL_TOL_S
: Maximum relative dual bound violation allowed in an optimal basic solution.

  Default 1.0e-12

  Accepted [0.0; +inf]

Groups *Simplex optimizer*, *Termination criteria*

`MSK_DPAR_BASIS_TOL_S`
Maximum absolute dual bound violation in an optimal basic solution.

Default 1.0e-6

Accepted [1.0e-9; +inf]

Groups *Simplex optimizer*, *Termination criteria*

`MSK_DPAR_BASIS_TOL_X`
Maximum absolute primal bound violation allowed in an optimal basic solution.

Default 1.0e-6

Accepted [1.0e-9; +inf]

Groups *Simplex optimizer*, *Termination criteria*

`MSK_DPAR_CHECK_CONVEXITY_REL_TOL`
This parameter controls when the full convexity check declares a problem to be non-convex. Increasing this tolerance relaxes the criteria for declaring the problem non-convex.

A problem is declared non-convex if negative (positive) pivot elements are detected in the Cholesky factor of a matrix which is required to be PSD (NSD). This parameter controls how much this non-negativity requirement may be violated.

If d_i is the pivot element for column i, then the matrix Q is considered to not be PSD if:

$$d_i \leq -|Q_{ii}|\texttt{check_convexity_rel_tol}$$

Default 1e-10

Accepted [0; +inf]

Groups *Interior-point method*

`MSK_DPAR_DATA_SYM_MAT_TOL`
Absolute zero tolerance for elements in in suymmetric matrixes. If any value in a symmetric matrix is smaller than this parameter in absolute terms **MOSEK** will treat the values as zero and generate a warning.

Default 1.0e-12

Accepted [1.0e-16; 1.0e-6]

Groups *Data check*

`MSK_DPAR_DATA_SYM_MAT_TOL_HUGE`
An element in a symmetric matrix which is larger than this value in absolute size causes an error.

Default 1.0e20

Accepted [0.0; +inf]

Groups *Data check*

`MSK_DPAR_DATA_SYM_MAT_TOL_LARGE`
An element in a symmetric matrix which is larger than this value in absolute size causes a warning message to be printed.

Default 1.0e10

Accepted [0.0; +inf]

Groups *Data check*

`MSK_DPAR_DATA_TOL_AIJ`
Absolute zero tolerance for elements in A. If any value A_{ij} is smaller than this parameter in absolute terms **MOSEK** will treat the values as zero and generate a warning.

Default 1.0e-12

Accepted [1.0e-16; 1.0e-6]

Groups *Data check*

`MSK_DPAR_DATA_TOL_AIJ_HUGE`
An element in A which is larger than this value in absolute size causes an error.

Default 1.0e20

Accepted [0.0; +inf]

Groups *Data check*

`MSK_DPAR_DATA_TOL_AIJ_LARGE`
An element in A which is larger than this value in absolute size causes a warning message to be printed.

Default 1.0e10

Accepted [0.0; +inf]

Groups *Data check*

`MSK_DPAR_DATA_TOL_BOUND_INF`
Any bound which in absolute value is greater than this parameter is considered infinite.

Default 1.0e16

Accepted [0.0; +inf]

Groups *Data check*

`MSK_DPAR_DATA_TOL_BOUND_WRN`
If a bound value is larger than this value in absolute size, then a warning message is issued.

Default 1.0e8

Accepted [0.0; +inf]

Groups *Data check*

`MSK_DPAR_DATA_TOL_C_HUGE`
An element in c which is larger than the value of this parameter in absolute terms is considered to be huge and generates an error.

Default 1.0e16

Accepted [0.0; +inf]

Groups *Data check*

`MSK_DPAR_DATA_TOL_CJ_LARGE`
An element in c which is larger than this value in absolute terms causes a warning message to be printed.

Default 1.0e8

Accepted [0.0; +inf]

Groups *Data check*

`MSK_DPAR_DATA_TOL_QIJ`
Absolute zero tolerance for elements in Q matrices.

Default 1.0e-16

Accepted [0.0; +inf]

Groups *Data check*

`MSK_DPAR_DATA_TOL_X`
Zero tolerance for constraints and variables i.e. if the distance between the lower and upper bound is less than this value, then the lower and upper bound is considered identical.

Default 1.0e-8

Accepted [0.0; +inf]

Groups *Data check*

`MSK_DPAR_INTPNT_CO_TOL_DFEAS`
Dual feasibility tolerance used by the conic interior-point optimizer.

Default 1.0e-8

Accepted [0.0; 1.0]

Groups *Interior-point method*, *Termination criteria*, *Conic interior-point method*

See also *MSK_DPAR_INTPNT_CO_TOL_NEAR_REL*

`MSK_DPAR_INTPNT_CO_TOL_INFEAS`
Controls when the conic interior-point optimizer declares the model primal or dual infeasible. A small number means the optimizer gets more conservative about declaring the model infeasible.

Default 1.0e-10

Accepted [0.0; 1.0]

Groups *Interior-point method*, *Termination criteria*, *Conic interior-point method*

`MSK_DPAR_INTPNT_CO_TOL_MU_RED`
Relative complementarity gap feasibility tolerance used by the conic interior-point optimizer.

Default 1.0e-8

Accepted [0.0; 1.0]

Groups *Interior-point method*, *Termination criteria*, *Conic interior-point method*

`MSK_DPAR_INTPNT_CO_TOL_NEAR_REL`
If **MOSEK** cannot compute a solution that has the prescribed accuracy, then it will multiply the termination tolerances with value of this parameter. If the solution then satisfies the termination criteria, then the solution is denoted near optimal, near feasible and so forth.

Default 1000

Accepted [1.0; +inf]

Groups *Interior-point method*, *Termination criteria*, *Conic interior-point method*

`MSK_DPAR_INTPNT_CO_TOL_PFEAS`
Primal feasibility tolerance used by the conic interior-point optimizer.

Default 1.0e-8

Accepted [0.0; 1.0]

Groups *Interior-point method*, *Termination criteria*, *Conic interior-point method*

See also *MSK_DPAR_INTPNT_CO_TOL_NEAR_REL*

`MSK_DPAR_INTPNT_CO_TOL_REL_GAP`
Relative gap termination tolerance used by the conic interior-point optimizer.

Default 1.0e-7

Accepted [0.0; 1.0]

Groups *Interior-point method*, *Termination criteria*, *Conic interior-point method*

See also *MSK_DPAR_INTPNT_CO_TOL_NEAR_REL*

`MSK_DPAR_INTPNT_NL_MERIT_BAL`
Controls if the complementarity and infeasibility is converging to zero at about equal rates.

Default 1.0e-4

Accepted [0.0; 0.99]

Groups *Interior-point method*, *Nonlinear convex method*

`MSK_DPAR_INTPNT_NL_TOL_DFEAS`
Dual feasibility tolerance used when a nonlinear model is solved.

Default 1.0e-8

Accepted [0.0; 1.0]

Groups *Interior-point method*, *Termination criteria*, *Nonlinear convex method*

`MSK_DPAR_INTPNT_NL_TOL_MU_RED`
Relative complementarity gap tolerance.

Default 1.0e-12

Accepted [0.0; 1.0]

Groups *Interior-point method*, *Termination criteria*, *Nonlinear convex method*

`MSK_DPAR_INTPNT_NL_TOL_NEAR_REL`
If the **MOSEK** nonlinear interior-point optimizer cannot compute a solution that has the prescribed accuracy, then it will multiply the termination tolerances with value of this parameter. If the solution then satisfies the termination criteria, then the solution is denoted near optimal, near feasible and so forth.

Default 1000.0

Accepted [1.0; +inf]

Groups *Interior-point method*, *Termination criteria*, *Nonlinear convex method*

`MSK_DPAR_INTPNT_NL_TOL_PFEAS`
Primal feasibility tolerance used when a nonlinear model is solved.

Default 1.0e-8

Accepted [0.0; 1.0]

Groups *Interior-point method*, *Termination criteria*, *Nonlinear convex method*

`MSK_DPAR_INTPNT_NL_TOL_REL_GAP`
Relative gap termination tolerance for nonlinear problems.

Default 1.0e-6

Accepted [1.0e-14; +inf]

Groups *Termination criteria*, *Interior-point method*, *Nonlinear convex method*

`MSK_DPAR_INTPNT_NL_TOL_REL_STEP`
Relative step size to the boundary for general nonlinear optimization problems.

Default 0.995

Accepted [1.0e-4; 0.9999999]

Groups *Interior-point method*, *Nonlinear convex method*

`MSK_DPAR_INTPNT_QO_TOL_DFEAS`
Dual feasibility tolerance used when the interior-point optimizer is applied to a quadratic optimization problem..

Default 1.0e-8

Accepted [0.0; 1.0]

Groups *Interior-point method*, *Termination criteria*

See also *MSK_DPAR_INTPNT_QO_TOL_NEAR_REL*

MSK_DPAR_INTPNT_QO_TOL_INFEAS
Controls when the conic interior-point optimizer declares the model primal or dual infeasible. A small number means the optimizer gets more conservative about declaring the model infeasible.

Default 1.0e-10

Accepted [0.0; 1.0]

Groups *Interior-point method*, *Termination criteria*

MSK_DPAR_INTPNT_QO_TOL_MU_RED
Relative complementarity gap feasibility tolerance used when interior-point optimizer is applied to a quadratic optimization problem.

Default 1.0e-8

Accepted [0.0; 1.0]

Groups *Interior-point method*, *Termination criteria*

MSK_DPAR_INTPNT_QO_TOL_NEAR_REL
If **MOSEK** cannot compute a solution that has the prescribed accuracy, then it will multiply the termination tolerances with value of this parameter. If the solution then satisfies the termination criteria, then the solution is denoted near optimal, near feasible and so forth.

Default 1000

Accepted [1.0; +inf]

Groups *Interior-point method*, *Termination criteria*

MSK_DPAR_INTPNT_QO_TOL_PFEAS
Primal feasibility tolerance used when the interior-point optimizer is applied to a quadratic optimization problem.

Default 1.0e-8

Accepted [0.0; 1.0]

Groups *Interior-point method*, *Termination criteria*

See also *MSK_DPAR_INTPNT_QO_TOL_NEAR_REL*

MSK_DPAR_INTPNT_QO_TOL_REL_GAP
Relative gap termination tolerance used when the interior-point optimizer is applied to a quadratic optimization problem.

Default 1.0e-8

Accepted [0.0; 1.0]

Groups *Interior-point method*, *Termination criteria*

See also *MSK_DPAR_INTPNT_QO_TOL_NEAR_REL*

MSK_DPAR_INTPNT_TOL_DFEAS
Dual feasibility tolerance used for linear and quadratic optimization problems.

Default 1.0e-8

Accepted [0.0; 1.0]

Groups *Interior-point method*, *Termination criteria*

MSK_DPAR_INTPNT_TOL_DSAFE
Controls the initial dual starting point used by the interior-point optimizer. If the interior-point optimizer converges slowly and/or the constraint or variable bounds are very large, then it might be worthwhile to increase this value.

Default 1.0

Accepted [1.0e-4; +inf]

Groups *Interior-point method*

`MSK_DPAR_INTPNT_TOL_INFEAS`
Controls when the optimizer declares the model primal or dual infeasible. A small number means the optimizer gets more conservative about declaring the model infeasible.

Default 1.0e-10

Accepted [0.0; 1.0]

Groups *Interior-point method*, *Termination criteria*, *Nonlinear convex method*

`MSK_DPAR_INTPNT_TOL_MU_RED`
Relative complementarity gap tolerance.

Default 1.0e-16

Accepted [0.0; 1.0]

Groups *Interior-point method*, *Termination criteria*

`MSK_DPAR_INTPNT_TOL_PATH`
Controls how close the interior-point optimizer follows the central path. A large value of this parameter means the central is followed very closely. On numerical unstable problems it may be worthwhile to increase this parameter.

Default 1.0e-8

Accepted [0.0; 0.9999]

Groups *Interior-point method*

`MSK_DPAR_INTPNT_TOL_PFEAS`
Primal feasibility tolerance used for linear and quadratic optimization problems.

Default 1.0e-8

Accepted [0.0; 1.0]

Groups *Interior-point method*, *Termination criteria*

`MSK_DPAR_INTPNT_TOL_PSAFE`
Controls the initial primal starting point used by the interior-point optimizer. If the interior-point optimizer converges slowly and/or the constraint or variable bounds are very large, then it may be worthwhile to increase this value.

Default 1.0

Accepted [1.0e-4; +inf]

Groups *Interior-point method*

`MSK_DPAR_INTPNT_TOL_REL_GAP`
Relative gap termination tolerance.

Default 1.0e-8

Accepted [1.0e-14; +inf]

Groups *Termination criteria*, *Interior-point method*

`MSK_DPAR_INTPNT_TOL_REL_STEP`
Relative step size to the boundary for linear and quadratic optimization problems.

Default 0.9999

Accepted [1.0e-4; 0.999999]

Groups *Interior-point method*

`MSK_DPAR_INTPNT_TOL_STEP_SIZE`
Minimal step size tolerance. If the step size falls below the value of this parameter, then the interior-point optimizer assumes that it is stalled. In other words the interior-point optimizer does not make any progress and therefore it is better stop.

Default 1.0e-6

Accepted [0.0; 1.0]

Groups *Interior-point method*

`MSK_DPAR_LOWER_OBJ_CUT`
If either a primal or dual feasible solution is found proving that the optimal objective value is outside, the interval [*MSK_DPAR_LOWER_OBJ_CUT*, *MSK_DPAR_UPPER_OBJ_CUT*], then **MOSEK** is terminated.

Default -1.0e30

Accepted [-inf; +inf]

Groups *Termination criteria*

See also *MSK_DPAR_LOWER_OBJ_CUT_FINITE_TRH*

`MSK_DPAR_LOWER_OBJ_CUT_FINITE_TRH`
If the lower objective cut is less than the value of this parameter value, then the lower objective cut i.e. *MSK_DPAR_LOWER_OBJ_CUT* is treated as $-\infty$.

Default -0.5e30

Accepted [-inf; +inf]

Groups *Termination criteria*

`MSK_DPAR_MIO_DISABLE_TERM_TIME`

This parameter specifies the number of seconds n during which the termination criteria governed by

- *MSK_IPAR_MIO_MAX_NUM_RELAXS*
- *MSK_IPAR_MIO_MAX_NUM_BRANCHES*
- *MSK_DPAR_MIO_NEAR_TOL_ABS_GAP*
- *MSK_DPAR_MIO_NEAR_TOL_REL_GAP*

is disabled since the beginning of the optimization.

A negative value is identical to infinity i.e. the termination criteria are never checked.

Default -1.0

Accepted [-inf; +inf]

Groups *Mixed-integer optimization*, *Termination criteria*

See also *MSK_IPAR_MIO_MAX_NUM_RELAXS*, *MSK_IPAR_MIO_MAX_NUM_BRANCHES*, *MSK_DPAR_MIO_NEAR_TOL_ABS_GAP*, *MSK_DPAR_MIO_NEAR_TOL_REL_GAP*

`MSK_DPAR_MIO_MAX_TIME`
This parameter limits the maximum time spent by the mixed-integer optimizer. A negative number means infinity.

Default -1.0

Accepted [-inf; +inf]

Groups *Mixed-integer optimization*, *Termination criteria*

`MSK_DPAR_MIO_NEAR_TOL_ABS_GAP`
Relaxed absolute optimality tolerance employed by the mixed-integer optimizer. This termination criteria is delayed. See *MSK_DPAR_MIO_DISABLE_TERM_TIME* for details.

Default 0.0

Accepted [0.0; +inf]

Groups *Mixed-integer optimization*

See also *MSK_DPAR_MIO_DISABLE_TERM_TIME*

`MSK_DPAR_MIO_NEAR_TOL_REL_GAP`
The mixed-integer optimizer is terminated when this tolerance is satisfied. This termination criteria is delayed. See *MSK_DPAR_MIO_DISABLE_TERM_TIME* for details.

Default 1.0e-3

Accepted [0.0; +inf]

Groups *Mixed-integer optimization*, *Termination criteria*

See also *MSK_DPAR_MIO_DISABLE_TERM_TIME*

`MSK_DPAR_MIO_REL_GAP_CONST`
This value is used to compute the relative gap for the solution to an integer optimization problem.

Default 1.0e-10

Accepted [1.0e-15; +inf]

Groups *Mixed-integer optimization*, *Termination criteria*

`MSK_DPAR_MIO_TOL_ABS_GAP`
Absolute optimality tolerance employed by the mixed-integer optimizer.

Default 0.0

Accepted [0.0; +inf]

Groups *Mixed-integer optimization*

`MSK_DPAR_MIO_TOL_ABS_RELAX_INT`
Absolute integer feasibility tolerance. If the distance to the nearest integer is less than this tolerance then an integer constraint is assumed to be satisfied.

Default 1.0e-5

Accepted [1e-9; +inf]

Groups *Mixed-integer optimization*

`MSK_DPAR_MIO_TOL_FEAS`
Feasibility tolerance for mixed integer solver.

Default 1.0e-6

Accepted [1e-9; 1e-3]

Groups *Mixed-integer optimization*

`MSK_DPAR_MIO_TOL_REL_DUAL_BOUND_IMPROVEMENT`
If the relative improvement of the dual bound is smaller than this value, the solver will terminate the root cut generation. A value of 0.0 means that the value is selected automatically.

Default 0.0

Accepted [0.0; 1.0]

Groups *Mixed-integer optimization*

`MSK_DPAR_MIO_TOL_REL_GAP`
Relative optimality tolerance employed by the mixed-integer optimizer.

Default 1.0e-4

Accepted [0.0; +inf]

Groups *Mixed-integer optimization*, *Termination criteria*

`MSK_DPAR_OPTIMIZER_MAX_TIME`
Maximum amount of time the optimizer is allowed to spent on the optimization. A negative number means infinity.

Default -1.0

Accepted [-inf; +inf]

Groups *Termination criteria*

`MSK_DPAR_PRESOLVE_TOL_ABS_LINDEP`
Absolute tolerance employed by the linear dependency checker.

Default 1.0e-6

Accepted [0.0; +inf]

Groups *Presolve*

`MSK_DPAR_PRESOLVE_TOL_AIJ`
Absolute zero tolerance employed for a_{ij} in the presolve.

Default 1.0e-12

Accepted [1.0e-15; +inf]

Groups *Presolve*

`MSK_DPAR_PRESOLVE_TOL_REL_LINDEP`
Relative tolerance employed by the linear dependency checker.

Default 1.0e-10

Accepted [0.0; +inf]

Groups *Presolve*

`MSK_DPAR_PRESOLVE_TOL_S`
Absolute zero tolerance employed for s_i in the presolve.

Default 1.0e-8

Accepted [0.0; +inf]

Groups *Presolve*

`MSK_DPAR_PRESOLVE_TOL_X`
Absolute zero tolerance employed for x_j in the presolve.

Default 1.0e-8

Accepted [0.0; +inf]

Groups *Presolve*

`MSK_DPAR_QCQO_REFORMULATE_REL_DROP_TOL`
This parameter determines when columns are dropped in incomplete Cholesky factorization during reformulation of quadratic problems.

Default 1e-15

Accepted [0; +inf]

Groups *Interior-point method*

`MSK_DPAR_SEMIDEFINITE_TOL_APPROX`
Tolerance to define a matrix to be positive semidefinite.

Default 1.0e-10

Accepted [1.0e-15; +inf]

Groups *Data check*

MSK_DPAR_SIM_LU_TOL_REL_PIV
Relative pivot tolerance employed when computing the LU factorization of the basis in the simplex optimizers and in the basis identification procedure.

A value closer to 1.0 generally improves numerical stability but typically also implies an increase in the computational work.

Default 0.01

Accepted [1.0e-6; 0.999999]

Groups *Basis identification*, *Simplex optimizer*

MSK_DPAR_SIMPLEX_ABS_TOL_PIV
Absolute pivot tolerance employed by the simplex optimizers.

Default 1.0e-7

Accepted [1.0e-12; +inf]

Groups *Simplex optimizer*

MSK_DPAR_UPPER_OBJ_CUT
If either a primal or dual feasible solution is found proving that the optimal objective value is outside, the interval [*MSK_DPAR_LOWER_OBJ_CUT*, *MSK_DPAR_UPPER_OBJ_CUT*], then **MOSEK** is terminated.

Default 1.0e30

Accepted [-inf; +inf]

Groups *Termination criteria*

See also *MSK_DPAR_UPPER_OBJ_CUT_FINITE_TRH*

MSK_DPAR_UPPER_OBJ_CUT_FINITE_TRH
If the upper objective cut is greater than the value of this parameter, then the upper objective cut *MSK_DPAR_UPPER_OBJ_CUT* is treated as ∞.

Default 0.5e30

Accepted [-inf; +inf]

Groups *Termination criteria*

13.2.2 Integer parameters

MSK_IPAR_ANA_SOL_BASIS
Controls whether the basis matrix is analyzed in solution analyzer.

Default *ON*

Accepted *ON*, *OFF*

Groups *Analysis*

MSK_IPAR_ANA_SOL_PRINT_VIOLATED
Controls whether a list of violated constraints is printed.

All constraints violated by more than the value set by the parameter *MSK_DPAR_ANA_SOL_INFEAS_TOL* will be printed.

Default *OFF*

Accepted *ON*, *OFF*

Groups *Analysis*

`MSK_IPAR_AUTO_SORT_A_BEFORE_OPT`
Controls whether the elements in each column of A are sorted before an optimization is performed. This is not required but makes the optimization more deterministic.

Default *OFF*

Accepted *ON*, *OFF*

Groups *Debugging*

`MSK_IPAR_AUTO_UPDATE_SOL_INFO`
Controls whether the solution information items are automatically updated after an optimization is performed.

Default *OFF*

Accepted *ON*, *OFF*

Groups *Overall system*

`MSK_IPAR_BASIS_SOLVE_USE_PLUS_ONE`
If a slack variable is in the basis, then the corresponding column in the basis is a unit vector with -1 in the right position. However, if this parameter is set to *MSK_ON*, -1 is replaced by 1.

Default *OFF*

Accepted *ON*, *OFF*

Groups *Simplex optimizer*

`MSK_IPAR_BI_CLEAN_OPTIMIZER`
Controls which simplex optimizer is used in the clean-up phase.

Default *FREE*

Accepted *FREE*, *INTPNT*, *CONIC*, *PRIMAL_SIMPLEX*, *DUAL_SIMPLEX*, *FREE_SIMPLEX*, *MIXED_INT*

Groups *Basis identification*, *Overall solver*

`MSK_IPAR_BI_IGNORE_MAX_ITER`
If the parameter *MSK_IPAR_INTPNT_BASIS* has the value *MSK_BI_NO_ERROR* and the interior-point optimizer has terminated due to maximum number of iterations, then basis identification is performed if this parameter has the value *MSK_ON*.

Default *OFF*

Accepted *ON*, *OFF*

Groups *Interior-point method*, *Basis identification*

`MSK_IPAR_BI_IGNORE_NUM_ERROR`
If the parameter *MSK_IPAR_INTPNT_BASIS* has the value *MSK_BI_NO_ERROR* and the interior-point optimizer has terminated due to a numerical problem, then basis identification is performed if this parameter has the value *MSK_ON*.

Default *OFF*

Accepted *ON*, *OFF*

Groups *Interior-point method*, *Basis identification*

`MSK_IPAR_BI_MAX_ITERATIONS`
Controls the maximum number of simplex iterations allowed to optimize a basis after the basis identification.

Default 1000000

Accepted [0; +inf]

Groups *Basis identification*, *Termination criteria*

`MSK_IPAR_CACHE_LICENSE`
Specifies if the license is kept checked out for the lifetime of the mosek environment (*MSK_ON*) or returned to the server immediately after the optimization (*MSK_OFF*).

By default the license is checked out for the lifetime of the **MOSEK** environment by the first call to the optimizer.

Check-in and check-out of licenses have an overhead. Frequent communication with the license server should be avoided.

Default *ON*

Accepted *ON*, *OFF*

Groups *License manager*

`MSK_IPAR_CHECK_CONVEXITY`
Specify the level of convexity check on quadratic problems.

Default *FULL*

Accepted *NONE*, *SIMPLE*, *FULL*

Groups *Data check*, *Nonlinear convex method*

`MSK_IPAR_COMPRESS_STATFILE`
Control compression of stat files.

Default *ON*

Accepted *ON*, *OFF*

`MSK_IPAR_INFEAS_GENERIC_NAMES`
Controls whether generic names are used when an infeasible subproblem is created.

Default *OFF*

Accepted *ON*, *OFF*

Groups *Infeasibility report*

`MSK_IPAR_INFEAS_PREFER_PRIMAL`
If both certificates of primal and dual infeasibility are supplied then only the primal is used when this option is turned on.

Default *ON*

Accepted *ON*, *OFF*

Groups *Overall solver*

`MSK_IPAR_INFEAS_REPORT_AUTO`
Controls whether an infeasibility report is automatically produced after the optimization if the problem is primal or dual infeasible.

Default *OFF*

Accepted *ON*, *OFF*

Groups *Data input/output*, *Solution input/output*

`MSK_IPAR_INFEAS_REPORT_LEVEL`
Controls the amount of information presented in an infeasibility report. Higher values imply more information.

Default 1

Accepted [0; +inf]

Groups *Infeasibility report*, *Output information*

`MSK_IPAR_INTPNT_BASIS`
Controls whether the interior-point optimizer also computes an optimal basis.

Default *ALWAYS*

Accepted *NEVER*, *ALWAYS*, *NO_ERROR*, *IF_FEASIBLE*, *RESERVERED*

Groups *Interior-point method*, *Basis identification*

See also *MSK_IPAR_BI_IGNORE_MAX_ITER*, *MSK_IPAR_BI_IGNORE_NUM_ERROR*, *MSK_IPAR_BI_MAX_ITERATIONS*, *MSK_IPAR_BI_CLEAN_OPTIMIZER*

`MSK_IPAR_INTPNT_DIFF_STEP`
Controls whether different step sizes are allowed in the primal and dual space.

Default *ON*

Accepted

- *ON*: Different step sizes are allowed.
- *OFF*: Different step sizes are not allowed.

Groups *Interior-point method*

`MSK_IPAR_INTPNT_HOTSTART`
Currently not in use.

Default *NONE*

Accepted *NONE*, *PRIMAL*, *DUAL*, *PRIMAL_DUAL*

Groups *Interior-point method*

`MSK_IPAR_INTPNT_MAX_ITERATIONS`
Controls the maximum number of iterations allowed in the interior-point optimizer.

Default 400

Accepted [0; +inf]

Groups *Interior-point method*, *Termination criteria*

`MSK_IPAR_INTPNT_MAX_NUM_COR`
Controls the maximum number of correctors allowed by the multiple corrector procedure. A negative value means that **MOSEK** is making the choice.

Default -1

Accepted [-1; +inf]

Groups *Interior-point method*

`MSK_IPAR_INTPNT_MAX_NUM_REFINEMENT_STEPS`
Maximum number of steps to be used by the iterative refinement of the search direction. A negative value implies that the optimizer chooses the maximum number of iterative refinement steps.

Default -1

Accepted [-inf; +inf]

Groups *Interior-point method*

`MSK_IPAR_INTPNT_MULTI_THREAD`
Controls whether the interior-point optimizers are allowed to employ multiple threads if more threads is available.

Default *ON*

Accepted *ON*, *OFF*

Groups *Overall system*

MSK_IPAR_INTPNT_OFF_COL_TRH
Controls how many offending columns are detected in the Jacobian of the constraint matrix.

0	no detection
1	aggressive detection
> 1	higher values mean less aggressive detection

Default 40

Accepted [0; +inf]

Groups *Interior-point method*

MSK_IPAR_INTPNT_ORDER_METHOD
Controls the ordering strategy used by the interior-point optimizer when factorizing the Newton equation system.

Default *FREE*

Accepted *FREE*, *APPMINLOC*, *EXPERIMENTAL*, *TRY_GRAPHPAR*, *FORCE_GRAPHPAR*, *NONE*

Groups *Interior-point method*

MSK_IPAR_INTPNT_REGULARIZATION_USE
Controls whether regularization is allowed.

Default *ON*

Accepted *ON*, *OFF*

Groups *Interior-point method*

MSK_IPAR_INTPNT_SCALING
Controls how the problem is scaled before the interior-point optimizer is used.

Default *FREE*

Accepted *FREE*, *NONE*, *MODERATE*, *AGGRESSIVE*

Groups *Interior-point method*

MSK_IPAR_INTPNT_SOLVE_FORM
Controls whether the primal or the dual problem is solved.

Default *FREE*

Accepted *FREE*, *PRIMAL*, *DUAL*

Groups *Interior-point method*

MSK_IPAR_INTPNT_STARTING_POINT
Starting point used by the interior-point optimizer.

Default *FREE*

Accepted *FREE*, *GUESS*, *CONSTANT*, *SATISFY_BOUNDS*

Groups *Interior-point method*

MSK_IPAR_LICENSE_DEBUG
This option is used to turn on debugging of the license manager.

Default *OFF*

Accepted *ON*, *OFF*

Groups *License manager*

MSK_IPAR_LICENSE_PAUSE_TIME
If *MSK_IPAR_LICENSE_WAIT* = *MSK_ON* and no license is available, then **MOSEK** sleeps a number of milliseconds between each check of whether a license has become free.

Default 100

Accepted [0; 1000000]

Groups *License manager*

`MSK_IPAR_LICENSE_SUPPRESS_EXPIRE_WRNS`
Controls whether license features expire warnings are suppressed.

Default *OFF*

Accepted *ON*, *OFF*

Groups *License manager*, *Output information*

`MSK_IPAR_LICENSE_TRH_EXPIRY_WRN`
If a license feature expires in a numbers days less than the value of this parameter then a warning will be issued.

Default 7

Accepted [0; +inf]

Groups *License manager*, *Output information*

`MSK_IPAR_LICENSE_WAIT`
If all licenses are in use **MOSEK** returns with an error code. However, by turning on this parameter **MOSEK** will wait for an available license.

Default *OFF*

Accepted *ON*, *OFF*

Groups *Overall solver*, *Overall system*, *License manager*

`MSK_IPAR_LOG`
Controls the amount of log information. The value 0 implies that all log information is suppressed. A higher level implies that more information is logged.

Please note that if a task is employed to solve a sequence of optimization problems the value of this parameter is reduced by the value of *MSK_IPAR_LOG_CUT_SECOND_OPT* for the second and any subsequent optimizations.

Default 10

Accepted [0; +inf]

Groups *Output information*, *Logging*

See also *MSK_IPAR_LOG_CUT_SECOND_OPT*

`MSK_IPAR_LOG_ANA_PRO`
Controls amount of output from the problem analyzer.

Default 1

Accepted [0; +inf]

Groups *Analysis*, *Logging*

`MSK_IPAR_LOG_BI`
Controls the amount of output printed by the basis identification procedure. A higher level implies that more information is logged.

Default 1

Accepted [0; +inf]

Groups *Basis identification*, *Output information*, *Logging*

`MSK_IPAR_LOG_BI_FREQ`
Controls how frequent the optimizer outputs information about the basis identification and how frequent the user-defined callback function is called.

Default 2500

Accepted [0; +inf]

Groups *Basis identification*, *Output information*, *Logging*

`MSK_IPAR_LOG_CHECK_CONVEXITY`
Controls logging in convexity check on quadratic problems. Set to a positive value to turn logging on. If a quadratic coefficient matrix is found to violate the requirement of PSD (NSD) then a list of negative (positive) pivot elements is printed. The absolute value of the pivot elements is also shown.

Default 0

Accepted [0; +inf]

Groups *Data check*, *Nonlinear convex method*

`MSK_IPAR_LOG_CUT_SECOND_OPT`
If a task is employed to solve a sequence of optimization problems, then the value of the log levels is reduced by the value of this parameter. E.g *MSK_IPAR_LOG* and *MSK_IPAR_LOG_SIM* are reduced by the value of this parameter for the second and any subsequent optimizations.

Default 1

Accepted [0; +inf]

Groups *Output information*, *Logging*

See also *MSK_IPAR_LOG*, *MSK_IPAR_LOG_INTPNT*, *MSK_IPAR_LOG_MIO*, *MSK_IPAR_LOG_SIM*

`MSK_IPAR_LOG_EXPAND`
Controls the amount of logging when a data item such as the maximum number constrains is expanded.

Default 0

Accepted [0; +inf]

Groups *Output information*, *Logging*

`MSK_IPAR_LOG_FEAS_REPAIR`
Controls the amount of output printed when performing feasibility repair. A value higher than one means extensive logging.

Default 1

Accepted [0; +inf]

Groups *Output information*, *Logging*

`MSK_IPAR_LOG_FILE`
If turned on, then some log info is printed when a file is written or read.

Default 1

Accepted [0; +inf]

Groups *Data input/output*, *Output information*, *Logging*

`MSK_IPAR_LOG_INFEAS_ANA`
Controls amount of output printed by the infeasibility analyzer procedures. A higher level implies that more information is logged.

Default 1

Accepted [0; +inf]

Groups *Infeasibility report*, *Output information*, *Logging*

`MSK_IPAR_LOG_INTPNT`
Controls amount of output printed by the interior-point optimizer. A higher level implies that more information is logged.

Default 1

Accepted [0; +inf]

Groups *Interior-point method*, *Output information*, *Logging*

`MSK_IPAR_LOG_MIO`
Controls the log level for the mixed-integer optimizer. A higher level implies that more information is logged.

Default 4

Accepted [0; +inf]

Groups *Mixed-integer optimization*, *Output information*, *Logging*

`MSK_IPAR_LOG_MIO_FREQ`
Controls how frequent the mixed-integer optimizer prints the log line. It will print line every time *MSK_IPAR_LOG_MIO_FREQ* relaxations have been solved.

Default 10

Accepted [-inf; +inf]

Groups *Mixed-integer optimization*, *Output information*, *Logging*

`MSK_IPAR_LOG_ORDER`
If turned on, then factor lines are added to the log.

Default 1

Accepted [0; +inf]

Groups *Output information*, *Logging*

`MSK_IPAR_LOG_PRESOLVE`
Controls amount of output printed by the presolve procedure. A higher level implies that more information is logged.

Default 1

Accepted [0; +inf]

Groups *Logging*

`MSK_IPAR_LOG_RESPONSE`
Controls amount of output printed when response codes are reported. A higher level implies that more information is logged.

Default 0

Accepted [0; +inf]

Groups *Output information*, *Logging*

`MSK_IPAR_LOG_SENSITIVITY`
Controls the amount of logging during the sensitivity analysis.

0. Means no logging information is produced.
1. Timing information is printed.
2. Sensitivity results are printed.

Default 1

Accepted [0; +inf]

Groups *Output information*, *Logging*

`MSK_IPAR_LOG_SENSITIVITY_OPT`
Controls the amount of logging from the optimizers employed during the sensitivity analysis. 0 means no logging information is produced.

Default 0

Accepted [0; +inf]

Groups *Output information*, *Logging*

`MSK_IPAR_LOG_SIM`
Controls amount of output printed by the simplex optimizer. A higher level implies that more information is logged.

Default 4

Accepted [0; +inf]

Groups *Simplex optimizer*, *Output information*, *Logging*

`MSK_IPAR_LOG_SIM_FREQ`
Controls how frequent the simplex optimizer outputs information about the optimization and how frequent the user-defined callback function is called.

Default 1000

Accepted [0; +inf]

Groups *Simplex optimizer*, *Output information*, *Logging*

`MSK_IPAR_LOG_SIM_MINOR`
Currently not in use.

Default 1

Accepted [0; +inf]

Groups *Simplex optimizer*, *Output information*

`MSK_IPAR_LOG_STORAGE`
When turned on, **MOSEK** prints messages regarding the storage usage and allocation.

Default 0

Accepted [0; +inf]

Groups *Output information*, *Overall system*, *Logging*

`MSK_IPAR_MAX_NUM_WARNINGS`
Each warning is shown a limit number times controlled by this parameter. A negative value is identical to infinite number of times.

Default 10

Accepted [-inf; +inf]

Groups *Output information*

`MSK_IPAR_MIO_BRANCH_DIR`
Controls whether the mixed-integer optimizer is branching up or down by default.

Default *FREE*

Accepted *FREE*, *UP*, *DOWN*, *NEAR*, *FAR*, *ROOT_LP*, *GUIDED*, *PSEUDOCOST*

Groups *Mixed-integer optimization*

`MSK_IPAR_MIO_CONSTRUCT_SOL`
If set to *MSK_ON* and all integer variables have been given a value for which a feasible mixed integer solution exists, then **MOSEK** generates an initial solution to the mixed integer problem by fixing all integer values and solving the remaining problem.

Default *OFF*

Accepted *ON*, *OFF*

Groups *Mixed-integer optimization*

`MSK_IPAR_MIO_CUT_CLIQUE`
Controls whether clique cuts should be generated.

Default *ON*

Accepted

- *ON*: Turns generation of this cut class on.
- *OFF*: Turns generation of this cut class off.

Groups *Mixed-integer optimization*

`MSK_IPAR_MIO_CUT_CMIR`
Controls whether mixed integer rounding cuts should be generated.

Default *ON*

Accepted

- *ON*: Turns generation of this cut class on.
- *OFF*: Turns generation of this cut class off.

Groups *Mixed-integer optimization*

`MSK_IPAR_MIO_CUT_GMI`
Controls whether GMI cuts should be generated.

Default *ON*

Accepted

- *ON*: Turns generation of this cut class on.
- *OFF*: Turns generation of this cut class off.

Groups *Mixed-integer optimization*

`MSK_IPAR_MIO_CUT_IMPLIED_BOUND`
Controls whether implied bound cuts should be generated.

Default *OFF*

Accepted

- *ON*: Turns generation of this cut class on.
- *OFF*: Turns generation of this cut class off.

Groups *Mixed-integer optimization*

`MSK_IPAR_MIO_CUT_KNAPSACK_COVER`
Controls whether knapsack cover cuts should be generated.

Default *OFF*

Accepted

- *ON*: Turns generation of this cut class on.
- *OFF*: Turns generation of this cut class off.

Groups *Mixed-integer optimization*

`MSK_IPAR_MIO_CUT_SELECTION_LEVEL`
Controls how aggressively generated cuts are selected to be included in the relaxation.

-1. The optimizer chooses the level of cut selection

0.Generated cuts less likely to be added to the relaxation

1.Cuts are more aggressively selected to be included in the relaxation

Default -1

Accepted [-1; +1]

Groups *Mixed-integer optimization*

`MSK_IPAR_MIO_HEURISTIC_LEVEL`
Controls the heuristic employed by the mixed-integer optimizer to locate an initial good integer feasible solution. A value of zero means the heuristic is not used at all. A larger value than 0 means that a gradually more sophisticated heuristic is used which is computationally more expensive. A negative value implies that the optimizer chooses the heuristic. Normally a value around 3 to 5 should be optimal.

Default -1

Accepted [-inf; +inf]

Groups *Mixed-integer optimization*

`MSK_IPAR_MIO_MAX_NUM_BRANCHES`
Maximum number of branches allowed during the branch and bound search. A negative value means infinite.

Default -1

Accepted [-inf; +inf]

Groups *Mixed-integer optimization*, *Termination criteria*

See also *MSK_DPAR_MIO_DISABLE_TERM_TIME*

`MSK_IPAR_MIO_MAX_NUM_RELAXS`
Maximum number of relaxations allowed during the branch and bound search. A negative value means infinite.

Default -1

Accepted [-inf; +inf]

Groups *Mixed-integer optimization*

See also *MSK_DPAR_MIO_DISABLE_TERM_TIME*

`MSK_IPAR_MIO_MAX_NUM_SOLUTIONS`
The mixed-integer optimizer can be terminated after a certain number of different feasible solutions has been located. If this parameter has the value $n > 0$, then the mixed-integer optimizer will be terminated when n feasible solutions have been located.

Default -1

Accepted [-inf; +inf]

Groups *Mixed-integer optimization*, *Termination criteria*

See also *MSK_DPAR_MIO_DISABLE_TERM_TIME*

`MSK_IPAR_MIO_MODE`
Controls whether the optimizer includes the integer restrictions when solving a (mixed) integer optimization problem.

Default *SATISFIED*

Accepted *IGNORED*, *SATISFIED*

Groups *Overall solver*

`MSK_IPAR_MIO_MT_USER_CB`
If true user callbacks are called from each thread used by mixed-integer optimizer. Otherwise it is only called from a single thread.

Default *OFF*

Accepted *ON*, *OFF*

Groups *Overall system*

MSK_IPAR_MIO_NODE_OPTIMIZER
Controls which optimizer is employed at the non-root nodes in the mixed-integer optimizer.

Default *FREE*

Accepted *FREE*, *INTPNT*, *CONIC*, *PRIMAL_SIMPLEX*, *DUAL_SIMPLEX*, *FREE_SIMPLEX*, *MIXED_INT*

Groups *Mixed-integer optimization*

MSK_IPAR_MIO_NODE_SELECTION
Controls the node selection strategy employed by the mixed-integer optimizer.

Default *FREE*

Accepted *FREE*, *FIRST*, *BEST*, *WORST*, *HYBRID*, *PSEUDO*

Groups *Mixed-integer optimization*

MSK_IPAR_MIO_PERSPECTIVE_REFORMULATE
Enables or disables perspective reformulation in presolve.

Default *ON*

Accepted *ON*, *OFF*

Groups *Mixed-integer optimization*

MSK_IPAR_MIO_PROBING_LEVEL
Controls the amount of probing employed by the mixed-integer optimizer in presolve.

-1. The optimizer chooses the level of probing employed

0.Probing is disabled

1.A low amount of probing is employed

2.A medium amount of probing is employed

3.A high amount of probing is employed

Default -1

Accepted [-1; 3]

Groups *Mixed-integer optimization*

MSK_IPAR_MIO_RINS_MAX_NODES
Controls the maximum number of nodes allowed in each call to the RINS heuristic. The default value of -1 means that the value is determined automatically. A value of zero turns off the heuristic.

Default -1

Accepted [-1; +inf]

Groups *Mixed-integer optimization*

MSK_IPAR_MIO_ROOT_OPTIMIZER
Controls which optimizer is employed at the root node in the mixed-integer optimizer.

Default *FREE*

Accepted *FREE*, *INTPNT*, *CONIC*, *PRIMAL_SIMPLEX*, *DUAL_SIMPLEX*, *FREE_SIMPLEX*, *MIXED_INT*

Groups *Mixed-integer optimization*

`MSK_IPAR_MIO_ROOT_REPEAT_PRESOLVE_LEVEL`
Controls whether presolve can be repeated at root node.

- -1 The optimizer chooses whether presolve is repeated
- 0 Never repeat presolve
- 1 Always repeat presolve

Default -1

Accepted [-1; 1]

Groups *Mixed-integer optimization*

`MSK_IPAR_MIO_VB_DETECTION_LEVEL`
Controls how much effort is put into detecting variable bounds.

-1. The optimizer chooses

0.No variable bounds are detected

1.Only detect variable bounds that are directly represented in the problem

2.Detect variable bounds in probing

Default -1

Accepted [-1; +2]

Groups *Mixed-integer optimization*

`MSK_IPAR_MT_SPINCOUNT`
Set the number of iterations to spin before sleeping.

Default 0

Accepted [0; 1000000000]

Groups *Overall system*

`MSK_IPAR_NUM_THREADS`
Controls the number of threads employed by the optimizer. If set to 0 the number of threads used will be equal to the number of cores detected on the machine.

Default 0

Accepted [0; +inf]

Groups *Overall system*

`MSK_IPAR_OPF_MAX_TERMS_PER_LINE`
The maximum number of terms (linear and quadratic) per line when an OPF file is written.

Default 5

Accepted [0; +inf]

Groups *Data input/output*

`MSK_IPAR_OPF_WRITE_HEADER`
Write a text header with date and **MOSEK** version in an OPF file.

Default *ON*

Accepted *ON*, *OFF*

Groups *Data input/output*

`MSK_IPAR_OPF_WRITE_HINTS`
Write a hint section with problem dimensions in the beginning of an OPF file.

Default *ON*

Accepted *ON*, *OFF*

Groups *Data input/output*

MSK_IPAR_OPF_WRITE_PARAMETERS
Write a parameter section in an OPF file.

Default *OFF*

Accepted *ON*, *OFF*

Groups *Data input/output*

MSK_IPAR_OPF_WRITE_PROBLEM
Write objective, constraints, bounds etc. to an OPF file.

Default *ON*

Accepted *ON*, *OFF*

Groups *Data input/output*

MSK_IPAR_OPF_WRITE_SOL_BAS
If *MSK_IPAR_OPF_WRITE_SOLUTIONS* is *MSK_ON* and a basic solution is defined, include the basic solution in OPF files.

Default *ON*

Accepted *ON*, *OFF*

Groups *Data input/output*

MSK_IPAR_OPF_WRITE_SOL_ITG
If *MSK_IPAR_OPF_WRITE_SOLUTIONS* is *MSK_ON* and an integer solution is defined, write the integer solution in OPF files.

Default *ON*

Accepted *ON*, *OFF*

Groups *Data input/output*

MSK_IPAR_OPF_WRITE_SOL_ITR
If *MSK_IPAR_OPF_WRITE_SOLUTIONS* is *MSK_ON* and an interior solution is defined, write the interior solution in OPF files.

Default *ON*

Accepted *ON*, *OFF*

Groups *Data input/output*

MSK_IPAR_OPF_WRITE_SOLUTIONS
Enable inclusion of solutions in the OPF files.

Default *OFF*

Accepted *ON*, *OFF*

Groups *Data input/output*

MSK_IPAR_OPTIMIZER
The parameter controls which optimizer is used to optimize the task.

Default *FREE*

Accepted *FREE*, *INTPNT*, *CONIC*, *PRIMAL_SIMPLEX*, *DUAL_SIMPLEX*, *FREE_SIMPLEX*, *MIXED_INT*

Groups *Overall solver*

`MSK_IPAR_PARAM_READ_CASE_NAME`
If turned on, then names in the parameter file are case sensitive.

Default *ON*

Accepted *ON*, *OFF*

Groups *Data input/output*

`MSK_IPAR_PARAM_READ_IGN_ERROR`
If turned on, then errors in parameter settings is ignored.

Default *OFF*

Accepted *ON*, *OFF*

Groups *Data input/output*

`MSK_IPAR_PRESOLVE_ELIMINATOR_MAX_FILL`
Controls the maximum amount of fill-in that can be created by one pivot in the elimination phase of the presolve. A negative value means the parameter value is selected automatically.

Default -1

Accepted [-inf; +inf]

Groups *Presolve*

`MSK_IPAR_PRESOLVE_ELIMINATOR_MAX_NUM_TRIES`
Control the maximum number of times the eliminator is tried. A negative value implies **MOSEK** decides.

Default -1

Accepted [-inf; +inf]

Groups *Presolve*

`MSK_IPAR_PRESOLVE_LEVEL`
Currently not used.

Default -1

Accepted [-inf; +inf]

Groups *Overall solver*, *Presolve*

`MSK_IPAR_PRESOLVE_LINDEP_ABS_WORK_TRH`
The linear dependency check is potentially computationally expensive.

Default 100

Accepted [-inf; +inf]

Groups *Presolve*

`MSK_IPAR_PRESOLVE_LINDEP_REL_WORK_TRH`
The linear dependency check is potentially computationally expensive.

Default 100

Accepted [-inf; +inf]

Groups *Presolve*

`MSK_IPAR_PRESOLVE_LINDEP_USE`
Controls whether the linear constraints are checked for linear dependencies.

Default *ON*

Accepted

- *ON*: Turns the linear dependency check on.

- *OFF*: Turns the linear dependency check off.

Groups *Presolve*

MSK_IPAR_PRESOLVE_MAX_NUM_REDUCTIONS
Controls the maximum number of reductions performed by the presolve. The value of the parameter is normally only changed in connection with debugging. A negative value implies that an infinite number of reductions are allowed.

Default -1

Accepted [-inf; +inf]

Groups *Overall solver*, *Presolve*

MSK_IPAR_PRESOLVE_USE
Controls whether the presolve is applied to a problem before it is optimized.

Default *FREE*

Accepted *OFF*, *ON*, *FREE*

Groups *Overall solver*, *Presolve*

MSK_IPAR_PRIMAL_REPAIR_OPTIMIZER
Controls which optimizer that is used to find the optimal repair.

Default *FREE*

Accepted *FREE*, *INTPNT*, *CONIC*, *PRIMAL_SIMPLEX*, *DUAL_SIMPLEX*, *FREE_SIMPLEX*, *MIXED_INT*

Groups *Overall solver*

MSK_IPAR_READ_DATA_COMPRESSED
If this option is turned on,it is assumed that the data file is compressed.

Default *FREE*

Accepted *NONE*, *FREE*, *GZIP*

Groups *Data input/output*

MSK_IPAR_READ_DATA_FORMAT
Format of the data file to be read.

Default *EXTENSION*

Accepted *EXTENSION*, *MPS*, *LP*, *OP*, *XML*, *FREE_MPS*, *TASK*, *CB*, *JSON_TASK*

Groups *Data input/output*

MSK_IPAR_READ_DEBUG
Turns on additional debugging information when reading files.

Default *OFF*

Accepted *ON*, *OFF*

Groups *Data input/output*

MSK_IPAR_READ_KEEP_FREE_CON
Controls whether the free constraints are included in the problem.

Default *OFF*

Accepted

- *ON*: The free constraints are kept.
- *OFF*: The free constraints are discarded.

Groups *Data input/output*

MSK_IPAR_READ_LP_DROP_NEW_VARS_IN_BOU
: If this option is turned on, **MOSEK** will drop variables that are defined for the first time in the bounds section.

  Default *OFF*

  Accepted *ON*, *OFF*

  Groups *Data input/output*

MSK_IPAR_READ_LP_QUOTED_NAMES
: If a name is in quotes when reading an LP file, the quotes will be removed.

  Default *ON*

  Accepted *ON*, *OFF*

  Groups *Data input/output*

MSK_IPAR_READ_MPS_FORMAT
: Controls how strictly the MPS file reader interprets the MPS format.

  Default *FREE*

  Accepted *STRICT*, *RELAXED*, *FREE*, *CPLEX*

  Groups *Data input/output*

MSK_IPAR_READ_MPS_WIDTH
: Controls the maximal number of characters allowed in one line of the MPS file.

  Default 1024

  Accepted [80; +inf]

  Groups *Data input/output*

MSK_IPAR_READ_TASK_IGNORE_PARAM
: Controls whether **MOSEK** should ignore the parameter setting defined in the task file and use the default parameter setting instead.

  Default *OFF*

  Accepted *ON*, *OFF*

  Groups *Data input/output*

MSK_IPAR_REMOVE_UNUSED_SOLUTIONS
: Removes unsued solutions before the optimization is performed.

  Default *OFF*

  Accepted *ON*, *OFF*

  Groups *Overall system*

MSK_IPAR_SENSITIVITY_ALL
: Not applicable.

  Default *OFF*

  Accepted *ON*, *OFF*

  Groups *Overall solver*

MSK_IPAR_SENSITIVITY_OPTIMIZER
: Controls which optimizer is used for optimal partition sensitivity analysis.

  Default *FREE_SIMPLEX*

  Accepted *FREE*, *INTPNT*, *CONIC*, *PRIMAL_SIMPLEX*, *DUAL_SIMPLEX*, *FREE_SIMPLEX*, *MIXED_INT*

  Groups *Overall solver*, *Simplex optimizer*

MSK_IPAR_SENSITIVITY_TYPE
Controls which type of sensitivity analysis is to be performed.

Default *BASIS*

Accepted *BASIS*, *OPTIMAL_PARTITION*

Groups *Overall solver*

MSK_IPAR_SIM_BASIS_FACTOR_USE
Controls whether an LU factorization of the basis is used in a hot-start. Forcing a refactorization sometimes improves the stability of the simplex optimizers, but in most cases there is a performance penalty.

Default *ON*

Accepted *ON*, *OFF*

Groups *Simplex optimizer*

MSK_IPAR_SIM_DEGEN
Controls how aggressively degeneration is handled.

Default *FREE*

Accepted *NONE*, *FREE*, *AGGRESSIVE*, *MODERATE*, *MINIMUM*

Groups *Simplex optimizer*

MSK_IPAR_SIM_DUAL_CRASH
Controls whether crashing is performed in the dual simplex optimizer.

If this parameter is set to x, then a crash will be performed if a basis consists of more than $(100-x)$ mod f_v entries, where f_v is the number of fixed variables.

Default 90

Accepted [0; +inf]

Groups *Dual simplex*

MSK_IPAR_SIM_DUAL_PHASEONE_METHOD
An experimental feature.

Default 0

Accepted [0; 10]

Groups *Simplex optimizer*

MSK_IPAR_SIM_DUAL_RESTRICT_SELECTION
The dual simplex optimizer can use a so-called restricted selection/pricing strategy to chooses the outgoing variable. Hence, if restricted selection is applied, then the dual simplex optimizer first choose a subset of all the potential outgoing variables. Next, for some time it will choose the outgoing variable only among the subset. From time to time the subset is redefined.

A larger value of this parameter implies that the optimizer will be more aggressive in its restriction strategy, i.e. a value of 0 implies that the restriction strategy is not applied at all.

Default 50

Accepted [0; 100]

Groups *Dual simplex*

MSK_IPAR_SIM_DUAL_SELECTION
Controls the choice of the incoming variable, known as the selection strategy, in the dual simplex optimizer.

Default *FREE*

Accepted *FREE*, *FULL*, *ASE*, *DEVEX*, *SE*, *PARTIAL*

Groups *Dual simplex*

`MSK_IPAR_SIM_EXPLOIT_DUPVEC`
Controls if the simplex optimizers are allowed to exploit duplicated columns.

Default *OFF*

Accepted *ON*, *OFF*, *FREE*

Groups *Simplex optimizer*

`MSK_IPAR_SIM_HOTSTART`
Controls the type of hot-start that the simplex optimizer perform.

Default *FREE*

Accepted *NONE*, *FREE*, *STATUS_KEYS*

Groups *Simplex optimizer*

`MSK_IPAR_SIM_HOTSTART_LU`
Determines if the simplex optimizer should exploit the initial factorization.

Default *ON*

Accepted

- *ON*: Factorization is reused if possible.
- *OFF*: Factorization is recomputed.

Groups *Simplex optimizer*

`MSK_IPAR_SIM_MAX_ITERATIONS`
Maximum number of iterations that can be used by a simplex optimizer.

Default 10000000

Accepted [0; +inf]

Groups *Simplex optimizer*, *Termination criteria*

`MSK_IPAR_SIM_MAX_NUM_SETBACKS`
Controls how many set-backs are allowed within a simplex optimizer. A set-back is an event where the optimizer moves in the wrong direction. This is impossible in theory but may happen due to numerical problems.

Default 250

Accepted [0; +inf]

Groups *Simplex optimizer*

`MSK_IPAR_SIM_NON_SINGULAR`
Controls if the simplex optimizer ensures a non-singular basis, if possible.

Default *ON*

Accepted *ON*, *OFF*

Groups *Simplex optimizer*

`MSK_IPAR_SIM_PRIMAL_CRASH`
Controls whether crashing is performed in the primal simplex optimizer.

In general, if a basis consists of more than (100-this parameter value)% fixed variables, then a crash will be performed.

Default 90

Accepted [0; +inf]

Groups *Primal simplex*

MSK_IPAR_SIM_PRIMAL_PHASEONE_METHOD
An experimental feature.

Default 0

Accepted [0; 10]

Groups *Simplex optimizer*

MSK_IPAR_SIM_PRIMAL_RESTRICT_SELECTION
The primal simplex optimizer can use a so-called restricted selection/pricing strategy to chooses the outgoing variable. Hence, if restricted selection is applied, then the primal simplex optimizer first choose a subset of all the potential incoming variables. Next, for some time it will choose the incoming variable only among the subset. From time to time the subset is redefined.

A larger value of this parameter implies that the optimizer will be more aggressive in its restriction strategy, i.e. a value of 0 implies that the restriction strategy is not applied at all.

Default 50

Accepted [0; 100]

Groups *Primal simplex*

MSK_IPAR_SIM_PRIMAL_SELECTION
Controls the choice of the incoming variable, known as the selection strategy, in the primal simplex optimizer.

Default *FREE*

Accepted *FREE*, *FULL*, *ASE*, *DEVEX*, *SE*, *PARTIAL*

Groups *Primal simplex*

MSK_IPAR_SIM_REFACTOR_FREQ
Controls how frequent the basis is refactorized. The value 0 means that the optimizer determines the best point of refactorization.

It is strongly recommended NOT to change this parameter.

Default 0

Accepted [0; +inf]

Groups *Simplex optimizer*

MSK_IPAR_SIM_REFORMULATION
Controls if the simplex optimizers are allowed to reformulate the problem.

Default *OFF*

Accepted *ON*, *OFF*, *FREE*, *AGGRESSIVE*

Groups *Simplex optimizer*

MSK_IPAR_SIM_SAVE_LU
Controls if the LU factorization stored should be replaced with the LU factorization corresponding to the initial basis.

Default *OFF*

Accepted *ON*, *OFF*

Groups *Simplex optimizer*

MSK_IPAR_SIM_SCALING
Controls how much effort is used in scaling the problem before a simplex optimizer is used.

Default *FREE*

Accepted *FREE*, *NONE*, *MODERATE*, *AGGRESSIVE*

Groups *Simplex optimizer*

MSK_IPAR_SIM_SCALING_METHOD
Controls how the problem is scaled before a simplex optimizer is used.

Default *POW2*

Accepted *POW2*, *FREE*

Groups *Simplex optimizer*

MSK_IPAR_SIM_SOLVE_FORM
Controls whether the primal or the dual problem is solved by the primal-/dual-simplex optimizer.

Default *FREE*

Accepted *FREE*, *PRIMAL*, *DUAL*

Groups *Simplex optimizer*

MSK_IPAR_SIM_STABILITY_PRIORITY
Controls how high priority the numerical stability should be given.

Default 50

Accepted [0; 100]

Groups *Simplex optimizer*

MSK_IPAR_SIM_SWITCH_OPTIMIZER
The simplex optimizer sometimes chooses to solve the dual problem instead of the primal problem. This implies that if you have chosen to use the dual simplex optimizer and the problem is dualized, then it actually makes sense to use the primal simplex optimizer instead. If this parameter is on and the problem is dualized and furthermore the simplex optimizer is chosen to be the primal (dual) one, then it is switched to the dual (primal).

Default *OFF*

Accepted *ON*, *OFF*

Groups *Simplex optimizer*

MSK_IPAR_SOL_FILTER_KEEP_BASIC
If turned on, then basic and super basic constraints and variables are written to the solution file independent of the filter setting.

Default *OFF*

Accepted *ON*, *OFF*

Groups *Solution input/output*

MSK_IPAR_SOL_FILTER_KEEP_RANGED
If turned on, then ranged constraints and variables are written to the solution file independent of the filter setting.

Default *OFF*

Accepted *ON*, *OFF*

Groups *Solution input/output*

MSK_IPAR_SOL_READ_NAME_WIDTH
When a solution is read by **MOSEK** and some constraint, variable or cone names contain blanks, then a maximum name width much be specified. A negative value implies that no name contain blanks.

Default -1

Accepted [-inf; +inf]

Groups *Data input/output*, *Solution input/output*

`MSK_IPAR_SOL_READ_WIDTH`
Controls the maximal acceptable width of line in the solutions when read by **MOSEK**.

Default 1024

Accepted [80; +inf]

Groups *Data input/output*, *Solution input/output*

`MSK_IPAR_SOLUTION_CALLBACK`
Indicates whether solution callbacks will be performed during the optimization.

Default *OFF*

Accepted *ON*, *OFF*

Groups *Progress callback*, *Overall solver*

`MSK_IPAR_TIMING_LEVEL`
Controls the amount of timing performed inside **MOSEK**.

Default 1

Accepted [0; +inf]

Groups *Overall system*

`MSK_IPAR_WRITE_BAS_CONSTRAINTS`
Controls whether the constraint section is written to the basic solution file.

Default *ON*

Accepted *ON*, *OFF*

Groups *Data input/output*, *Solution input/output*

`MSK_IPAR_WRITE_BAS_HEAD`
Controls whether the header section is written to the basic solution file.

Default *ON*

Accepted *ON*, *OFF*

Groups *Data input/output*, *Solution input/output*

`MSK_IPAR_WRITE_BAS_VARIABLES`
Controls whether the variables section is written to the basic solution file.

Default *ON*

Accepted *ON*, *OFF*

Groups *Data input/output*, *Solution input/output*

`MSK_IPAR_WRITE_DATA_COMPRESSED`
Controls whether the data file is compressed while it is written. 0 means no compression while higher values mean more compression.

Default 0

Accepted [0; +inf]

Groups *Data input/output*

`MSK_IPAR_WRITE_DATA_FORMAT`
Controls the file format when writing task data to a file.

Default *EXTENSION*

Accepted *EXTENSION*, *MPS*, *LP*, *OP*, *XML*, *FREE_MPS*, *TASK*, *CB*, *JSON_TASK*

Groups *Data input/output*

`MSK_IPAR_WRITE_DATA_PARAM`
If this option is turned on the parameter settings are written to the data file as parameters.

Default *OFF*

Accepted *ON*, *OFF*

Groups *Data input/output*

`MSK_IPAR_WRITE_FREE_CON`
Controls whether the free constraints are written to the data file.

Default *ON*

Accepted

- *ON*: The free constraints are written.
- *OFF*: The free constraints are discarded.

Groups *Data input/output*

`MSK_IPAR_WRITE_GENERIC_NAMES`
Controls whether the generic names or user-defined names are used in the data file.

Default *OFF*

Accepted

- *ON*: Generic names are used.
- *OFF*: Generic names are not used.

Groups *Data input/output*

`MSK_IPAR_WRITE_GENERIC_NAMES_IO`
Index origin used in generic names.

Default 1

Accepted [0; +inf]

Groups *Data input/output*

`MSK_IPAR_WRITE_IGNORE_INCOMPATIBLE_ITEMS`
Controls if the writer ignores incompatible problem items when writing files.

Default *OFF*

Accepted

- *ON*: Ignore items that cannot be written to the current output file format.
- *OFF*: Produce an error if the problem contains items that cannot the written to the current output file format.

Groups *Data input/output*

`MSK_IPAR_WRITE_INT_CONSTRAINTS`
Controls whether the constraint section is written to the integer solution file.

Default *ON*

Accepted *ON*, *OFF*

Groups *Data input/output*, *Solution input/output*

`MSK_IPAR_WRITE_INT_HEAD`
Controls whether the header section is written to the integer solution file.

Default *ON*

Accepted *ON*, *OFF*

Groups *Data input/output*, *Solution input/output*

`MSK_IPAR_WRITE_INT_VARIABLES`
Controls whether the variables section is written to the integer solution file.

Default *ON*

Accepted *ON*, *OFF*

Groups *Data input/output*, *Solution input/output*

`MSK_IPAR_WRITE_LP_FULL_OBJ`
Write all variables, including the ones with 0-coefficients, in the objective.

Default *ON*

Accepted *ON*, *OFF*

Groups *Data input/output*

`MSK_IPAR_WRITE_LP_LINE_WIDTH`
Maximum width of line in an LP file written by **MOSEK**.

Default 80

Accepted [40; +inf]

Groups *Data input/output*

`MSK_IPAR_WRITE_LP_QUOTED_NAMES`
If this option is turned on, then **MOSEK** will quote invalid LP names when writing an LP file.

Default *ON*

Accepted *ON*, *OFF*

Groups *Data input/output*

`MSK_IPAR_WRITE_LP_STRICT_FORMAT`
Controls whether LP output files satisfy the LP format strictly.

Default *OFF*

Accepted *ON*, *OFF*

Groups *Data input/output*

`MSK_IPAR_WRITE_LP_TERMS_PER_LINE`
Maximum number of terms on a single line in an LP file written by **MOSEK**. 0 means unlimited.

Default 10

Accepted [0; +inf]

Groups *Data input/output*

`MSK_IPAR_WRITE_MPS_FORMAT`
Controls in which format the MPS is written.

Default *FREE*

Accepted *STRICT*, *RELAXED*, *FREE*, *CPLEX*

Groups *Data input/output*

`MSK_IPAR_WRITE_MPS_INT`
Controls if marker records are written to the MPS file to indicate whether variables are integer restricted.

Default *ON*

Accepted

- *ON*: Marker records are written.
- *OFF*: Marker records are not written.

Groups *Data input/output*

`MSK_IPAR_WRITE_PRECISION`
Controls the precision with which `double` numbers are printed in the MPS data file. In general it is not worthwhile to use a value higher than 15.

Default 15

Accepted [0; +inf]

Groups *Data input/output*

`MSK_IPAR_WRITE_SOL_BARVARIABLES`
Controls whether the symmetric matrix variables section is written to the solution file.

Default *ON*

Accepted *ON*, *OFF*

Groups *Data input/output*, *Solution input/output*

`MSK_IPAR_WRITE_SOL_CONSTRAINTS`
Controls whether the constraint section is written to the solution file.

Default *ON*

Accepted *ON*, *OFF*

Groups *Data input/output*, *Solution input/output*

`MSK_IPAR_WRITE_SOL_HEAD`
Controls whether the header section is written to the solution file.

Default *ON*

Accepted *ON*, *OFF*

Groups *Data input/output*, *Solution input/output*

`MSK_IPAR_WRITE_SOL_IGNORE_INVALID_NAMES`
Even if the names are invalid MPS names, then they are employed when writing the solution file.

Default *OFF*

Accepted *ON*, *OFF*

Groups *Data input/output*, *Solution input/output*

`MSK_IPAR_WRITE_SOL_VARIABLES`
Controls whether the variables section is written to the solution file.

Default *ON*

Accepted *ON*, *OFF*

Groups *Data input/output*, *Solution input/output*

`MSK_IPAR_WRITE_TASK_INC_SOL`
Controls whether the solutions are stored in the task file too.

Default *ON*

Accepted *ON*, *OFF*

Groups *Data input/output*

`MSK_IPAR_WRITE_XML_MODE`
Controls if linear coefficients should be written by row or column when writing in the XML file format.

Default *ROW*

Accepted *ROW*, *COL*

Groups *Data input/output*

13.2.3 String parameters

`MSK_SPAR_BAS_SOL_FILE_NAME`
Name of the `bas` solution file.

Accepted Any valid file name.

Groups *Data input/output*, *Solution input/output*

`MSK_SPAR_DATA_FILE_NAME`
Data are read and written to this file.

Accepted Any valid file name.

Groups *Data input/output*

`MSK_SPAR_DEBUG_FILE_NAME`
MOSEK debug file.

Accepted Any valid file name.

Groups *Data input/output*

`MSK_SPAR_INT_SOL_FILE_NAME`
Name of the `int` solution file.

Accepted Any valid file name.

Groups *Data input/output*, *Solution input/output*

`MSK_SPAR_ITR_SOL_FILE_NAME`
Name of the `itr` solution file.

Accepted Any valid file name.

Groups *Data input/output*, *Solution input/output*

`MSK_SPAR_MIO_DEBUG_STRING`
For internal debugging purposes.

Accepted Any valid string.

Groups *Data input/output*

`MSK_SPAR_PARAM_COMMENT_SIGN`
Only the first character in this string is used. It is considered as a start of comment sign in the **MOSEK** parameter file. Spaces are ignored in the string.

Default

%%

Accepted Any valid string.

Groups *Data input/output*

`MSK_SPAR_PARAM_READ_FILE_NAME`
Modifications to the parameter database is read from this file.

Accepted Any valid file name.

Groups *Data input/output*

`MSK_SPAR_PARAM_WRITE_FILE_NAME`
The parameter database is written to this file.

Accepted Any valid file name.

Groups *Data input/output*

`MSK_SPAR_READ_MPS_BOU_NAME`
Name of the BOUNDS vector used. An empty name means that the first BOUNDS vector is used.

Accepted Any valid MPS name.

Groups *Data input/output*

`MSK_SPAR_READ_MPS_OBJ_NAME`
Name of the free constraint used as objective function. An empty name means that the first constraint is used as objective function.

Accepted Any valid MPS name.

Groups *Data input/output*

`MSK_SPAR_READ_MPS_RAN_NAME`
Name of the RANGE vector used. An empty name means that the first RANGE vector is used.

Accepted Any valid MPS name.

Groups *Data input/output*

`MSK_SPAR_READ_MPS_RHS_NAME`
Name of the RHS used. An empty name means that the first RHS vector is used.

Accepted Any valid MPS name.

Groups *Data input/output*

`MSK_SPAR_REMOTE_ACCESS_TOKEN`
An access token used to submit tasks to a remote **MOSEK** server. An access token is a random 32-byte string encoded in base64, i.e. it is a 44 character ASCII string.

Accepted Any valid string.

Groups *Overall system*

`MSK_SPAR_SENSITIVITY_FILE_NAME`
Not applicable.

Accepted Any valid string.

Groups *Data input/output*

`MSK_SPAR_SENSITIVITY_RES_FILE_NAME`
Not applicable.

Accepted Any valid string.

Groups *Data input/output*

`MSK_SPAR_SOL_FILTER_XC_LOW`
A filter used to determine which constraints should be listed in the solution file. A value of 0.5 means that all constraints having `xc[i]>0.5` should be listed, whereas `+0.5` means that all constraints having `xc[i]>=blc[i]+0.5` should be listed. An empty filter means that no filter is applied.

Accepted Any valid filter.

Groups *Data input/output*, *Solution input/output*

`MSK_SPAR_SOL_FILTER_XC_UPR`
A filter used to determine which constraints should be listed in the solution file. A value of `0.5` means that all constraints having `xc[i]<0.5` should be listed, whereas `-0.5` means all constraints having `xc[i]<=buc[i]-0.5` should be listed. An empty filter means that no filter is applied.

Accepted Any valid filter.

Groups *Data input/output*, *Solution input/output*

`MSK_SPAR_SOL_FILTER_XX_LOW`
A filter used to determine which variables should be listed in the solution file. A value of "0.5" means that all constraints having `xx[j]>=0.5` should be listed, whereas "+0.5" means that all constraints having `xx[j]>=blx[j]+0.5` should be listed. An empty filter means no filter is applied.

Accepted Any valid filter.

Groups *Data input/output*, *Solution input/output*

`MSK_SPAR_SOL_FILTER_XX_UPR`
A filter used to determine which variables should be listed in the solution file. A value of "0.5" means that all constraints having `xx[j]<0.5` should be printed, whereas "-0.5" means all constraints having `xx[j]<=bux[j]-0.5` should be listed. An empty filter means no filter is applied.

Accepted Any valid file name.

Groups *Data input/output*, *Solution input/output*

`MSK_SPAR_STAT_FILE_NAME`
Statistics file name.

Accepted Any valid file name.

Groups *Data input/output*

`MSK_SPAR_STAT_KEY`
Key used when writing the summary file.

Accepted Any valid string.

Groups *Data input/output*

`MSK_SPAR_STAT_NAME`
Name used when writing the statistics file.

Accepted Any valid XML string.

Groups *Data input/output*

`MSK_SPAR_WRITE_LP_GEN_VAR_NAME`
Sometimes when an LP file is written additional variables must be inserted. They will have the prefix denoted by this parameter.

Default xmskgen

Accepted Any valid string.

Groups *Data input/output*

13.3 Response codes

- *Termination*
- *Warnings*
- *Errors*

13.3.1 Termination

`MSK_RES_OK`
No error occurred.

`MSK_RES_TRM_MAX_ITERATIONS`
The optimizer terminated at the maximum number of iterations.

`MSK_RES_TRM_MAX_TIME`
The optimizer terminated at the maximum amount of time.

`MSK_RES_TRM_OBJECTIVE_RANGE`
The optimizer terminated with an objective value outside the objective range.

`MSK_RES_TRM_MIO_NEAR_REL_GAP`
The mixed-integer optimizer terminated as the delayed near optimal relative gap tolerance was satisfied.

`MSK_RES_TRM_MIO_NEAR_ABS_GAP`
The mixed-integer optimizer terminated as the delayed near optimal absolute gap tolerance was satisfied.

`MSK_RES_TRM_MIO_NUM_RELAXS`
The mixed-integer optimizer terminated as the maximum number of relaxations was reached.

`MSK_RES_TRM_MIO_NUM_BRANCHES`
The mixed-integer optimizer terminated as the maximum number of branches was reached.

`MSK_RES_TRM_NUM_MAX_NUM_INT_SOLUTIONS`
The mixed-integer optimizer terminated as the maximum number of feasible solutions was reached.

`MSK_RES_TRM_STALL`
The optimizer is terminated due to slow progress.

Stalling means that numerical problems prevent the optimizer from making reasonable progress and that it make no sense to continue. In many cases this happens if the problem is badly scaled or otherwise ill-conditioned. There is no guarantee that the solution will be (near) feasible or near optimal. However, often stalling happens near the optimum, and the returned solution may be of good quality. Therefore, it is recommended to check the status of then solution. If the solution near optimal the solution is most likely good enough for most practical purposes.

Please note that if a linear optimization problem is solved using the interior-point optimizer with basis identification turned on, the returned basic solution likely to have high accuracy, even though the optimizer stalled.

Some common causes of stalling are a) badly scaled models, b) near feasible or near infeasible problems and c) a non-convex problems. Case c) is only relevant for general non-linear problems. It is not possible in general for **MOSEK** to check if a specific problems is convex since such a check would be NP hard in itself. This implies that care should be taken when solving problems involving general user defined functions.

`MSK_RES_TRM_USER_CALLBACK`
The optimizer terminated due to the return of the user-defined callback function.

`MSK_RES_TRM_MAX_NUM_SETBACKS`
The optimizer terminated as the maximum number of set-backs was reached. This indicates serious numerical problems and a possibly badly formulated problem.

`MSK_RES_TRM_NUMERICAL_PROBLEM`
The optimizer terminated due to numerical problems.

`MSK_RES_TRM_INTERNAL`
The optimizer terminated due to some internal reason. Please contact **MOSEK** support.

`MSK_RES_TRM_INTERNAL_STOP`
The optimizer terminated for internal reasons. Please contact **MOSEK** support.

13.3.2 Warnings

`MSK_RES_WRN_OPEN_PARAM_FILE`
The parameter file could not be opened.

`MSK_RES_WRN_LARGE_BOUND`
A numerically large bound value is specified.

`MSK_RES_WRN_LARGE_LO_BOUND`
A numerically large lower bound value is specified.

`MSK_RES_WRN_LARGE_UP_BOUND`
A numerically large upper bound value is specified.

`MSK_RES_WRN_LARGE_CON_FX`
An equality constraint is fixed to a numerically large value. This can cause numerical problems.

`MSK_RES_WRN_LARGE_CJ`
A numerically large value is specified for one c_j.

`MSK_RES_WRN_LARGE_AIJ`
A numerically large value is specified for an $a_{i,j}$ element in A. The parameter *MSK_DPAR_DATA_TOL_AIJ_LARGE* controls when an $a_{i,j}$ is considered large.

`MSK_RES_WRN_ZERO_AIJ`
One or more zero elements are specified in A.

`MSK_RES_WRN_NAME_MAX_LEN`
A name is longer than the buffer that is supposed to hold it.

`MSK_RES_WRN_SPAR_MAX_LEN`
A value for a string parameter is longer than the buffer that is supposed to hold it.

`MSK_RES_WRN_MPS_SPLIT_RHS_VECTOR`
An RHS vector is split into several nonadjacent parts in an MPS file.

`MSK_RES_WRN_MPS_SPLIT_RAN_VECTOR`
A RANGE vector is split into several nonadjacent parts in an MPS file.

`MSK_RES_WRN_MPS_SPLIT_BOU_VECTOR`
A BOUNDS vector is split into several nonadjacent parts in an MPS file.

`MSK_RES_WRN_LP_OLD_QUAD_FORMAT`
Missing '/2' after quadratic expressions in bound or objective.

`MSK_RES_WRN_LP_DROP_VARIABLE`
Ignored a variable because the variable was not previously defined. Usually this implies that a variable appears in the bound section but not in the objective or the constraints.

`MSK_RES_WRN_NZ_IN_UPR_TRI`
Non-zero elements specified in the upper triangle of a matrix were ignored.

`MSK_RES_WRN_DROPPED_NZ_QOBJ`
One or more non-zero elements were dropped in the Q matrix in the objective.

`MSK_RES_WRN_IGNORE_INTEGER`
Ignored integer constraints.

`MSK_RES_WRN_NO_GLOBAL_OPTIMIZER`
No global optimizer is available.

`MSK_RES_WRN_MIO_INFEASIBLE_FINAL`
The final mixed-integer problem with all the integer variables fixed at their optimal values is infeasible.

`MSK_RES_WRN_SOL_FILTER`
Invalid solution filter is specified.

`MSK_RES_WRN_UNDEF_SOL_FILE_NAME`
Undefined name occurred in a solution.

`MSK_RES_WRN_SOL_FILE_IGNORED_CON`
One or more lines in the constraint section were ignored when reading a solution file.

`MSK_RES_WRN_SOL_FILE_IGNORED_VAR`
One or more lines in the variable section were ignored when reading a solution file.

`MSK_RES_WRN_TOO_FEW_BASIS_VARS`
An incomplete basis has been specified. Too few basis variables are specified.

`MSK_RES_WRN_TOO_MANY_BASIS_VARS`
A basis with too many variables has been specified.

`MSK_RES_WRN_NO_NONLINEAR_FUNCTION_WRITE`
The problem contains a general nonlinear function in either the objective or the constraints. Such a nonlinear function cannot be written to a disk file. Note that quadratic terms when inputted explicitly can be written to disk.

`MSK_RES_WRN_LICENSE_EXPIRE`
The license expires.

`MSK_RES_WRN_LICENSE_SERVER`
The license server is not responding.

`MSK_RES_WRN_EMPTY_NAME`
A variable or constraint name is empty. The output file may be invalid.

`MSK_RES_WRN_USING_GENERIC_NAMES`
Generic names are used because a name is not valid. For instance when writing an LP file the names must not contain blanks or start with a digit.

`MSK_RES_WRN_LICENSE_FEATURE_EXPIRE`
The license expires.

`MSK_RES_WRN_PARAM_NAME_DOU`
The parameter name is not recognized as a double parameter.

`MSK_RES_WRN_PARAM_NAME_INT`
The parameter name is not recognized as a integer parameter.

`MSK_RES_WRN_PARAM_NAME_STR`
The parameter name is not recognized as a string parameter.

`MSK_RES_WRN_PARAM_STR_VALUE`
The string is not recognized as a symbolic value for the parameter.

`MSK_RES_WRN_PARAM_IGNORED_CMIO`
A parameter was ignored by the conic mixed integer optimizer.

`MSK_RES_WRN_ZEROS_IN_SPARSE_ROW`
One or more (near) zero elements are specified in a sparse row of a matrix. Since, it is redundant to specify zero elements then it may indicate an error.

`MSK_RES_WRN_ZEROS_IN_SPARSE_COL`
One or more (near) zero elements are specified in a sparse column of a matrix. It is redundant to specify zero elements. Hence, it may indicate an error.

`MSK_RES_WRN_INCOMPLETE_LINEAR_DEPENDENCY_CHECK`
The linear dependency check(s) is incomplete. Normally this is not an important warning unless the optimization problem has been formulated with linear dependencies. Linear dependencies may prevent **MOSEK** from solving the problem.

`MSK_RES_WRN_ELIMINATOR_SPACE`
The eliminator is skipped at least once due to lack of space.

`MSK_RES_WRN_PRESOLVE_OUTOFSPACE`
The presolve is incomplete due to lack of space.

`MSK_RES_WRN_WRITE_CHANGED_NAMES`
Some names were changed because they were invalid for the output file format.

`MSK_RES_WRN_WRITE_DISCARDED_CFIX`
The fixed objective term could not be converted to a variable and was discarded in the output file.

`MSK_RES_WRN_CONSTRUCT_SOLUTION_INFEAS`
After fixing the integer variables at the suggested values then the problem is infeasible.

`MSK_RES_WRN_CONSTRUCT_INVALID_SOL_ITG`
The initial value for one or more of the integer variables is not feasible.

`MSK_RES_WRN_CONSTRUCT_NO_SOL_ITG`
The construct solution requires an integer solution.

`MSK_RES_WRN_DUPLICATE_CONSTRAINT_NAMES`
Two constraint names are identical.

`MSK_RES_WRN_DUPLICATE_VARIABLE_NAMES`
Two variable names are identical.

`MSK_RES_WRN_DUPLICATE_BARVARIABLE_NAMES`
Two barvariable names are identical.

`MSK_RES_WRN_DUPLICATE_CONE_NAMES`
Two cone names are identical.

`MSK_RES_WRN_ANA_LARGE_BOUNDS`
This warning is issued by the problem analyzer, if one or more constraint or variable bounds are very large. One should consider omitting these bounds entirely by setting them to +inf or -inf.

`MSK_RES_WRN_ANA_C_ZERO`
This warning is issued by the problem analyzer, if the coefficients in the linear part of the objective are all zero.

`MSK_RES_WRN_ANA_EMPTY_COLS`
This warning is issued by the problem analyzer, if columns, in which all coefficients are zero, are found.

`MSK_RES_WRN_ANA_CLOSE_BOUNDS`
This warning is issued by problem analyzer, if ranged constraints or variables with very close upper and lower bounds are detected. One should consider treating such constraints as equalities and such variables as constants.

`MSK_RES_WRN_ANA_ALMOST_INT_BOUNDS`
This warning is issued by the problem analyzer if a constraint is bound nearly integral.

`MSK_RES_WRN_QUAD_CONES_WITH_ROOT_FIXED_AT_ZERO`
For at least one quadratic cone the root is fixed at (nearly) zero. This may cause problems such as a very large dual solution. Therefore, it is recommended to remove such cones before optimizing the problems, or to fix all the variables in the cone to 0.

`MSK_RES_WRN_RQUAD_CONES_WITH_ROOT_FIXED_AT_ZERO`
For at least one rotated quadratic cone at least one of the root variables are fixed at (nearly) zero. This may cause problems such as a very large dual solution. Therefore, it is recommended to remove such cones before optimizing the problems, or to fix all the variables in the cone to 0.

`MSK_RES_WRN_NO_DUALIZER`
No automatic dualizer is available for the specified problem. The primal problem is solved.

`MSK_RES_WRN_SYM_MAT_LARGE`
A numerically large value is specified for an $e_{i,j}$ element in E. The parameter *MSK_DPAR_DATA_SYM_MAT_TOL_LARGE* controls when an $e_{i,j}$ is considered large.

13.3.3 Errors

`MSK_RES_ERR_LICENSE`
Invalid license.

`MSK_RES_ERR_LICENSE_EXPIRED`
The license has expired.

`MSK_RES_ERR_LICENSE_VERSION`
The license is valid for another version of **MOSEK**.

`MSK_RES_ERR_SIZE_LICENSE`
The problem is bigger than the license.

`MSK_RES_ERR_PROB_LICENSE`
The software is not licensed to solve the problem.

`MSK_RES_ERR_FILE_LICENSE`
Invalid license file.

`MSK_RES_ERR_MISSING_LICENSE_FILE`
MOSEK cannot license file or a token server. See the **MOSEK** installation manual for details.

`MSK_RES_ERR_SIZE_LICENSE_CON`
The problem has too many constraints to be solved with the available license.

`MSK_RES_ERR_SIZE_LICENSE_VAR`
The problem has too many variables to be solved with the available license.

`MSK_RES_ERR_SIZE_LICENSE_INTVAR`
The problem contains too many integer variables to be solved with the available license.

`MSK_RES_ERR_OPTIMIZER_LICENSE`
The optimizer required is not licensed.

`MSK_RES_ERR_FLEXLM`
The FLEXlm license manager reported an error.

`MSK_RES_ERR_LICENSE_SERVER`
The license server is not responding.

`MSK_RES_ERR_LICENSE_MAX`
Maximum number of licenses is reached.

`MSK_RES_ERR_LICENSE_MOSEKLM_DAEMON`
The MOSEKLM license manager daemon is not up and running.

`MSK_RES_ERR_LICENSE_FEATURE`
A requested feature is not available in the license file(s). Most likely due to an incorrect license system setup.

`MSK_RES_ERR_PLATFORM_NOT_LICENSED`
A requested license feature is not available for the required platform.

`MSK_RES_ERR_LICENSE_CANNOT_ALLOCATE`
The license system cannot allocate the memory required.

`MSK_RES_ERR_LICENSE_CANNOT_CONNECT`
MOSEK cannot connect to the license server. Most likely the license server is not up and running.

`MSK_RES_ERR_LICENSE_INVALID_HOSTID`
The host ID specified in the license file does not match the host ID of the computer.

`MSK_RES_ERR_LICENSE_SERVER_VERSION`
The version specified in the checkout request is greater than the highest version number the daemon supports.

`MSK_RES_ERR_LICENSE_NO_SERVER_SUPPORT`
The license server does not support the requested feature. Possible reasons for this error include:

- The feature has expired.
- The feature's start date is later than today's date.
- The version requested is higher than feature's the highest supported version.
- A corrupted license file.

Try restarting the license and inspect the license server debug file, usually called `lmgrd.log`.

`MSK_RES_ERR_LICENSE_NO_SERVER_LINE`
: There is no `SERVER` line in the license file. All non-zero license count features need at least one `SERVER` line.

`MSK_RES_ERR_OPEN_DL`
: A dynamic link library could not be opened.

`MSK_RES_ERR_OLDER_DLL`
: The dynamic link library is older than the specified version.

`MSK_RES_ERR_NEWER_DLL`
: The dynamic link library is newer than the specified version.

`MSK_RES_ERR_LINK_FILE_DLL`
: A file cannot be linked to a stream in the DLL version.

`MSK_RES_ERR_THREAD_MUTEX_INIT`
: Could not initialize a mutex.

`MSK_RES_ERR_THREAD_MUTEX_LOCK`
: Could not lock a mutex.

`MSK_RES_ERR_THREAD_MUTEX_UNLOCK`
: Could not unlock a mutex.

`MSK_RES_ERR_THREAD_CREATE`
: Could not create a thread. This error may occur if a large number of environments are created and not deleted again. In any case it is a good practice to minimize the number of environments created.

`MSK_RES_ERR_THREAD_COND_INIT`
: Could not initialize a condition.

`MSK_RES_ERR_UNKNOWN`
: Unknown error.

`MSK_RES_ERR_SPACE`
: Out of space.

`MSK_RES_ERR_FILE_OPEN`
: Error while opening a file.

`MSK_RES_ERR_FILE_READ`
: File read error.

`MSK_RES_ERR_FILE_WRITE`
: File write error.

`MSK_RES_ERR_DATA_FILE_EXT`
: The data file format cannot be determined from the file name.

`MSK_RES_ERR_INVALID_FILE_NAME`
: An invalid file name has been specified.

`MSK_RES_ERR_INVALID_SOL_FILE_NAME`
: An invalid file name has been specified.

`MSK_RES_ERR_END_OF_FILE`
: End of file reached.

`MSK_RES_ERR_NULL_ENV`
: `env` is a NULL pointer.

`MSK_RES_ERR_NULL_TASK`
: `task` is a NULL pointer.

`MSK_RES_ERR_INVALID_STREAM`
An invalid stream is referenced.

`MSK_RES_ERR_NO_INIT_ENV`
`env` is not initialized.

`MSK_RES_ERR_INVALID_TASK`
The `task` is invalid.

`MSK_RES_ERR_NULL_POINTER`
An argument to a function is unexpectedly a NULL pointer.

`MSK_RES_ERR_LIVING_TASKS`
All tasks associated with an enviroment must be deleted before the environment is deleted. There are still some undeleted tasks.

`MSK_RES_ERR_BLANK_NAME`
An all blank name has been specified.

`MSK_RES_ERR_DUP_NAME`
The same name was used multiple times for the same problem item type.

`MSK_RES_ERR_INVALID_OBJ_NAME`
An invalid objective name is specified.

`MSK_RES_ERR_INVALID_CON_NAME`
An invalid constraint name is used.

`MSK_RES_ERR_INVALID_VAR_NAME`
An invalid variable name is used.

`MSK_RES_ERR_INVALID_CONE_NAME`
An invalid cone name is used.

`MSK_RES_ERR_INVALID_BARVAR_NAME`
An invalid symmetric matrix variable name is used.

`MSK_RES_ERR_SPACE_LEAKING`
MOSEK is leaking memory. This can be due to either an incorrect use of **MOSEK** or a bug.

`MSK_RES_ERR_SPACE_NO_INFO`
No available information about the space usage.

`MSK_RES_ERR_READ_FORMAT`
The specified format cannot be read.

`MSK_RES_ERR_MPS_FILE`
An error occurred while reading an MPS file.

`MSK_RES_ERR_MPS_INV_FIELD`
A field in the MPS file is invalid. Probably it is too wide.

`MSK_RES_ERR_MPS_INV_MARKER`
An invalid marker has been specified in the MPS file.

`MSK_RES_ERR_MPS_NULL_CON_NAME`
An empty constraint name is used in an MPS file.

`MSK_RES_ERR_MPS_NULL_VAR_NAME`
An empty variable name is used in an MPS file.

`MSK_RES_ERR_MPS_UNDEF_CON_NAME`
An undefined constraint name occurred in an MPS file.

`MSK_RES_ERR_MPS_UNDEF_VAR_NAME`
An undefined variable name occurred in an MPS file.

`MSK_RES_ERR_MPS_INV_CON_KEY`
An invalid constraint key occurred in an MPS file.

`MSK_RES_ERR_MPS_INV_BOUND_KEY`
An invalid bound key occurred in an MPS file.

`MSK_RES_ERR_MPS_INV_SEC_NAME`
An invalid section name occurred in an MPS file.

`MSK_RES_ERR_MPS_NO_OBJECTIVE`
No objective is defined in an MPS file.

`MSK_RES_ERR_MPS_SPLITTED_VAR`
All elements in a column of the A matrix must be specified consecutively. Hence, it is illegal to specify non-zero elements in A for variable 1, then for variable 2 and then variable 1 again.

`MSK_RES_ERR_MPS_MUL_CON_NAME`
A constraint name was specified multiple times in the `ROWS` section.

`MSK_RES_ERR_MPS_MUL_QSEC`
Multiple `QSECTION`s are specified for a constraint in the MPS data file.

`MSK_RES_ERR_MPS_MUL_QOBJ`
The Q term in the objective is specified multiple times in the MPS data file.

`MSK_RES_ERR_MPS_INV_SEC_ORDER`
The sections in the MPS data file are not in the correct order.

`MSK_RES_ERR_MPS_MUL_CSEC`
Multiple `CSECTION`s are given the same name.

`MSK_RES_ERR_MPS_CONE_TYPE`
Invalid cone type specified in a `CSECTION`.

`MSK_RES_ERR_MPS_CONE_OVERLAP`
A variable is specified to be a member of several cones.

`MSK_RES_ERR_MPS_CONE_REPEAT`
A variable is repeated within the `CSECTION`.

`MSK_RES_ERR_MPS_NON_SYMMETRIC_Q`
A non symmetric matrice has been speciefied.

`MSK_RES_ERR_MPS_DUPLICATE_Q_ELEMENT`
Duplicate elements is specfied in a Q matrix.

`MSK_RES_ERR_MPS_INVALID_OBJSENSE`
An invalid objective sense is specified.

`MSK_RES_ERR_MPS_TAB_IN_FIELD2`
A tab char occurred in field 2.

`MSK_RES_ERR_MPS_TAB_IN_FIELD3`
A tab char occurred in field 3.

`MSK_RES_ERR_MPS_TAB_IN_FIELD5`
A tab char occurred in field 5.

`MSK_RES_ERR_MPS_INVALID_OBJ_NAME`
An invalid objective name is specified.

`MSK_RES_ERR_LP_INCOMPATIBLE`
The problem cannot be written to an LP formatted file.

`MSK_RES_ERR_LP_EMPTY`
The problem cannot be written to an LP formatted file.

`MSK_RES_ERR_LP_DUP_SLACK_NAME`
The name of the slack variable added to a ranged constraint already exists.

`MSK_RES_ERR_WRITE_MPS_INVALID_NAME`
An invalid name is created while writing an MPS file. Usually this will make the MPS file unreadable.

`MSK_RES_ERR_LP_INVALID_VAR_NAME`
A variable name is invalid when used in an LP formatted file.

`MSK_RES_ERR_LP_FREE_CONSTRAINT`
Free constraints cannot be written in LP file format.

`MSK_RES_ERR_WRITE_OPF_INVALID_VAR_NAME`
Empty variable names cannot be written to OPF files.

`MSK_RES_ERR_LP_FILE_FORMAT`
Syntax error in an LP file.

`MSK_RES_ERR_WRITE_LP_FORMAT`
Problem cannot be written as an LP file.

`MSK_RES_ERR_READ_LP_MISSING_END_TAG`
Syntax error in LP file. Possibly missing End tag.

`MSK_RES_ERR_LP_FORMAT`
Syntax error in an LP file.

`MSK_RES_ERR_WRITE_LP_NON_UNIQUE_NAME`
An auto-generated name is not unique.

`MSK_RES_ERR_READ_LP_NONEXISTING_NAME`
A variable never occurred in objective or constraints.

`MSK_RES_ERR_LP_WRITE_CONIC_PROBLEM`
The problem contains cones that cannot be written to an LP formatted file.

`MSK_RES_ERR_LP_WRITE_GECO_PROBLEM`
The problem contains general convex terms that cannot be written to an LP formatted file.

`MSK_RES_ERR_WRITING_FILE`
An error occurred while writing file

`MSK_RES_ERR_OPF_FORMAT`
Syntax error in an OPF file

`MSK_RES_ERR_OPF_NEW_VARIABLE`
Introducing new variables is now allowed. When a `[variables]` section is present, it is not allowed to introduce new variables later in the problem.

`MSK_RES_ERR_INVALID_NAME_IN_SOL_FILE`
An invalid name occurred in a solution file.

`MSK_RES_ERR_LP_INVALID_CON_NAME`
A constraint name is invalid when used in an LP formatted file.

`MSK_RES_ERR_OPF_PREMATURE_EOF`
Premature end of file in an OPF file.

`MSK_RES_ERR_JSON_SYNTAX`
Syntax error in an JSON data

`MSK_RES_ERR_JSON_STRING`
Error in JSON string.

`MSK_RES_ERR_JSON_NUMBER_OVERFLOW`
Invalid number entry - wrong type or value overflow.

`MSK_RES_ERR_JSON_FORMAT`
Error in an JSON Task file

`MSK_RES_ERR_JSON_DATA`
Inconsistent data in JSON Task file

`MSK_RES_ERR_JSON_MISSING_DATA`
Missing data section in JSON task file.

`MSK_RES_ERR_ARGUMENT_LENNEQ`
Incorrect length of arguments.

`MSK_RES_ERR_ARGUMENT_TYPE`
Incorrect argument type.

`MSK_RES_ERR_NR_ARGUMENTS`
Incorrect number of function arguments.

`MSK_RES_ERR_IN_ARGUMENT`
A function argument is incorrect.

`MSK_RES_ERR_ARGUMENT_DIMENSION`
A function argument is of incorrect dimension.

`MSK_RES_ERR_INDEX_IS_TOO_SMALL`
An index in an argument is too small.

`MSK_RES_ERR_INDEX_IS_TOO_LARGE`
An index in an argument is too large.

`MSK_RES_ERR_PARAM_NAME`
The parameter name is not correct.

`MSK_RES_ERR_PARAM_NAME_DOU`
The parameter name is not correct for a double parameter.

`MSK_RES_ERR_PARAM_NAME_INT`
The parameter name is not correct for an integer parameter.

`MSK_RES_ERR_PARAM_NAME_STR`
The parameter name is not correct for a string parameter.

`MSK_RES_ERR_PARAM_INDEX`
Parameter index is out of range.

`MSK_RES_ERR_PARAM_IS_TOO_LARGE`
The parameter value is too large.

`MSK_RES_ERR_PARAM_IS_TOO_SMALL`
The parameter value is too small.

`MSK_RES_ERR_PARAM_VALUE_STR`
The parameter value string is incorrect.

`MSK_RES_ERR_PARAM_TYPE`
The parameter type is invalid.

`MSK_RES_ERR_INF_DOU_INDEX`
A double information index is out of range for the specified type.

`MSK_RES_ERR_INF_INT_INDEX`
An integer information index is out of range for the specified type.

`MSK_RES_ERR_INDEX_ARR_IS_TOO_SMALL`
An index in an array argument is too small.

`MSK_RES_ERR_INDEX_ARR_IS_TOO_LARGE`
An index in an array argument is too large.

`MSK_RES_ERR_INF_LINT_INDEX`
A long integer information index is out of range for the specified type.

`MSK_RES_ERR_ARG_IS_TOO_SMALL`
The value of a argument is too small.

`MSK_RES_ERR_ARG_IS_TOO_LARGE`
The value of a argument is too small.

`MSK_RES_ERR_INVALID_WHICHSOL`
`whichsol` is invalid.

`MSK_RES_ERR_INF_DOU_NAME`
A double information name is invalid.

`MSK_RES_ERR_INF_INT_NAME`
An integer information name is invalid.

`MSK_RES_ERR_INF_TYPE`
The information type is invalid.

`MSK_RES_ERR_INF_LINT_NAME`
A long integer information name is invalid.

`MSK_RES_ERR_INDEX`
An index is out of range.

`MSK_RES_ERR_WHICHSOL`
The solution defined by `whichsol` does not exists.

`MSK_RES_ERR_SOLITEM`
The solution item number `solitem` is invalid. Please note that *MSK_SOL_ITEM_SNX* is invalid for the basic solution.

`MSK_RES_ERR_WHICHITEM_NOT_ALLOWED`
whichitem is unacceptable.

`MSK_RES_ERR_MAXNUMCON`
The maximum number of constraints specified is smaller than the number of constraints in the task.

`MSK_RES_ERR_MAXNUMVAR`
The maximum number of variables specified is smaller than the number of variables in the task.

`MSK_RES_ERR_MAXNUMBARVAR`
The maximum number of semidefinite variables specified is smaller than the number of semidefinite variables in the task.

`MSK_RES_ERR_MAXNUMQNZ`
The maximum number of non-zeros specified for the Q matrices is smaller than the number of non-zeros in the current Q matrices.

`MSK_RES_ERR_TOO_SMALL_MAX_NUM_NZ`
The maximum number of non-zeros specified is too small.

`MSK_RES_ERR_INVALID_IDX`
A specified index is invalid.

`MSK_RES_ERR_INVALID_MAX_NUM`
A specified index is invalid.

`MSK_RES_ERR_NUMCONLIM`
Maximum number of constraints limit is exceeded.

`MSK_RES_ERR_NUMVARLIM`
Maximum number of variables limit is exceeded.

`MSK_RES_ERR_TOO_SMALL_MAXNUMANZ`
The maximum number of non-zeros specified for A is smaller than the number of non-zeros in the current A.

`MSK_RES_ERR_INV_APTRE`
: `aptre[j]` is strictly smaller than `aptrb[j]` for some `j`.

`MSK_RES_ERR_MUL_A_ELEMENT`
: An element in A is defined multiple times.

`MSK_RES_ERR_INV_BK`
: Invalid bound key.

`MSK_RES_ERR_INV_BKC`
: Invalid bound key is specified for a constraint.

`MSK_RES_ERR_INV_BKX`
: An invalid bound key is specified for a variable.

`MSK_RES_ERR_INV_VAR_TYPE`
: An invalid variable type is specified for a variable.

`MSK_RES_ERR_SOLVER_PROBTYPE`
: Problem type does not match the chosen optimizer.

`MSK_RES_ERR_OBJECTIVE_RANGE`
: Empty objective range.

`MSK_RES_ERR_FIRST`
: Invalid `first`.

`MSK_RES_ERR_LAST`
: Invalid index `last`. A given index was out of expected range.

`MSK_RES_ERR_NEGATIVE_SURPLUS`
: Negative surplus.

`MSK_RES_ERR_NEGATIVE_APPEND`
: Cannot append a negative number.

`MSK_RES_ERR_UNDEF_SOLUTION`
: **MOSEK** has the following solution types:

  - an interior-point solution,
  - an basic solution,
  - and an integer solution.

  Each optimizer may set one or more of these solutions; e.g by default a successful optimization with the interior-point optimizer defines the interior-point solution, and, for linear problems, also the basic solution. This error occurs when asking for a solution or for information about a solution that is not defined.

`MSK_RES_ERR_BASIS`
: An invalid basis is specified. Either too many or too few basis variables are specified.

`MSK_RES_ERR_INV_SKC`
: Invalid value in `skc`.

`MSK_RES_ERR_INV_SKX`
: Invalid value in `skx`.

`MSK_RES_ERR_INV_SKN`
: Invalid value in `skn`.

`MSK_RES_ERR_INV_SK_STR`
: Invalid status key string encountered.

`MSK_RES_ERR_INV_SK`
: Invalid status key code.

`MSK_RES_ERR_INV_CONE_TYPE_STR`
: Invalid cone type string encountered.

`MSK_RES_ERR_INV_CONE_TYPE`
Invalid cone type code is encountered.

`MSK_RES_ERR_INVALID_SURPLUS`
Invalid surplus.

`MSK_RES_ERR_INV_NAME_ITEM`
An invalid name item code is used.

`MSK_RES_ERR_PRO_ITEM`
An invalid problem is used.

`MSK_RES_ERR_INVALID_FORMAT_TYPE`
Invalid format type.

`MSK_RES_ERR_FIRSTI`
Invalid `firsti`.

`MSK_RES_ERR_LASTI`
Invalid `lasti`.

`MSK_RES_ERR_FIRSTJ`
Invalid `firstj`.

`MSK_RES_ERR_LASTJ`
Invalid `lastj`.

`MSK_RES_ERR_MAX_LEN_IS_TOO_SMALL`
An maximum length that is too small has been specified.

`MSK_RES_ERR_NONLINEAR_EQUALITY`
The model contains a nonlinear equality which defines a nonconvex set.

`MSK_RES_ERR_NONCONVEX`
The optimization problem is nonconvex.

`MSK_RES_ERR_NONLINEAR_RANGED`
Nonlinear constraints with finite lower and upper bound always define a nonconvex feasible set.

`MSK_RES_ERR_CON_Q_NOT_PSD`
The quadratic constraint matrix is not positive semidefinite as expected for a constraint with finite upper bound. This results in a nonconvex problem. The parameter *MSK_DPAR_CHECK_CONVEXITY_REL_TOL* can be used to relax the convexity check.

`MSK_RES_ERR_CON_Q_NOT_NSD`
The quadratic constraint matrix is not negative semidefinite as expected for a constraint with finite lower bound. This results in a nonconvex problem. The parameter *MSK_DPAR_CHECK_CONVEXITY_REL_TOL* can be used to relax the convexity check.

`MSK_RES_ERR_OBJ_Q_NOT_PSD`
The quadratic coefficient matrix in the objective is not positive semidefinite as expected for a minimization problem. The parameter *MSK_DPAR_CHECK_CONVEXITY_REL_TOL* can be used to relax the convexity check.

`MSK_RES_ERR_OBJ_Q_NOT_NSD`
The quadratic coefficient matrix in the objective is not negative semidefinite as expected for a maximization problem. The parameter *MSK_DPAR_CHECK_CONVEXITY_REL_TOL* can be used to relax the convexity check.

`MSK_RES_ERR_ARGUMENT_PERM_ARRAY`
An invalid permutation array is specified.

`MSK_RES_ERR_CONE_INDEX`
An index of a non-existing cone has been specified.

`MSK_RES_ERR_CONE_SIZE`
A cone with too few members is specified.

`MSK_RES_ERR_CONE_OVERLAP`
One or more of the variables in the cone to be added is already member of another cone. Now assume the variable is x_j then add a new variable say x_k and the constraint

$$x_j = x_k$$

and then let x_k be member of the cone to be appended.

`MSK_RES_ERR_CONE_REP_VAR`
A variable is included multiple times in the cone.

`MSK_RES_ERR_MAXNUMCONE`
The value specified for `maxnumcone` is too small.

`MSK_RES_ERR_CONE_TYPE`
Invalid cone type specified.

`MSK_RES_ERR_CONE_TYPE_STR`
Invalid cone type specified.

`MSK_RES_ERR_CONE_OVERLAP_APPEND`
The cone to be appended has one variable which is already member of another cone.

`MSK_RES_ERR_REMOVE_CONE_VARIABLE`
A variable cannot be removed because it will make a cone invalid.

`MSK_RES_ERR_SOL_FILE_INVALID_NUMBER`
An invalid number is specified in a solution file.

`MSK_RES_ERR_HUGE_C`
A huge value in absolute size is specified for one c_j.

`MSK_RES_ERR_HUGE_AIJ`
A numerically huge value is specified for an $a_{i,j}$ element in A. The parameter *MSK_DPAR_DATA_TOL_AIJ_HUGE* controls when an $a_{i,j}$ is considered huge.

`MSK_RES_ERR_DUPLICATE_AIJ`
An element in the A matrix is specified twice.

`MSK_RES_ERR_LOWER_BOUND_IS_A_NAN`
The lower bound specified is not a number (nan).

`MSK_RES_ERR_UPPER_BOUND_IS_A_NAN`
The upper bound specified is not a number (nan).

`MSK_RES_ERR_INFINITE_BOUND`
A numerically huge bound value is specified.

`MSK_RES_ERR_INV_QOBJ_SUBI`
Invalid value in `qosubi`.

`MSK_RES_ERR_INV_QOBJ_SUBJ`
Invalid value in `qosubj`.

`MSK_RES_ERR_INV_QOBJ_VAL`
Invalid value in `qoval`.

`MSK_RES_ERR_INV_QCON_SUBK`
Invalid value in `qcsubk`.

`MSK_RES_ERR_INV_QCON_SUBI`
Invalid value in `qcsubi`.

`MSK_RES_ERR_INV_QCON_SUBJ`
Invalid value in `qcsubj`.

`MSK_RES_ERR_INV_QCON_VAL`
Invalid value in `qcval`.

`MSK_RES_ERR_QCON_SUBI_TOO_SMALL`
Invalid value in `qcsubi`.

`MSK_RES_ERR_QCON_SUBI_TOO_LARGE`
Invalid value in `qcsubi`.

`MSK_RES_ERR_QOBJ_UPPER_TRIANGLE`
An element in the upper triangle of Q^o is specified. Only elements in the lower triangle should be specified.

`MSK_RES_ERR_QCON_UPPER_TRIANGLE`
An element in the upper triangle of a Q^k is specified. Only elements in the lower triangle should be specified.

`MSK_RES_ERR_FIXED_BOUND_VALUES`
A fixed constraint/variable has been specified using the bound keys but the numerical value of the lower and upper bound is different.

`MSK_RES_ERR_NONLINEAR_FUNCTIONS_NOT_ALLOWED`
An operation that is invalid for problems with nonlinear functions defined has been attempted.

`MSK_RES_ERR_USER_FUNC_RET`
An user function reported an error.

`MSK_RES_ERR_USER_FUNC_RET_DATA`
An user function returned invalid data.

`MSK_RES_ERR_USER_NLO_FUNC`
The user-defined nonlinear function reported an error.

`MSK_RES_ERR_USER_NLO_EVAL`
The user-defined nonlinear function reported an error.

`MSK_RES_ERR_USER_NLO_EVAL_HESSUBI`
The user-defined nonlinear function reported an invalid subscript in the Hessian.

`MSK_RES_ERR_USER_NLO_EVAL_HESSUBJ`
The user-defined nonlinear function reported an invalid subscript in the Hessian.

`MSK_RES_ERR_INVALID_OBJECTIVE_SENSE`
An invalid objective sense is specified.

`MSK_RES_ERR_UNDEFINED_OBJECTIVE_SENSE`
The objective sense has not been specified before the optimization.

`MSK_RES_ERR_Y_IS_UNDEFINED`
The solution item y is undefined.

`MSK_RES_ERR_NAN_IN_DOUBLE_DATA`
An invalid floating point value was used in some double data.

`MSK_RES_ERR_NAN_IN_BLC`
l^c contains an invalid floating point value, i.e. a `NaN`.

`MSK_RES_ERR_NAN_IN_BUC`
u^c contains an invalid floating point value, i.e. a `NaN`.

`MSK_RES_ERR_NAN_IN_C`
c contains an invalid floating point value, i.e. a `NaN`.

`MSK_RES_ERR_NAN_IN_BLX`
l^x contains an invalid floating point value, i.e. a `NaN`.

`MSK_RES_ERR_NAN_IN_BUX`
u^x contains an invalid floating point value, i.e. a `NaN`.

`MSK_RES_ERR_INVALID_AIJ`
$a_{i,j}$ contains an invalid floating point value, i.e. a `NaN` or an infinite value.

MSK_RES_ERR_SYM_MAT_INVALID
: A symmetric matrix contains an invalid floating point value, i.e. a NaN or an infinite value.

MSK_RES_ERR_SYM_MAT_HUGE
: A symmetric matrix contains a huge value in absolute size. The parameter *MSK_DPAR_DATA_SYM_MAT_TOL_HUGE* controls when an $e_{i,j}$ is considered huge.

MSK_RES_ERR_INV_PROBLEM
: Invalid problem type. Probably a nonconvex problem has been specified.

MSK_RES_ERR_MIXED_CONIC_AND_NL
: The problem contains nonlinear terms conic constraints. The requested operation cannot be applied to this type of problem.

MSK_RES_ERR_GLOBAL_INV_CONIC_PROBLEM
: The global optimizer can only be applied to problems without semidefinite variables.

MSK_RES_ERR_INV_OPTIMIZER
: An invalid optimizer has been chosen for the problem. This means that the simplex or the conic optimizer is chosen to optimize a nonlinear problem.

MSK_RES_ERR_MIO_NO_OPTIMIZER
: No optimizer is available for the current class of integer optimization problems.

MSK_RES_ERR_NO_OPTIMIZER_VAR_TYPE
: No optimizer is available for this class of optimization problems.

MSK_RES_ERR_FINAL_SOLUTION
: An error occurred during the solution finalization.

MSK_RES_ERR_POSTSOLVE
: An error occurred during the postsolve. Please contact **MOSEK** support.

MSK_RES_ERR_OVERFLOW
: A computation produced an overflow i.e. a very large number.

MSK_RES_ERR_NO_BASIS_SOL
: No basic solution is defined.

MSK_RES_ERR_BASIS_FACTOR
: The factorization of the basis is invalid.

MSK_RES_ERR_BASIS_SINGULAR
: The basis is singular and hence cannot be factored.

MSK_RES_ERR_FACTOR
: An error occurred while factorizing a matrix.

MSK_RES_ERR_FEASREPAIR_CANNOT_RELAX
: An optimization problem cannot be relaxed. This is the case e.g. for general nonlinear optimization problems.

MSK_RES_ERR_FEASREPAIR_SOLVING_RELAXED
: The relaxed problem could not be solved to optimality. Please consult the log file for further details.

MSK_RES_ERR_FEASREPAIR_INCONSISTENT_BOUND
: The upper bound is less than the lower bound for a variable or a constraint. Please correct this before running the feasibility repair.

MSK_RES_ERR_REPAIR_INVALID_PROBLEM
: The feasibility repair does not support the specified problem type.

MSK_RES_ERR_REPAIR_OPTIMIZATION_FAILED
: Computation the optimal relaxation failed. The cause may have been numerical problems.

MSK_RES_ERR_NAME_MAX_LEN
: A name is longer than the buffer that is supposed to hold it.

`MSK_RES_ERR_NAME_IS_NULL`
The name buffer is a NULL pointer.

`MSK_RES_ERR_INVALID_COMPRESSION`
Invalid compression type.

`MSK_RES_ERR_INVALID_IOMODE`
Invalid io mode.

`MSK_RES_ERR_NO_PRIMAL_INFEAS_CER`
A certificate of primal infeasibility is not available.

`MSK_RES_ERR_NO_DUAL_INFEAS_CER`
A certificate of infeasibility is not available.

`MSK_RES_ERR_NO_SOLUTION_IN_CALLBACK`
The required solution is not available.

`MSK_RES_ERR_INV_MARKI`
Invalid value in marki.

`MSK_RES_ERR_INV_MARKJ`
Invalid value in markj.

`MSK_RES_ERR_INV_NUMI`
Invalid numi.

`MSK_RES_ERR_INV_NUMJ`
Invalid numj.

`MSK_RES_ERR_CANNOT_CLONE_NL`
A task with a nonlinear function callback cannot be cloned.

`MSK_RES_ERR_CANNOT_HANDLE_NL`
A function cannot handle a task with nonlinear function callbacks.

`MSK_RES_ERR_INVALID_ACCMODE`
An invalid access mode is specified.

`MSK_RES_ERR_TASK_INCOMPATIBLE`
The Task file is incompatible with this platform. This results from reading a file on a 32 bit platform generated on a 64 bit platform.

`MSK_RES_ERR_TASK_INVALID`
The Task file is invalid.

`MSK_RES_ERR_TASK_WRITE`
Failed to write the task file.

`MSK_RES_ERR_LU_MAX_NUM_TRIES`
Could not compute the LU factors of the matrix within the maximum number of allowed tries.

`MSK_RES_ERR_INVALID_UTF8`
An invalid UTF8 string is encountered.

`MSK_RES_ERR_INVALID_WCHAR`
An invalid `wchar` string is encountered.

`MSK_RES_ERR_NO_DUAL_FOR_ITG_SOL`
No dual information is available for the integer solution.

`MSK_RES_ERR_NO_SNX_FOR_BAS_SOL`
s_n^x is not available for the basis solution.

`MSK_RES_ERR_INTERNAL`
An internal error occurred. Please report this problem.

`MSK_RES_ERR_API_ARRAY_TOO_SMALL`
An input array was too short.

`MSK_RES_ERR_API_CB_CONNECT`
Failed to connect a callback object.

`MSK_RES_ERR_API_FATAL_ERROR`
An internal error occurred in the API. Please report this problem.

`MSK_RES_ERR_API_INTERNAL`
An internal fatal error occurred in an interface function.

`MSK_RES_ERR_SEN_FORMAT`
Syntax error in sensitivity analysis file.

`MSK_RES_ERR_SEN_UNDEF_NAME`
An undefined name was encountered in the sensitivity analysis file.

`MSK_RES_ERR_SEN_INDEX_RANGE`
Index out of range in the sensitivity analysis file.

`MSK_RES_ERR_SEN_BOUND_INVALID_UP`
Analysis of upper bound requested for an index, where no upper bound exists.

`MSK_RES_ERR_SEN_BOUND_INVALID_LO`
Analysis of lower bound requested for an index, where no lower bound exists.

`MSK_RES_ERR_SEN_INDEX_INVALID`
Invalid range given in the sensitivity file.

`MSK_RES_ERR_SEN_INVALID_REGEXP`
Syntax error in regexp or regexp longer than 1024.

`MSK_RES_ERR_SEN_SOLUTION_STATUS`
No optimal solution found to the original problem given for sensitivity analysis.

`MSK_RES_ERR_SEN_NUMERICAL`
Numerical difficulties encountered performing the sensitivity analysis.

`MSK_RES_ERR_SEN_UNHANDLED_PROBLEM_TYPE`
Sensitivity analysis cannot be performed for the specified problem. Sensitivity analysis is only possible for linear problems.

`MSK_RES_ERR_UNB_STEP_SIZE`
A step size in an optimizer was unexpectedly unbounded. For instance, if the step-size becomes unbounded in phase 1 of the simplex algorithm then an error occurs. Normally this will happen only if the problem is badly formulated. Please contact **MOSEK** support if this error occurs.

`MSK_RES_ERR_IDENTICAL_TASKS`
Some tasks related to this function call were identical. Unique tasks were expected.

`MSK_RES_ERR_AD_INVALID_CODELIST`
The code list data was invalid.

`MSK_RES_ERR_INTERNAL_TEST_FAILED`
An internal unit test function failed.

`MSK_RES_ERR_XML_INVALID_PROBLEM_TYPE`
The problem type is not supported by the XML format.

`MSK_RES_ERR_INVALID_AMPL_STUB`
Invalid AMPL stub.

`MSK_RES_ERR_INT64_TO_INT32_CAST`
An 32 bit integer could not cast to a 64 bit integer.

`MSK_RES_ERR_SIZE_LICENSE_NUMCORES`
The computer contains more cpu cores than the license allows for.

`MSK_RES_ERR_INFEAS_UNDEFINED`
The requested value is not defined for this solution type.

MSK_RES_ERR_NO_BARX_FOR_SOLUTION
: There is no $\overline{X}$ available for the solution specified. In particular note there are no $\overline{X}$ defined for the basic and integer solutions.

MSK_RES_ERR_NO_BARS_FOR_SOLUTION
: There is no $\bar{s}$ available for the solution specified. In particular note there are no $\bar{s}$ defined for the basic and integer solutions.

MSK_RES_ERR_BAR_VAR_DIM
: The dimension of a symmetric matrix variable has to greater than 0.

MSK_RES_ERR_SYM_MAT_INVALID_ROW_INDEX
: A row index specified for sparse symmetric matrix is invalid.

MSK_RES_ERR_SYM_MAT_INVALID_COL_INDEX
: A column index specified for sparse symmetric matrix is invalid.

MSK_RES_ERR_SYM_MAT_NOT_LOWER_TRINGULAR
: Only the lower triangular part of sparse symmetric matrix should be specified.

MSK_RES_ERR_SYM_MAT_INVALID_VALUE
: The numerical value specified in a sparse symmetric matrix is not a value floating value.

MSK_RES_ERR_SYM_MAT_DUPLICATE
: A value in a symmetric matric as been specified more than once.

MSK_RES_ERR_INVALID_SYM_MAT_DIM
: A sparse symmetric matrix of invalid dimension is specified.

MSK_RES_ERR_INVALID_FILE_FORMAT_FOR_SYM_MAT
: The file format does not support a problem with symmetric matrix variables.

MSK_RES_ERR_INVALID_FILE_FORMAT_FOR_CONES
: The file format does not support a problem with conic constraints.

MSK_RES_ERR_INVALID_FILE_FORMAT_FOR_GENERAL_NL
: The file format does not support a problem with general nonlinear terms.

MSK_RES_ERR_DUPLICATE_CONSTRAINT_NAMES
: Two constraint names are identical.

MSK_RES_ERR_DUPLICATE_VARIABLE_NAMES
: Two variable names are identical.

MSK_RES_ERR_DUPLICATE_BARVARIABLE_NAMES
: Two barvariable names are identical.

MSK_RES_ERR_DUPLICATE_CONE_NAMES
: Two cone names are identical.

MSK_RES_ERR_NON_UNIQUE_ARRAY
: An array does not contain unique elements.

MSK_RES_ERR_ARGUMENT_IS_TOO_LARGE
: The value of a function argument is too large.

MSK_RES_ERR_MIO_INTERNAL
: A fatal error occurred in the mixed integer optimizer. Please contact **MOSEK** support.

MSK_RES_ERR_INVALID_PROBLEM_TYPE
: An invalid problem type.

MSK_RES_ERR_UNHANDLED_SOLUTION_STATUS
: Unhandled solution status.

MSK_RES_ERR_UPPER_TRIANGLE
: An element in the upper triangle of a lower triangular matrix is specified.

`MSK_RES_ERR_LAU_SINGULAR_MATRIX`
A matrix is singular.

`MSK_RES_ERR_LAU_NOT_POSITIVE_DEFINITE`
A matrix is not positive definite.

`MSK_RES_ERR_LAU_INVALID_LOWER_TRIANGULAR_MATRIX`
An invalid lower triangular matrix.

`MSK_RES_ERR_LAU_UNKNOWN`
An unknown error.

`MSK_RES_ERR_LAU_ARG_M`
Invalid argument m.

`MSK_RES_ERR_LAU_ARG_N`
Invalid argument n.

`MSK_RES_ERR_LAU_ARG_K`
Invalid argument k.

`MSK_RES_ERR_LAU_ARG_TRANSA`
Invalid argument transa.

`MSK_RES_ERR_LAU_ARG_TRANSB`
Invalid argument transb.

`MSK_RES_ERR_LAU_ARG_UPLO`
Invalid argument uplo.

`MSK_RES_ERR_LAU_ARG_TRANS`
Invalid argument trans.

`MSK_RES_ERR_LAU_INVALID_SPARSE_SYMMETRIC_MATRIX`
An invalid sparse symmetric matrix is specfified. Note only the lower triangular part with no duplicates is specifed.

`MSK_RES_ERR_CBF_PARSE`
An error occurred while parsing an CBF file.

`MSK_RES_ERR_CBF_OBJ_SENSE`
An invalid objective sense is specified.

`MSK_RES_ERR_CBF_NO_VARIABLES`
No variables are specified.

`MSK_RES_ERR_CBF_TOO_MANY_CONSTRAINTS`
Too many constraints specified.

`MSK_RES_ERR_CBF_TOO_MANY_VARIABLES`
Too many variables specified.

`MSK_RES_ERR_CBF_NO_VERSION_SPECIFIED`
No version specified.

`MSK_RES_ERR_CBF_SYNTAX`
Invalid syntax.

`MSK_RES_ERR_CBF_DUPLICATE_OBJ`
Duplicate OBJ keyword.

`MSK_RES_ERR_CBF_DUPLICATE_CON`
Duplicate CON keyword.

`MSK_RES_ERR_CBF_DUPLICATE_VAR`
Duplicate VAR keyword.

`MSK_RES_ERR_CBF_DUPLICATE_INT`
Duplicate INT keyword.

`MSK_RES_ERR_CBF_INVALID_VAR_TYPE`
Invalid variable type.

`MSK_RES_ERR_CBF_INVALID_CON_TYPE`
Invalid constraint type.

`MSK_RES_ERR_CBF_INVALID_DOMAIN_DIMENSION`
Invalid domain dimension.

`MSK_RES_ERR_CBF_DUPLICATE_OBJACOORD`
Duplicate index in OBJCOORD.

`MSK_RES_ERR_CBF_DUPLICATE_BCOORD`
Duplicate index in BCOORD.

`MSK_RES_ERR_CBF_DUPLICATE_ACOORD`
Duplicate index in ACOORD.

`MSK_RES_ERR_CBF_TOO_FEW_VARIABLES`
Too few variables defined.

`MSK_RES_ERR_CBF_TOO_FEW_CONSTRAINTS`
Too few constraints defined.

`MSK_RES_ERR_CBF_TOO_FEW_INTS`
Too few ints are specified.

`MSK_RES_ERR_CBF_TOO_MANY_INTS`
Too many ints are specified.

`MSK_RES_ERR_CBF_INVALID_INT_INDEX`
Invalid INT index.

`MSK_RES_ERR_CBF_UNSUPPORTED`
Unsupported feature is present.

`MSK_RES_ERR_CBF_DUPLICATE_PSDVAR`
Duplicate PSDVAR keyword.

`MSK_RES_ERR_CBF_INVALID_PSDVAR_DIMENSION`
Invalid PSDVAR dimmension.

`MSK_RES_ERR_CBF_TOO_FEW_PSDVAR`
Too few variables defined.

`MSK_RES_ERR_MIO_INVALID_ROOT_OPTIMIZER`
An invalid root optimizer was selected for the problem type.

`MSK_RES_ERR_MIO_INVALID_NODE_OPTIMIZER`
An invalid node optimizer was selected for the problem type.

`MSK_RES_ERR_TOCONIC_CONSTR_Q_NOT_PSD`
The matrix defining the quadratric part of constraint is not positive semidefinite.

`MSK_RES_ERR_TOCONIC_CONSTRAINT_FX`
The quadratic constraint is an equality, thus not convex.

`MSK_RES_ERR_TOCONIC_CONSTRAINT_RA`
The quadratic constraint has finite lower and upper bound, and therefore it is not convex.

`MSK_RES_ERR_TOCONIC_CONSTR_NOT_CONIC`
The constraint is not conic representable.

`MSK_RES_ERR_TOCONIC_OBJECTIVE_NOT_PSD`
The matrix defining the quadratric part of the objective function is not positive semidefinite.

`MSK_RES_ERR_SERVER_CONNECT`
Failed to connect to remote solver server. The server string or the port string were invalid, or the server did not accept connection.

`MSK_RES_ERR_SERVER_PROTOCOL`
Unexpected message or data from solver server.

`MSK_RES_ERR_SERVER_STATUS`
Server returned non-ok HTTP status code

`MSK_RES_ERR_SERVER_TOKEN`
The job ID specified is incorrect or invalid

13.4 Constants

13.4.1 Language selection constants

`MSK_LANG_ENG`
English language selection

`MSK_LANG_DAN`
Danish language selection

13.4.2 Constraint or variable access modes

`MSK_ACC_VAR`
Access data by columns (variable oriented)

`MSK_ACC_CON`
Access data by rows (constraint oriented)

13.4.3 Basis identification

`MSK_BI_NEVER`
Never do basis identification.

`MSK_BI_ALWAYS`
Basis identification is always performed even if the interior-point optimizer terminates abnormally.

`MSK_BI_NO_ERROR`
Basis identification is performed if the interior-point optimizer terminates without an error.

`MSK_BI_IF_FEASIBLE`
Basis identification is not performed if the interior-point optimizer terminates with a problem status saying that the problem is primal or dual infeasible.

`MSK_BI_RESERVERED`
Not currently in use.

13.4.4 Bound keys

`MSK_BK_LO`
The constraint or variable has a finite lower bound and an infinite upper bound.

`MSK_BK_UP`
The constraint or variable has an infinite lower bound and an finite upper bound.

`MSK_BK_FX`
The constraint or variable is fixed.

`MSK_BK_FR`
The constraint or variable is free.

`MSK_BK_RA`
: The constraint or variable is ranged.

13.4.5 Mark

`MSK_MARK_LO`
: The lower bound is selected for sensitivity analysis.

`MSK_MARK_UP`
: The upper bound is selected for sensitivity analysis.

13.4.6 Degeneracy strategies

`MSK_SIM_DEGEN_NONE`
: The simplex optimizer should use no degeneration strategy.

`MSK_SIM_DEGEN_FREE`
: The simplex optimizer chooses the degeneration strategy.

`MSK_SIM_DEGEN_AGGRESSIVE`
: The simplex optimizer should use an aggressive degeneration strategy.

`MSK_SIM_DEGEN_MODERATE`
: The simplex optimizer should use a moderate degeneration strategy.

`MSK_SIM_DEGEN_MINIMUM`
: The simplex optimizer should use a minimum degeneration strategy.

13.4.7 Transposed matrix.

`MSK_TRANSPOSE_NO`
: No transpose is applied.

`MSK_TRANSPOSE_YES`
: A transpose is applied.

13.4.8 Triangular part of a symmetric matrix.

`MSK_UPLO_LO`
: Lower part.

`MSK_UPLO_UP`
: Upper part

13.4.9 Problem reformulation.

`MSK_SIM_REFORMULATION_ON`
: Allow the simplex optimizer to reformulate the problem.

`MSK_SIM_REFORMULATION_OFF`
: Disallow the simplex optimizer to reformulate the problem.

`MSK_SIM_REFORMULATION_FREE`
: The simplex optimizer can choose freely.

`MSK_SIM_REFORMULATION_AGGRESSIVE`
: The simplex optimizer should use an aggressive reformulation strategy.

13.4.10 Exploit duplicate columns.

`MSK_SIM_EXPLOIT_DUPVEC_ON`
Allow the simplex optimizer to exploit duplicated columns.

`MSK_SIM_EXPLOIT_DUPVEC_OFF`
Disallow the simplex optimizer to exploit duplicated columns.

`MSK_SIM_EXPLOIT_DUPVEC_FREE`
The simplex optimizer can choose freely.

13.4.11 Hot-start type employed by the simplex optimizer

`MSK_SIM_HOTSTART_NONE`
The simplex optimizer performs a coldstart.

`MSK_SIM_HOTSTART_FREE`
The simplex optimize chooses the hot-start type.

`MSK_SIM_HOTSTART_STATUS_KEYS`
Only the status keys of the constraints and variables are used to choose the type of hot-start.

13.4.12 Hot-start type employed by the interior-point optimizers.

`MSK_INTPNT_HOTSTART_NONE`
The interior-point optimizer performs a coldstart.

`MSK_INTPNT_HOTSTART_PRIMAL`
The interior-point optimizer exploits the primal solution only.

`MSK_INTPNT_HOTSTART_DUAL`
The interior-point optimizer exploits the dual solution only.

`MSK_INTPNT_HOTSTART_PRIMAL_DUAL`
The interior-point optimizer exploits both the primal and dual solution.

13.4.13 Progress callback codes

`MSK_CALLBACK_BEGIN_BI`
The basis identification procedure has been started.

`MSK_CALLBACK_BEGIN_CONIC`
The callback function is called when the conic optimizer is started.

`MSK_CALLBACK_BEGIN_DUAL_BI`
The callback function is called from within the basis identification procedure when the dual phase is started.

`MSK_CALLBACK_BEGIN_DUAL_SENSITIVITY`
Dual sensitivity analysis is started.

`MSK_CALLBACK_BEGIN_DUAL_SETUP_BI`
The callback function is called when the dual BI phase is started.

`MSK_CALLBACK_BEGIN_DUAL_SIMPLEX`
The callback function is called when the dual simplex optimizer started.

`MSK_CALLBACK_BEGIN_DUAL_SIMPLEX_BI`
The callback function is called from within the basis identification procedure when the dual simplex clean-up phase is started.

`MSK_CALLBACK_BEGIN_FULL_CONVEXITY_CHECK`
Begin full convexity check.

`MSK_CALLBACK_BEGIN_INFEAS_ANA`
The callback function is called when the infeasibility analyzer is started.

`MSK_CALLBACK_BEGIN_INTPNT`
The callback function is called when the interior-point optimizer is started.

`MSK_CALLBACK_BEGIN_LICENSE_WAIT`
Begin waiting for license.

`MSK_CALLBACK_BEGIN_MIO`
The callback function is called when the mixed-integer optimizer is started.

`MSK_CALLBACK_BEGIN_OPTIMIZER`
The callback function is called when the optimizer is started.

`MSK_CALLBACK_BEGIN_PRESOLVE`
The callback function is called when the presolve is started.

`MSK_CALLBACK_BEGIN_PRIMAL_BI`
The callback function is called from within the basis identification procedure when the primal phase is started.

`MSK_CALLBACK_BEGIN_PRIMAL_REPAIR`
Begin primal feasibility repair.

`MSK_CALLBACK_BEGIN_PRIMAL_SENSITIVITY`
Primal sensitivity analysis is started.

`MSK_CALLBACK_BEGIN_PRIMAL_SETUP_BI`
The callback function is called when the primal BI setup is started.

`MSK_CALLBACK_BEGIN_PRIMAL_SIMPLEX`
The callback function is called when the primal simplex optimizer is started.

`MSK_CALLBACK_BEGIN_PRIMAL_SIMPLEX_BI`
The callback function is called from within the basis identification procedure when the primal simplex clean-up phase is started.

`MSK_CALLBACK_BEGIN_QCQO_REFORMULATE`
Begin QCQO reformulation.

`MSK_CALLBACK_BEGIN_READ`
MOSEK has started reading a problem file.

`MSK_CALLBACK_BEGIN_ROOT_CUTGEN`
The callback function is called when root cut generation is started.

`MSK_CALLBACK_BEGIN_SIMPLEX`
The callback function is called when the simplex optimizer is started.

`MSK_CALLBACK_BEGIN_SIMPLEX_BI`
The callback function is called from within the basis identification procedure when the simplex clean-up phase is started.

`MSK_CALLBACK_BEGIN_TO_CONIC`
Begin conic reformulation.

`MSK_CALLBACK_BEGIN_WRITE`
MOSEK has started writing a problem file.

`MSK_CALLBACK_CONIC`
The callback function is called from within the conic optimizer after the information database has been updated.

`MSK_CALLBACK_DUAL_SIMPLEX`
The callback function is called from within the dual simplex optimizer.

`MSK_CALLBACK_END_BI`
The callback function is called when the basis identification procedure is terminated.

`MSK_CALLBACK_END_CONIC`
The callback function is called when the conic optimizer is terminated.

`MSK_CALLBACK_END_DUAL_BI`
The callback function is called from within the basis identification procedure when the dual phase is terminated.

`MSK_CALLBACK_END_DUAL_SENSITIVITY`
Dual sensitivity analysis is terminated.

`MSK_CALLBACK_END_DUAL_SETUP_BI`
The callback function is called when the dual BI phase is terminated.

`MSK_CALLBACK_END_DUAL_SIMPLEX`
The callback function is called when the dual simplex optimizer is terminated.

`MSK_CALLBACK_END_DUAL_SIMPLEX_BI`
The callback function is called from within the basis identification procedure when the dual clean-up phase is terminated.

`MSK_CALLBACK_END_FULL_CONVEXITY_CHECK`
End full convexity check.

`MSK_CALLBACK_END_INFEAS_ANA`
The callback function is called when the infeasibility analyzer is terminated.

`MSK_CALLBACK_END_INTPNT`
The callback function is called when the interior-point optimizer is terminated.

`MSK_CALLBACK_END_LICENSE_WAIT`
End waiting for license.

`MSK_CALLBACK_END_MIO`
The callback function is called when the mixed-integer optimizer is terminated.

`MSK_CALLBACK_END_OPTIMIZER`
The callback function is called when the optimizer is terminated.

`MSK_CALLBACK_END_PRESOLVE`
The callback function is called when the presolve is completed.

`MSK_CALLBACK_END_PRIMAL_BI`
The callback function is called from within the basis identification procedure when the primal phase is terminated.

`MSK_CALLBACK_END_PRIMAL_REPAIR`
End primal feasibility repair.

`MSK_CALLBACK_END_PRIMAL_SENSITIVITY`
Primal sensitivity analysis is terminated.

`MSK_CALLBACK_END_PRIMAL_SETUP_BI`
The callback function is called when the primal BI setup is terminated.

`MSK_CALLBACK_END_PRIMAL_SIMPLEX`
The callback function is called when the primal simplex optimizer is terminated.

`MSK_CALLBACK_END_PRIMAL_SIMPLEX_BI`
The callback function is called from within the basis identification procedure when the primal clean-up phase is terminated.

`MSK_CALLBACK_END_QCQO_REFORMULATE`
End QCQO reformulation.

`MSK_CALLBACK_END_READ`
MOSEK has finished reading a problem file.

`MSK_CALLBACK_END_ROOT_CUTGEN`
The callback function is called when root cut generation is is terminated.

`MSK_CALLBACK_END_SIMPLEX`
The callback function is called when the simplex optimizer is terminated.

`MSK_CALLBACK_END_SIMPLEX_BI`
The callback function is called from within the basis identification procedure when the simplex clean-up phase is terminated.

`MSK_CALLBACK_END_TO_CONIC`
End conic reformulation.

`MSK_CALLBACK_END_WRITE`
MOSEK has finished writing a problem file.

`MSK_CALLBACK_IM_BI`
The callback function is called from within the basis identification procedure at an intermediate point.

`MSK_CALLBACK_IM_CONIC`
The callback function is called at an intermediate stage within the conic optimizer where the information database has not been updated.

`MSK_CALLBACK_IM_DUAL_BI`
The callback function is called from within the basis identification procedure at an intermediate point in the dual phase.

`MSK_CALLBACK_IM_DUAL_SENSIVITY`
The callback function is called at an intermediate stage of the dual sensitivity analysis.

`MSK_CALLBACK_IM_DUAL_SIMPLEX`
The callback function is called at an intermediate point in the dual simplex optimizer.

`MSK_CALLBACK_IM_FULL_CONVEXITY_CHECK`
The callback function is called at an intermediate stage of the full convexity check.

`MSK_CALLBACK_IM_INTPNT`
The callback function is called at an intermediate stage within the interior-point optimizer where the information database has not been updated.

`MSK_CALLBACK_IM_LICENSE_WAIT`
MOSEK is waiting for a license.

`MSK_CALLBACK_IM_LU`
The callback function is called from within the LU factorization procedure at an intermediate point.

`MSK_CALLBACK_IM_MIO`
The callback function is called at an intermediate point in the mixed-integer optimizer.

`MSK_CALLBACK_IM_MIO_DUAL_SIMPLEX`
The callback function is called at an intermediate point in the mixed-integer optimizer while running the dual simplex optimizer.

`MSK_CALLBACK_IM_MIO_INTPNT`
The callback function is called at an intermediate point in the mixed-integer optimizer while running the interior-point optimizer.

`MSK_CALLBACK_IM_MIO_PRIMAL_SIMPLEX`
The callback function is called at an intermediate point in the mixed-integer optimizer while running the primal simplex optimizer.

`MSK_CALLBACK_IM_ORDER`
The callback function is called from within the matrix ordering procedure at an intermediate point.

`MSK_CALLBACK_IM_PRESOLVE`
The callback function is called from within the presolve procedure at an intermediate stage.

`MSK_CALLBACK_IM_PRIMAL_BI`
: The callback function is called from within the basis identification procedure at an intermediate point in the primal phase.

`MSK_CALLBACK_IM_PRIMAL_SENSIVITY`
: The callback function is called at an intermediate stage of the primal sensitivity analysis.

`MSK_CALLBACK_IM_PRIMAL_SIMPLEX`
: The callback function is called at an intermediate point in the primal simplex optimizer.

`MSK_CALLBACK_IM_QO_REFORMULATE`
: The callback function is called at an intermediate stage of the conic quadratic reformulation.

`MSK_CALLBACK_IM_READ`
: Intermediate stage in reading.

`MSK_CALLBACK_IM_ROOT_CUTGEN`
: The callback is called from within root cut generation at an intermediate stage.

`MSK_CALLBACK_IM_SIMPLEX`
: The callback function is called from within the simplex optimizer at an intermediate point.

`MSK_CALLBACK_IM_SIMPLEX_BI`
: The callback function is called from within the basis identification procedure at an intermediate point in the simplex clean-up phase. The frequency of the callbacks is controlled by the *MSK_IPAR_LOG_SIM_FREQ* parameter.

`MSK_CALLBACK_INTPNT`
: The callback function is called from within the interior-point optimizer after the information database has been updated.

`MSK_CALLBACK_NEW_INT_MIO`
: The callback function is called after a new integer solution has been located by the mixed-integer optimizer.

`MSK_CALLBACK_PRIMAL_SIMPLEX`
: The callback function is called from within the primal simplex optimizer.

`MSK_CALLBACK_READ_OPF`
: The callback function is called from the OPF reader.

`MSK_CALLBACK_READ_OPF_SECTION`
: A chunk of Q non-zeros has been read from a problem file.

`MSK_CALLBACK_SOLVING_REMOTE`
: The callback function is called while the task is being solved on a remote server.

`MSK_CALLBACK_UPDATE_DUAL_BI`
: The callback function is called from within the basis identification procedure at an intermediate point in the dual phase.

`MSK_CALLBACK_UPDATE_DUAL_SIMPLEX`
: The callback function is called in the dual simplex optimizer.

`MSK_CALLBACK_UPDATE_DUAL_SIMPLEX_BI`
: The callback function is called from within the basis identification procedure at an intermediate point in the dual simplex clean-up phase. The frequency of the callbacks is controlled by the *MSK_IPAR_LOG_SIM_FREQ* parameter.

`MSK_CALLBACK_UPDATE_PRESOLVE`
: The callback function is called from within the presolve procedure.

`MSK_CALLBACK_UPDATE_PRIMAL_BI`
: The callback function is called from within the basis identification procedure at an intermediate point in the primal phase.

`MSK_CALLBACK_UPDATE_PRIMAL_SIMPLEX`
: The callback function is called in the primal simplex optimizer.

`MSK_CALLBACK_UPDATE_PRIMAL_SIMPLEX_BI`
The callback function is called from within the basis identification procedure at an intermediate point in the primal simplex clean-up phase. The frequency of the callbacks is controlled by the *MSK_IPAR_LOG_SIM_FREQ* parameter.

`MSK_CALLBACK_WRITE_OPF`
The callback function is called from the OPF writer.

13.4.14 Types of convexity checks.

`MSK_CHECK_CONVEXITY_NONE`
No convexity check.

`MSK_CHECK_CONVEXITY_SIMPLE`
Perform simple and fast convexity check.

`MSK_CHECK_CONVEXITY_FULL`
Perform a full convexity check.

13.4.15 Compression types

`MSK_COMPRESS_NONE`
No compression is used.

`MSK_COMPRESS_FREE`
The type of compression used is chosen automatically.

`MSK_COMPRESS_GZIP`
The type of compression used is gzip compatible.

13.4.16 Cone types

`MSK_CT_QUAD`
The cone is a quadratic cone.

`MSK_CT_RQUAD`
The cone is a rotated quadratic cone.

13.4.17 Name types

`MSK_NAME_TYPE_GEN`
General names. However, no duplicate and blank names are allowed.

`MSK_NAME_TYPE_MPS`
MPS type names.

`MSK_NAME_TYPE_LP`
LP type names.

13.4.18 Cone types

`MSK_SYMMAT_TYPE_SPARSE`
Sparse symmetric matrix.

13.4.19 Data format types

`MSK_DATA_FORMAT_EXTENSION`
The file extension is used to determine the data file format.

`MSK_DATA_FORMAT_MPS`
The data file is MPS formatted.

`MSK_DATA_FORMAT_LP`
The data file is LP formatted.

`MSK_DATA_FORMAT_OP`
The data file is an optimization problem formatted file.

`MSK_DATA_FORMAT_XML`
The data file is an XML formatted file.

`MSK_DATA_FORMAT_FREE_MPS`
The data a free MPS formatted file.

`MSK_DATA_FORMAT_TASK`
Generic task dump file.

`MSK_DATA_FORMAT_CB`
Conic benchmark format,

`MSK_DATA_FORMAT_JSON_TASK`
JSON based task format.

13.4.20 Double information items

`MSK_DINF_BI_CLEAN_DUAL_TIME`
Time spent within the dual clean-up optimizer of the basis identification procedure since its invocation.

`MSK_DINF_BI_CLEAN_PRIMAL_TIME`
Time spent within the primal clean-up optimizer of the basis identification procedure since its invocation.

`MSK_DINF_BI_CLEAN_TIME`
Time spent within the clean-up phase of the basis identification procedure since its invocation.

`MSK_DINF_BI_DUAL_TIME`
Time spent within the dual phase basis identification procedure since its invocation.

`MSK_DINF_BI_PRIMAL_TIME`
Time spent within the primal phase of the basis identification procedure since its invocation.

`MSK_DINF_BI_TIME`
Time spent within the basis identification procedure since its invocation.

`MSK_DINF_INTPNT_DUAL_FEAS`
Dual feasibility measure reported by the interior-point optimizer. (For the interior-point optimizer this measure is not directly related to the original problem because a homogeneous model is employed.)

`MSK_DINF_INTPNT_DUAL_OBJ`
Dual objective value reported by the interior-point optimizer.

`MSK_DINF_INTPNT_FACTOR_NUM_FLOPS`
An estimate of the number of flops used in the factorization.

`MSK_DINF_INTPNT_OPT_STATUS`
A measure of optimality of the solution. It should converge to $+1$ if the problem has a primal-dual optimal solution, and converge to -1 if the problem is (strictly) primal or dual infeasible. If the measure converges to another constant, or fails to settle, the problem is usually ill-posed.

`MSK_DINF_INTPNT_ORDER_TIME`
Order time (in seconds).

`MSK_DINF_INTPNT_PRIMAL_FEAS`
Primal feasibility measure reported by the interior-point optimizer. (For the interior-point optimizer this measure is not directly related to the original problem because a homogeneous model is employed).

`MSK_DINF_INTPNT_PRIMAL_OBJ`
Primal objective value reported by the interior-point optimizer.

`MSK_DINF_INTPNT_TIME`
Time spent within the interior-point optimizer since its invocation.

`MSK_DINF_MIO_CLIQUE_SEPARATION_TIME`
Seperation time for clique cuts.

`MSK_DINF_MIO_CMIR_SEPARATION_TIME`
Seperation time for CMIR cuts.

`MSK_DINF_MIO_CONSTRUCT_SOLUTION_OBJ`
If **MOSEK** has successfully constructed an integer feasible solution, then this item contains the optimal objective value corresponding to the feasible solution.

`MSK_DINF_MIO_DUAL_BOUND_AFTER_PRESOLVE`
Value of the dual bound after presolve but before cut generation.

`MSK_DINF_MIO_GMI_SEPARATION_TIME`
Seperation time for GMI cuts.

`MSK_DINF_MIO_HEURISTIC_TIME`
Total time spent in the optimizer.

`MSK_DINF_MIO_IMPLIED_BOUND_TIME`
Seperation time for implied bound cuts.

`MSK_DINF_MIO_KNAPSACK_COVER_SEPARATION_TIME`
Seperation time for knapsack cover.

`MSK_DINF_MIO_OBJ_ABS_GAP`
Given the mixed-integer optimizer has computed a feasible solution and a bound on the optimal objective value, then this item contains the absolute gap defined by

$$|(\text{objective value of feasible solution}) - (\text{objective bound})|.$$

Otherwise it has the value -1.0.

`MSK_DINF_MIO_OBJ_BOUND`
The best known bound on the objective function. This value is undefined until at least one relaxation has been solved: To see if this is the case check that *MSK_IINF_MIO_NUM_RELAX* is strictly positive.

`MSK_DINF_MIO_OBJ_INT`
The primal objective value corresponding to the best integer feasible solution. Please note that at least one integer feasible solution must have been located i.e. check *MSK_IINF_MIO_NUM_INT_SOLUTIONS*.

`MSK_DINF_MIO_OBJ_REL_GAP`
Given that the mixed-integer optimizer has computed a feasible solution and a bound on the optimal objective value, then this item contains the relative gap defined by

$$\frac{|(\text{objective value of feasible solution}) - (\text{objective bound})|}{\max(\delta, |(\text{objective value of feasible solution})|)}.$$

where δ is given by the parameter *MSK_DPAR_MIO_REL_GAP_CONST*. Otherwise it has the value -1.0.

`MSK_DINF_MIO_OPTIMIZER_TIME`
Total time spent in the optimizer.

`MSK_DINF_MIO_PROBING_TIME`
Total time for probing.

`MSK_DINF_MIO_ROOT_CUTGEN_TIME`
Total time for cut generation.

`MSK_DINF_MIO_ROOT_OPTIMIZER_TIME`
Time spent in the optimizer while solving the root relaxation.

`MSK_DINF_MIO_ROOT_PRESOLVE_TIME`
Time spent in while presolving the root relaxation.

`MSK_DINF_MIO_TIME`
Time spent in the mixed-integer optimizer.

`MSK_DINF_MIO_USER_OBJ_CUT`
If the objective cut is used, then this information item has the value of the cut.

`MSK_DINF_OPTIMIZER_TIME`
Total time spent in the optimizer since it was invoked.

`MSK_DINF_PRESOLVE_ELI_TIME`
Total time spent in the eliminator since the presolve was invoked.

`MSK_DINF_PRESOLVE_LINDEP_TIME`
Total time spent in the linear dependency checker since the presolve was invoked.

`MSK_DINF_PRESOLVE_TIME`
Total time (in seconds) spent in the presolve since it was invoked.

`MSK_DINF_PRIMAL_REPAIR_PENALTY_OBJ`
The optimal objective value of the penalty function.

`MSK_DINF_QCQO_REFORMULATE_MAX_PERTURBATION`
Maximum absolute diagonal perturbation occuring during the QCQO reformulation.

`MSK_DINF_QCQO_REFORMULATE_TIME`
Time spent with conic quadratic reformulation.

`MSK_DINF_QCQO_REFORMULATE_WORST_CHOLESKY_COLUMN_SCALING`
Worst Cholesky column scaling.

`MSK_DINF_QCQO_REFORMULATE_WORST_CHOLESKY_DIAG_SCALING`
Worst Cholesky diagonal scaling.

`MSK_DINF_RD_TIME`
Time spent reading the data file.

`MSK_DINF_SIM_DUAL_TIME`
Time spent in the dual simplex optimizer since invoking it.

`MSK_DINF_SIM_FEAS`
Feasibility measure reported by the simplex optimizer.

`MSK_DINF_SIM_OBJ`
Objective value reported by the simplex optimizer.

`MSK_DINF_SIM_PRIMAL_TIME`
Time spent in the primal simplex optimizer since invoking it.

`MSK_DINF_SIM_TIME`
Time spent in the simplex optimizer since invoking it.

`MSK_DINF_SOL_BAS_DUAL_OBJ`
Dual objective value of the basic solution.

MSK_DINF_SOL_BAS_DVIOLCON
: Maximal dual bound violation for x^c in the basic solution.

MSK_DINF_SOL_BAS_DVIOLVAR
: Maximal dual bound violation for x^x in the basic solution.

MSK_DINF_SOL_BAS_NRM_BARX
: Infinity norm of $\overline{X}$ in the basic solution.

MSK_DINF_SOL_BAS_NRM_SLC
: Infinity norm of s_l^c in the basic solution.

MSK_DINF_SOL_BAS_NRM_SLX
: Infinity norm of s_l^x in the basic solution.

MSK_DINF_SOL_BAS_NRM_SUC
: Infinity norm of s_u^c in the basic solution.

MSK_DINF_SOL_BAS_NRM_SUX
: Infinity norm of s_u^X in the basic solution.

MSK_DINF_SOL_BAS_NRM_XC
: Infinity norm of x^c in the basic solution.

MSK_DINF_SOL_BAS_NRM_XX
: Infinity norm of x^x in the basic solution.

MSK_DINF_SOL_BAS_NRM_Y
: Infinity norm of y in the basic solution.

MSK_DINF_SOL_BAS_PRIMAL_OBJ
: Primal objective value of the basic solution.

MSK_DINF_SOL_BAS_PVIOLCON
: Maximal primal bound violation for x^c in the basic solution.

MSK_DINF_SOL_BAS_PVIOLVAR
: Maximal primal bound violation for x^x in the basic solution.

MSK_DINF_SOL_ITG_NRM_BARX
: Infinity norm of $\overline{X}$ in the integer solution.

MSK_DINF_SOL_ITG_NRM_XC
: Infinity norm of x^c in the integer solution.

MSK_DINF_SOL_ITG_NRM_XX
: Infinity norm of x^x in the integer solution.

MSK_DINF_SOL_ITG_PRIMAL_OBJ
: Primal objective value of the integer solution.

MSK_DINF_SOL_ITG_PVIOLBARVAR
: Maximal primal bound violation for $\overline{X}$ in the integer solution.

MSK_DINF_SOL_ITG_PVIOLCON
: Maximal primal bound violation for x^c in the integer solution.

MSK_DINF_SOL_ITG_PVIOLCONES
: Maximal primal violation for primal conic constraints in the integer solution.

MSK_DINF_SOL_ITG_PVIOLITG
: Maximal violation for the integer constraints in the integer solution.

MSK_DINF_SOL_ITG_PVIOLVAR
: Maximal primal bound violation for x^x in the integer solution.

MSK_DINF_SOL_ITR_DUAL_OBJ
: Dual objective value of the interior-point solution.

`MSK_DINF_SOL_ITR_DVIOLBARVAR`
Maximal dual bound violation for $\overline{X}$ in the interior-point solution.

`MSK_DINF_SOL_ITR_DVIOLCON`
Maximal dual bound violation for x^c in the interior-point solution.

`MSK_DINF_SOL_ITR_DVIOLCONES`
Maximal dual violation for dual conic constraints in the interior-point solution.

`MSK_DINF_SOL_ITR_DVIOLVAR`
Maximal dual bound violation for x^x in the interior-point solution.

`MSK_DINF_SOL_ITR_NRM_BARS`
Infinity norm of $\overline{S}$ in the interior-point solution.

`MSK_DINF_SOL_ITR_NRM_BARX`
Infinity norm of $\overline{X}$ in the interior-point solution.

`MSK_DINF_SOL_ITR_NRM_SLC`
Infinity norm of s_l^c in the interior-point solution.

`MSK_DINF_SOL_ITR_NRM_SLX`
Infinity norm of s_l^x in the interior-point solution.

`MSK_DINF_SOL_ITR_NRM_SNX`
Infinity norm of s_n^x in the interior-point solution.

`MSK_DINF_SOL_ITR_NRM_SUC`
Infinity norm of s_u^c in the interior-point solution.

`MSK_DINF_SOL_ITR_NRM_SUX`
Infinity norm of s_u^X in the interior-point solution.

`MSK_DINF_SOL_ITR_NRM_XC`
Infinity norm of x^c in the interior-point solution.

`MSK_DINF_SOL_ITR_NRM_XX`
Infinity norm of x^x in the interior-point solution.

`MSK_DINF_SOL_ITR_NRM_Y`
Infinity norm of y in the interior-point solution.

`MSK_DINF_SOL_ITR_PRIMAL_OBJ`
Primal objective value of the interior-point solution.

`MSK_DINF_SOL_ITR_PVIOLBARVAR`
Maximal primal bound violation for $\overline{X}$ in the interior-point solution.

`MSK_DINF_SOL_ITR_PVIOLCON`
Maximal primal bound violation for x^c in the interior-point solution.

`MSK_DINF_SOL_ITR_PVIOLCONES`
Maximal primal violation for primal conic constraints in the interior-point solution.

`MSK_DINF_SOL_ITR_PVIOLVAR`
Maximal primal bound violation for x^x in the interior-point solution.

`MSK_DINF_TO_CONIC_TIME`
Time spent in the last to conic reformulation.

13.4.21 License feature

`MSK_FEATURE_PTS`
Base system.

`MSK_FEATURE_PTON`
Nonlinear extension.

13.4.22 Long integer information items.

`MSK_LIINF_BI_CLEAN_DUAL_DEG_ITER`
Number of dual degenerate clean iterations performed in the basis identification.

`MSK_LIINF_BI_CLEAN_DUAL_ITER`
Number of dual clean iterations performed in the basis identification.

`MSK_LIINF_BI_CLEAN_PRIMAL_DEG_ITER`
Number of primal degenerate clean iterations performed in the basis identification.

`MSK_LIINF_BI_CLEAN_PRIMAL_ITER`
Number of primal clean iterations performed in the basis identification.

`MSK_LIINF_BI_DUAL_ITER`
Number of dual pivots performed in the basis identification.

`MSK_LIINF_BI_PRIMAL_ITER`
Number of primal pivots performed in the basis identification.

`MSK_LIINF_INTPNT_FACTOR_NUM_NZ`
Number of non-zeros in factorization.

`MSK_LIINF_MIO_INTPNT_ITER`
Number of interior-point iterations performed by the mixed-integer optimizer.

`MSK_LIINF_MIO_PRESOLVED_ANZ`
Number of non-zero entries in the constraint matrix of presolved problem.

`MSK_LIINF_MIO_SIM_MAXITER_SETBACKS`
Number of times the the simplex optimizer has hit the maximum iteration limit when re-optimizing.

`MSK_LIINF_MIO_SIMPLEX_ITER`
Number of simplex iterations performed by the mixed-integer optimizer.

`MSK_LIINF_RD_NUMANZ`
Number of non-zeros in A that is read.

`MSK_LIINF_RD_NUMQNZ`
Number of Q non-zeros.

13.4.23 Integer information items.

`MSK_IINF_ANA_PRO_NUM_CON`
Number of constraints in the problem.

`MSK_IINF_ANA_PRO_NUM_CON_EQ`
Number of equality constraints.

`MSK_IINF_ANA_PRO_NUM_CON_FR`
Number of unbounded constraints.

`MSK_IINF_ANA_PRO_NUM_CON_LO`
Number of constraints with a lower bound and an infinite upper bound.

`MSK_IINF_ANA_PRO_NUM_CON_RA`
Number of constraints with finite lower and upper bounds.

`MSK_IINF_ANA_PRO_NUM_CON_UP`
Number of constraints with an upper bound and an infinite lower bound.

`MSK_IINF_ANA_PRO_NUM_VAR`
Number of variables in the problem.

`MSK_IINF_ANA_PRO_NUM_VAR_BIN`
Number of binary (0-1) variables.

`MSK_IINF_ANA_PRO_NUM_VAR_CONT`
Number of continuous variables.

`MSK_IINF_ANA_PRO_NUM_VAR_EQ`
Number of fixed variables.

`MSK_IINF_ANA_PRO_NUM_VAR_FR`
Number of free variables.

`MSK_IINF_ANA_PRO_NUM_VAR_INT`
Number of general integer variables.

`MSK_IINF_ANA_PRO_NUM_VAR_LO`
Number of variables with a lower bound and an infinite upper bound.

`MSK_IINF_ANA_PRO_NUM_VAR_RA`
Number of variables with finite lower and upper bounds.

`MSK_IINF_ANA_PRO_NUM_VAR_UP`
Number of variables with an upper bound and an infinite lower bound. This value is set by

`MSK_IINF_INTPNT_FACTOR_DIM_DENSE`
Dimension of the dense sub system in factorization.

`MSK_IINF_INTPNT_ITER`
Number of interior-point iterations since invoking the interior-point optimizer.

`MSK_IINF_INTPNT_NUM_THREADS`
Number of threads that the interior-point optimizer is using.

`MSK_IINF_INTPNT_SOLVE_DUAL`
Non-zero if the interior-point optimizer is solving the dual problem.

`MSK_IINF_MIO_ABSGAP_SATISFIED`
Non-zero if absolute gap is within tolerances.

`MSK_IINF_MIO_CLIQUE_TABLE_SIZE`
Size of the clique table.

`MSK_IINF_MIO_CONSTRUCT_NUM_ROUNDINGS`
Number of values in the integer solution that is rounded to an integer value.

`MSK_IINF_MIO_CONSTRUCT_SOLUTION`
If this item has the value 0, then **MOSEK** did not try to construct an initial integer feasible solution. If the item has a positive value, then **MOSEK** successfully constructed an initial integer feasible solution.

`MSK_IINF_MIO_INITIAL_SOLUTION`
Is non-zero if an initial integer solution is specified.

`MSK_IINF_MIO_NEAR_ABSGAP_SATISFIED`
Non-zero if absolute gap is within relaxed tolerances.

`MSK_IINF_MIO_NEAR_RELGAP_SATISFIED`
Non-zero if relative gap is within relaxed tolerances.

`MSK_IINF_MIO_NODE_DEPTH`
Depth of the last node solved.

`MSK_IINF_MIO_NUM_ACTIVE_NODES`
Number of active branch bound nodes.

`MSK_IINF_MIO_NUM_BRANCH`
Number of branches performed during the optimization.

`MSK_IINF_MIO_NUM_CLIQUE_CUTS`
Number of clique cuts.

`MSK_IINF_MIO_NUM_CMIR_CUTS`
Number of Complemented Mixed Integer Rounding (CMIR) cuts.

`MSK_IINF_MIO_NUM_GOMORY_CUTS`
Number of Gomory cuts.

`MSK_IINF_MIO_NUM_IMPLIED_BOUND_CUTS`
Number of implied bound cuts.

`MSK_IINF_MIO_NUM_INT_SOLUTIONS`
Number of integer feasible solutions that has been found.

`MSK_IINF_MIO_NUM_KNAPSACK_COVER_CUTS`
Number of clique cuts.

`MSK_IINF_MIO_NUM_RELAX`
Number of relaxations solved during the optimization.

`MSK_IINF_MIO_NUM_REPEATED_PRESOLVE`
Number of times presolve was repeated at root.

`MSK_IINF_MIO_NUMCON`
Number of constraints in the problem solved by the mixed-integer optimizer.

`MSK_IINF_MIO_NUMINT`
Number of integer variables in the problem solved be the mixed-integer optimizer.

`MSK_IINF_MIO_NUMVAR`
Number of variables in the problem solved by the mixed-integer optimizer.

`MSK_IINF_MIO_OBJ_BOUND_DEFINED`
Non-zero if a valid objective bound has been found, otherwise zero.

`MSK_IINF_MIO_PRESOLVED_NUMBIN`
Number of binary variables in the problem solved be the mixed-integer optimizer.

`MSK_IINF_MIO_PRESOLVED_NUMCON`
Number of constraints in the presolved problem.

`MSK_IINF_MIO_PRESOLVED_NUMCONT`
Number of continuous variables in the problem solved be the mixed-integer optimizer.

`MSK_IINF_MIO_PRESOLVED_NUMINT`
Number of integer variables in the presolved problem.

`MSK_IINF_MIO_PRESOLVED_NUMVAR`
Number of variables in the presolved problem.

`MSK_IINF_MIO_RELGAP_SATISFIED`
Non-zero if relative gap is within tolerances.

`MSK_IINF_MIO_TOTAL_NUM_CUTS`
Total number of cuts generated by the mixed-integer optimizer.

`MSK_IINF_MIO_USER_OBJ_CUT`
If it is non-zero, then the objective cut is used.

`MSK_IINF_OPT_NUMCON`
Number of constraints in the problem solved when the optimizer is called.

`MSK_IINF_OPT_NUMVAR`
Number of variables in the problem solved when the optimizer is called

`MSK_IINF_OPTIMIZE_RESPONSE`
The response code returned by optimize.

`MSK_IINF_RD_NUMBARVAR`
Number of variables read.

`MSK_IINF_RD_NUMCON`
Number of constraints read.

`MSK_IINF_RD_NUMCONE`
Number of conic constraints read.

`MSK_IINF_RD_NUMINTVAR`
Number of integer-constrained variables read.

`MSK_IINF_RD_NUMQ`
Number of nonempty Q matrices read.

`MSK_IINF_RD_NUMVAR`
Number of variables read.

`MSK_IINF_RD_PROTYPE`
Problem type.

`MSK_IINF_SIM_DUAL_DEG_ITER`
The number of dual degenerate iterations.

`MSK_IINF_SIM_DUAL_HOTSTART`
If 1 then the dual simplex algorithm is solving from an advanced basis.

`MSK_IINF_SIM_DUAL_HOTSTART_LU`
If 1 then a valid basis factorization of full rank was located and used by the dual simplex algorithm.

`MSK_IINF_SIM_DUAL_INF_ITER`
The number of iterations taken with dual infeasibility.

`MSK_IINF_SIM_DUAL_ITER`
Number of dual simplex iterations during the last optimization.

`MSK_IINF_SIM_NUMCON`
Number of constraints in the problem solved by the simplex optimizer.

`MSK_IINF_SIM_NUMVAR`
Number of variables in the problem solved by the simplex optimizer.

`MSK_IINF_SIM_PRIMAL_DEG_ITER`
The number of primal degenerate iterations.

`MSK_IINF_SIM_PRIMAL_HOTSTART`
If 1 then the primal simplex algorithm is solving from an advanced basis.

`MSK_IINF_SIM_PRIMAL_HOTSTART_LU`
If 1 then a valid basis factorization of full rank was located and used by the primal simplex algorithm.

`MSK_IINF_SIM_PRIMAL_INF_ITER`
The number of iterations taken with primal infeasibility.

`MSK_IINF_SIM_PRIMAL_ITER`
Number of primal simplex iterations during the last optimization.

`MSK_IINF_SIM_SOLVE_DUAL`
Is non-zero if dual problem is solved.

`MSK_IINF_SOL_BAS_PROSTA`
Problem status of the basic solution. Updated after each optimization.

`MSK_IINF_SOL_BAS_SOLSTA`
Solution status of the basic solution. Updated after each optimization.

`MSK_IINF_SOL_ITG_PROSTA`
Problem status of the integer solution. Updated after each optimization.

`MSK_IINF_SOL_ITG_SOLSTA`
Solution status of the integer solution. Updated after each optimization.

`MSK_IINF_SOL_ITR_PROSTA`
: Problem status of the interior-point solution. Updated after each optimization.

`MSK_IINF_SOL_ITR_SOLSTA`
: Solution status of the interior-point solution. Updated after each optimization.

`MSK_IINF_STO_NUM_A_REALLOC`
: Number of times the storage for storing A has been changed. A large value may indicates that memory fragmentation may occur.

13.4.24 Information item types

`MSK_INF_DOU_TYPE`
: Is a double information type.

`MSK_INF_INT_TYPE`
: Is an integer.

`MSK_INF_LINT_TYPE`
: Is a long integer.

13.4.25 Input/output modes

`MSK_IOMODE_READ`
: The file is read-only.

`MSK_IOMODE_WRITE`
: The file is write-only. If the file exists then it is truncated when it is opened. Otherwise it is created when it is opened.

`MSK_IOMODE_READWRITE`
: The file is to read and written.

13.4.26 Specifies the branching direction.

`MSK_BRANCH_DIR_FREE`
: The mixed-integer optimizer decides which branch to choose.

`MSK_BRANCH_DIR_UP`
: The mixed-integer optimizer always chooses the up branch first.

`MSK_BRANCH_DIR_DOWN`
: The mixed-integer optimizer always chooses the down branch first.

`MSK_BRANCH_DIR_NEAR`
: Branch in direction nearest to selected fractional variable.

`MSK_BRANCH_DIR_FAR`
: Branch in direction farthest from selected fractional variable.

`MSK_BRANCH_DIR_ROOT_LP`
: Chose direction based on root lp value of selected variable.

`MSK_BRANCH_DIR_GUIDED`
: Branch in direction of current incumbent.

`MSK_BRANCH_DIR_PSEUDOCOST`
: Branch based on the pseudocost of the variable.

13.4.27 Continuous mixed-integer solution type

`MSK_MIO_CONT_SOL_NONE`
No interior-point or basic solution are reported when the mixed-integer optimizer is used.

`MSK_MIO_CONT_SOL_ROOT`
The reported interior-point and basic solutions are a solution to the root node problem when mixed-integer optimizer is used.

`MSK_MIO_CONT_SOL_ITG`
The reported interior-point and basic solutions are a solution to the problem with all integer variables fixed at the value they have in the integer solution. A solution is only reported in case the problem has a primal feasible solution.

`MSK_MIO_CONT_SOL_ITG_REL`
In case the problem is primal feasible then the reported interior-point and basic solutions are a solution to the problem with all integer variables fixed at the value they have in the integer solution. If the problem is primal infeasible, then the solution to the root node problem is reported.

13.4.28 Integer restrictions

`MSK_MIO_MODE_IGNORED`
The integer constraints are ignored and the problem is solved as a continuous problem.

`MSK_MIO_MODE_SATISFIED`
Integer restrictions should be satisfied.

13.4.29 Mixed-integer node selection types

`MSK_MIO_NODE_SELECTION_FREE`
The optimizer decides the node selection strategy.

`MSK_MIO_NODE_SELECTION_FIRST`
The optimizer employs a depth first node selection strategy.

`MSK_MIO_NODE_SELECTION_BEST`
The optimizer employs a best bound node selection strategy.

`MSK_MIO_NODE_SELECTION_WORST`
The optimizer employs a worst bound node selection strategy.

`MSK_MIO_NODE_SELECTION_HYBRID`
The optimizer employs a hybrid strategy.

`MSK_MIO_NODE_SELECTION_PSEUDO`
The optimizer employs selects the node based on a pseudo cost estimate.

13.4.30 MPS file format type

`MSK_MPS_FORMAT_STRICT`
It is assumed that the input file satisfies the MPS format strictly.

`MSK_MPS_FORMAT_RELAXED`
It is assumed that the input file satisfies a slightly relaxed version of the MPS format.

`MSK_MPS_FORMAT_FREE`
It is assumed that the input file satisfies the free MPS format. This implies that spaces are not allowed in names. Otherwise the format is free.

`MSK_MPS_FORMAT_CPLEX`
The CPLEX compatible version of the MPS format is employed.

13.4.31 Objective sense types

`MSK_OBJECTIVE_SENSE_MINIMIZE`
The problem should be minimized.

`MSK_OBJECTIVE_SENSE_MAXIMIZE`
The problem should be maximized.

13.4.32 On/off

`MSK_ON`
Switch the option on.

`MSK_OFF`
Switch the option off.

13.4.33 Optimizer types

`MSK_OPTIMIZER_CONIC`
The optimizer for problems having conic constraints.

`MSK_OPTIMIZER_DUAL_SIMPLEX`
The dual simplex optimizer is used.

`MSK_OPTIMIZER_FREE`
The optimizer is chosen automatically.

`MSK_OPTIMIZER_FREE_SIMPLEX`
One of the simplex optimizers is used.

`MSK_OPTIMIZER_INTPNT`
The interior-point optimizer is used.

`MSK_OPTIMIZER_MIXED_INT`
The mixed-integer optimizer.

`MSK_OPTIMIZER_PRIMAL_SIMPLEX`
The primal simplex optimizer is used.

13.4.34 Ordering strategies

`MSK_ORDER_METHOD_FREE`
The ordering method is chosen automatically.

`MSK_ORDER_METHOD_APPMINLOC`
Approximate minimum local fill-in ordering is employed.

`MSK_ORDER_METHOD_EXPERIMENTAL`
This option should not be used.

`MSK_ORDER_METHOD_TRY_GRAPHPAR`
Always try the graph partitioning based ordering.

`MSK_ORDER_METHOD_FORCE_GRAPHPAR`
Always use the graph partitioning based ordering even if it is worse than the approximate minimum local fill ordering.

`MSK_ORDER_METHOD_NONE`
No ordering is used.

13.4.35 Presolve method.

`MSK_PRESOLVE_MODE_OFF`
The problem is not presolved before it is optimized.

`MSK_PRESOLVE_MODE_ON`
The problem is presolved before it is optimized.

`MSK_PRESOLVE_MODE_FREE`
It is decided automatically whether to presolve before the problem is optimized.

13.4.36 Parameter type

`MSK_PAR_INVALID_TYPE`
Not a valid parameter.

`MSK_PAR_DOU_TYPE`
Is a double parameter.

`MSK_PAR_INT_TYPE`
Is an integer parameter.

`MSK_PAR_STR_TYPE`
Is a string parameter.

13.4.37 Problem data items

`MSK_PI_VAR`
Item is a variable.

`MSK_PI_CON`
Item is a constraint.

`MSK_PI_CONE`
Item is a cone.

13.4.38 Problem types

`MSK_PROBTYPE_LO`
The problem is a linear optimization problem.

`MSK_PROBTYPE_QO`
The problem is a quadratic optimization problem.

`MSK_PROBTYPE_QCQO`
The problem is a quadratically constrained optimization problem.

`MSK_PROBTYPE_GECO`
General convex optimization.

`MSK_PROBTYPE_CONIC`
A conic optimization.

`MSK_PROBTYPE_MIXED`
General nonlinear constraints and conic constraints. This combination can not be solved by **MOSEK**.

13.4.39 Problem status keys

`MSK_PRO_STA_UNKNOWN`
Unknown problem status.

`MSK_PRO_STA_PRIM_AND_DUAL_FEAS`
The problem is primal and dual feasible.

`MSK_PRO_STA_PRIM_FEAS`
The problem is primal feasible.

`MSK_PRO_STA_DUAL_FEAS`
The problem is dual feasible.

`MSK_PRO_STA_NEAR_PRIM_AND_DUAL_FEAS`
The problem is at least nearly primal and dual feasible.

`MSK_PRO_STA_NEAR_PRIM_FEAS`
The problem is at least nearly primal feasible.

`MSK_PRO_STA_NEAR_DUAL_FEAS`
The problem is at least nearly dual feasible.

`MSK_PRO_STA_PRIM_INFEAS`
The problem is primal infeasible.

`MSK_PRO_STA_DUAL_INFEAS`
The problem is dual infeasible.

`MSK_PRO_STA_PRIM_AND_DUAL_INFEAS`
The problem is primal and dual infeasible.

`MSK_PRO_STA_ILL_POSED`
The problem is ill-posed. For example, it may be primal and dual feasible but have a positive duality gap.

`MSK_PRO_STA_PRIM_INFEAS_OR_UNBOUNDED`
The problem is either primal infeasible or unbounded. This may occur for mixed-integer problems.

13.4.40 XML writer output mode

`MSK_WRITE_XML_MODE_ROW`
Write in row order.

`MSK_WRITE_XML_MODE_COL`
Write in column order.

13.4.41 Response code type

`MSK_RESPONSE_OK`
The response code is OK.

`MSK_RESPONSE_WRN`
The response code is a warning.

`MSK_RESPONSE_TRM`
The response code is an optimizer termination status.

`MSK_RESPONSE_ERR`
The response code is an error.

`MSK_RESPONSE_UNK`
The response code does not belong to any class.

13.4.42 Scaling type

`MSK_SCALING_FREE`
The optimizer chooses the scaling heuristic.

`MSK_SCALING_NONE`
No scaling is performed.

`MSK_SCALING_MODERATE`
A conservative scaling is performed.

`MSK_SCALING_AGGRESSIVE`
A very aggressive scaling is performed.

13.4.43 Scaling method

`MSK_SCALING_METHOD_POW2`
Scales only with power of 2 leaving the mantissa untouched.

`MSK_SCALING_METHOD_FREE`
The optimizer chooses the scaling heuristic.

13.4.44 Sensitivity types

`MSK_SENSITIVITY_TYPE_BASIS`
Basis sensitivity analysis is performed.

`MSK_SENSITIVITY_TYPE_OPTIMAL_PARTITION`
Optimal partition sensitivity analysis is performed.

13.4.45 Simplex selection strategy

`MSK_SIM_SELECTION_FREE`
The optimizer chooses the pricing strategy.

`MSK_SIM_SELECTION_FULL`
The optimizer uses full pricing.

`MSK_SIM_SELECTION_ASE`
The optimizer uses approximate steepest-edge pricing.

`MSK_SIM_SELECTION_DEVEX`
The optimizer uses devex steepest-edge pricing (or if it is not available an approximate steep-edge selection).

`MSK_SIM_SELECTION_SE`
The optimizer uses steepest-edge selection (or if it is not available an approximate steep-edge selection).

`MSK_SIM_SELECTION_PARTIAL`
The optimizer uses a partial selection approach. The approach is usually beneficial if the number of variables is much larger than the number of constraints.

13.4.46 Solution items

`MSK_SOL_ITEM_XC`
Solution for the constraints.

`MSK_SOL_ITEM_XX`
Variable solution.

`MSK_SOL_ITEM_Y`
: Lagrange multipliers for equations.

`MSK_SOL_ITEM_SLC`
: Lagrange multipliers for lower bounds on the constraints.

`MSK_SOL_ITEM_SUC`
: Lagrange multipliers for upper bounds on the constraints.

`MSK_SOL_ITEM_SLX`
: Lagrange multipliers for lower bounds on the variables.

`MSK_SOL_ITEM_SUX`
: Lagrange multipliers for upper bounds on the variables.

`MSK_SOL_ITEM_SNX`
: Lagrange multipliers corresponding to the conic constraints on the variables.

13.4.47 Solution status keys

`MSK_SOL_STA_UNKNOWN`
: Status of the solution is unknown.

`MSK_SOL_STA_OPTIMAL`
: The solution is optimal.

`MSK_SOL_STA_PRIM_FEAS`
: The solution is primal feasible.

`MSK_SOL_STA_DUAL_FEAS`
: The solution is dual feasible.

`MSK_SOL_STA_PRIM_AND_DUAL_FEAS`
: The solution is both primal and dual feasible.

`MSK_SOL_STA_NEAR_OPTIMAL`
: The solution is nearly optimal.

`MSK_SOL_STA_NEAR_PRIM_FEAS`
: The solution is nearly primal feasible.

`MSK_SOL_STA_NEAR_DUAL_FEAS`
: The solution is nearly dual feasible.

`MSK_SOL_STA_NEAR_PRIM_AND_DUAL_FEAS`
: The solution is nearly both primal and dual feasible.

`MSK_SOL_STA_PRIM_INFEAS_CER`
: The solution is a certificate of primal infeasibility.

`MSK_SOL_STA_DUAL_INFEAS_CER`
: The solution is a certificate of dual infeasibility.

`MSK_SOL_STA_NEAR_PRIM_INFEAS_CER`
: The solution is almost a certificate of primal infeasibility.

`MSK_SOL_STA_NEAR_DUAL_INFEAS_CER`
: The solution is almost a certificate of dual infeasibility.

`MSK_SOL_STA_PRIM_ILLPOSED_CER`
: The solution is a certificate that the primal problem is illposed.

`MSK_SOL_STA_DUAL_ILLPOSED_CER`
: The solution is a certificate that the dual problem is illposed.

`MSK_SOL_STA_INTEGER_OPTIMAL`
: The primal solution is integer optimal.

`MSK_SOL_STA_NEAR_INTEGER_OPTIMAL`
The primal solution is near integer optimal.

13.4.48 Solution types

`MSK_SOL_BAS`
The basic solution.

`MSK_SOL_ITR`
The interior solution.

`MSK_SOL_ITG`
The integer solution.

13.4.49 Solve primal or dual form

`MSK_SOLVE_FREE`
The optimizer is free to solve either the primal or the dual problem.

`MSK_SOLVE_PRIMAL`
The optimizer should solve the primal problem.

`MSK_SOLVE_DUAL`
The optimizer should solve the dual problem.

13.4.50 Status keys

`MSK_SK_UNK`
The status for the constraint or variable is unknown.

`MSK_SK_BAS`
The constraint or variable is in the basis.

`MSK_SK_SUPBAS`
The constraint or variable is super basic.

`MSK_SK_LOW`
The constraint or variable is at its lower bound.

`MSK_SK_UPR`
The constraint or variable is at its upper bound.

`MSK_SK_FIX`
The constraint or variable is fixed.

`MSK_SK_INF`
The constraint or variable is infeasible in the bounds.

13.4.51 Starting point types

`MSK_STARTING_POINT_FREE`
The starting point is chosen automatically.

`MSK_STARTING_POINT_GUESS`
The optimizer guesses a starting point.

`MSK_STARTING_POINT_CONSTANT`
The optimizer constructs a starting point by assigning a constant value to all primal and dual variables. This starting point is normally robust.

`MSK_STARTING_POINT_SATISFY_BOUNDS`
: The starting point is chosen to satisfy all the simple bounds on nonlinear variables. If this starting point is employed, then more care than usual should employed when choosing the bounds on the nonlinear variables. In particular very tight bounds should be avoided.

13.4.52 Stream types

`MSK_STREAM_LOG`
: Log stream. Contains the aggregated contents of all other streams. This means that a message written to any other stream will also be written to this stream.

`MSK_STREAM_MSG`
: Message stream. Log information relating to performance and progress of the optimization is written to this stream.

`MSK_STREAM_ERR`
: Error stream. Error messages are written to this stream.

`MSK_STREAM_WRN`
: Warning stream. Warning messages are written to this stream.

13.4.53 Integer values

`MSK_MAX_STR_LEN`
: Maximum string length allowed in **MOSEK**.

`MSK_LICENSE_BUFFER_LENGTH`
: The length of a license key buffer.

13.4.54 Variable types

`MSK_VAR_TYPE_CONT`
: Is a continuous variable.

`MSK_VAR_TYPE_INT`
: Is an integer variable.

CHAPTER

FOURTEEN

SUPPORTED FILE FORMATS

MOSEK supports a range of problem and solution formats listed in Table 14.1 and Table 14.2. The **Task format** is **MOSEK**'s native binary format and it supports all features that **MOSEK** supports. The **OPF format** is **MOSEK**'s human-readable alternative that supports nearly all features (everything except semidefinite problems). In general, text formats are significantly slower to read, but can be examined and edited directly in any text editor.

Problem formats

See Table 14.1.

Table 14.1: List of supported file formats for optimization problems.

Format Type	Ext.	Binary/Text	LP	QO	CQO	SDP
LP	lp	plain text	X	X		
MPS	mps	plain text	X	X		
OPF	opf	plain text	X	X	X	
CBF	cbf	plain text	X		X	X
OSiL	xml	xml text	X	X		
Task format	task	binary	X	X	X	X
Jtask format	jtask	text	X	X	X	X

Solution formats

See Table 14.2.

Table 14.2: List of supported solution formats.

Format Type	Ext.	Binary/Text	Description
SOL	sol	plain text	Interior Solution
	bas	plain text	Basic Solution
	int	plain text	Integer
Jsol format	jsol	text	Solution

Compression

MOSEK supports GZIP compression of files. Problem files with an additional `.gz` extension are assumed to be compressed when read, and are automatically compressed when written. For example, a file called

```
problem.mps.gz
```

will be considered as a GZIP compressed MPS file.

14.1 The LP File Format

MOSEK supports the LP file format with some extensions. The LP format is not a completely well-defined standard and hence different optimization packages may interpret the same LP file in slightly different ways. **MOSEK** tries to emulate as closely as possible CPLEX's behavior, but tries to stay backward compatible.

The LP file format can specify problems on the form

$$\begin{array}{lccccc} \text{minimize/maximize} & & & c^T x + \frac{1}{2} q^o(x) & & \\ \text{subject to} & l^c & \leq & Ax + \frac{1}{2} q(x) & \leq & u^c, \\ & l^x & \leq & x & \leq & u^x, \\ & & & x_{\mathcal{J}} \text{ integer}, & & \end{array}$$

where

- $x \in \mathbb{R}^n$ is the vector of decision variables.
- $c \in \mathbb{R}^n$ is the linear term in the objective.
- $q^o :\in \mathbb{R}^n \to \mathbb{R}$ is the quadratic term in the objective where

$$q^o(x) = x^T Q^o x$$

and it is assumed that

$$Q^o = (Q^o)^T.$$

- $A \in \mathbb{R}^{m \times n}$ is the constraint matrix.
- $l^c \in \mathbb{R}^m$ is the lower limit on the activity for the constraints.
- $u^c \in \mathbb{R}^m$ is the upper limit on the activity for the constraints.
- $l^x \in \mathbb{R}^n$ is the lower limit on the activity for the variables.
- $u^x \in \mathbb{R}^n$ is the upper limit on the activity for the variables.
- $q : \mathbb{R}^n \to \mathbb{R}$ is a vector of quadratic functions. Hence,

$$q_i(x) = x^T Q^i x$$

where it is assumed that

$$Q^i = (Q^i)^T.$$

- $\mathcal{J} \subseteq \{1, 2, \ldots, n\}$ is an index set of the integer constrained variables.

14.1.1 File Sections

An LP formatted file contains a number of sections specifying the objective, constraints, variable bounds, and variable types. The section keywords may be any mix of upper and lower case letters.

Objective Function

The first section beginning with one of the keywords

```
max
maximum
maximize
min
minimum
minimize
```

defines the objective sense and the objective function, i.e.

$$c^T x + \frac{1}{2} x^T Q^o x.$$

The objective may be given a name by writing

```
myname:
```

before the expressions. If no name is given, then the objective is named `obj`.

The objective function contains linear and quadratic terms. The linear terms are written as:

```
4 x1 + x2 - 0.1 x3
```

and so forth. The quadratic terms are written in square brackets (`[ ]`) and are either squared or multiplied as in the examples

```
x1^2
```

and

```
x1 * x2
```

There may be zero or more pairs of brackets containing quadratic expressions.

An example of an objective section is

```
minimize
myobj: 4 x1 + x2 - 0.1 x3 + [ x1^2 + 2.1 x1 * x2 ]/2
```

Please note that the quadratic expressions are multiplied with $\frac{1}{2}$, so that the above expression means

$$\text{minimize} \quad 4x_1 + x_2 - 0.1 \cdot x_3 + \tfrac{1}{2}(x_1^2 + 2.1 \cdot x_1 \cdot x_2)$$

If the same variable occurs more than once in the linear part, the coefficients are added, so that `4 x1 + 2 x1` is equivalent to `6 x1`. In the quadratic expressions `x1 * x2` is equivalent to `x2 * x1` and, as in the linear part, if the same variables multiplied or squared occur several times their coefficients are added.

Constraints

The second section beginning with one of the keywords

```
subj to
subject to
s.t.
st
```

defines the linear constraint matrix A and the quadratic matrices Q^i.

A constraint contains a name (optional), expressions adhering to the same rules as in the objective and a bound:

```
subject to
con1: x1 + x2 + [ x3^2 ]/2 <= 5.1
```

The bound type (here `<=`) may be any of `<`, `<=`, `=`, `>`, `>=` (`<` and `<=` mean the same), and the bound may be any number.

In the standard LP format it is not possible to define more than one bound, but **MOSEK** supports defining ranged constraints by using double-colon (`::`) instead of a single-colon (`:`) after the constraint name, i.e.

$$-5 \leq x_1 + x_2 \leq 5 \tag{14.1}$$

may be written as

```
con:: -5 < x_1 + x_2 < 5
```

By default **MOSEK** writes ranged constraints this way.

If the files must adhere to the LP standard, ranged constraints must either be split into upper bounded and lower bounded constraints or be written as an equality with a slack variable. For example the expression (14.1) may be written as

$$x_1 + x_2 - sl_1 = 0, \ -5 \leq sl_1 \leq 5.$$

Bounds

Bounds on the variables can be specified in the bound section beginning with one of the keywords

```
bound
bounds
```

The bounds section is optional but should, if present, follow the `subject to` section. All variables listed in the bounds section must occur in either the objective or a constraint.

The default lower and upper bounds are 0 and $+\infty$. A variable may be declared free with the keyword `free`, which means that the lower bound is $-\infty$ and the upper bound is $+\infty$. Furthermore it may be assigned a finite lower and upper bound. The bound definitions for a given variable may be written in one or two lines, and bounds can be any number or $\pm\infty$ (written as `+inf`/`-inf`/`+infinity`/`-infinity`) as in the example

```
bounds
x1 free
x2 <= 5
0.1 <= x2
x3 = 42
2 <= x4 < +inf
```

Variable Types

The final two sections are optional and must begin with one of the keywords

```
bin
binaries
binary
```

and

```
gen
general
```

Under `general` all integer variables are listed, and under `binary` all binary (integer variables with bounds 0 and 1) are listed:

```
general
x1 x2
binary
x3 x4
```

Again, all variables listed in the binary or general sections must occur in either the objective or a constraint.

Terminating Section

Finally, an LP formatted file must be terminated with the keyword

```
end
```

14.1.2 LP File Examples

Linear example `lo1.lp`

```
\ File: lo1.lp
maximize
obj: 3 x1 + x2 + 5 x3 + x4
subject to
c1:  3 x1 + x2 + 2 x3 = 30
c2:  2 x1 + x2 + 3 x3 + x4 >= 15
c3:  2 x2 + 3 x4 <= 25
bounds
 0 <= x1 <= +infinity
 0 <= x2 <= 10
 0 <= x3 <= +infinity
 0 <= x4 <= +infinity
end
```

Mixed integer example `milo1.lp`

```
maximize
obj: x1 + 6.4e-01 x2
subject to
c1:  5e+01 x1 + 3.1e+01 x2 <= 2.5e+02
c2:  3e+00 x1 - 2e+00 x2 >= -4e+00
bounds
 0 <= x1 <= +infinity
 0 <= x2 <= +infinity
general
 x1 x2
end
```

14.1.3 LP Format peculiarities

Comments

Anything on a line after a \ is ignored and is treated as a comment.

Names

A name for an objective, a constraint or a variable may contain the letters *a-z*, *A-Z*, the digits *0-9* and the characters

```
!"#$%&()/,.;?@_'`|~
```

The first character in a name must not be a number, a period or the letter `e` or `E`. Keywords must not be used as names.

MOSEK accepts any character as valid for names, except `\0`. A name that is not allowed in LP file will be changed and a warning will be issued.

The algorithm for making names LP valid works as follows: The name is interpreted as an `utf-8` string. For a unicode character `c`:

- If `c==_` (underscore), the output is `__` (two underscores).
- If `c` is a valid LP name character, the output is just `c`.
- If `c` is another character in the ASCII range, the output is `_XX`, where `XX` is the hexadecimal code for the character.
- If `c` is a character in the range *127-65535*, the output is `_uXXXX`, where `XXXX` is the hexadecimal code for the character.
- If `c` is a character above 65535, the output is `_UXXXXXXXX`, where `XXXXXXXX` is the hexadecimal code for the character.

Invalid `utf-8` substrings are escaped as `_XX'`, and if a name starts with a period, *e* or *E*, that character is escaped as `_XX`.

Variable Bounds

Specifying several upper or lower bounds on one variable is possible but **MOSEK** uses only the tightest bounds. If a variable is fixed (with `=`), then it is considered the tightest bound.

MOSEK Extensions to the LP Format

Some optimization software packages employ a more strict definition of the LP format than the one used by **MOSEK**. The limitations imposed by the strict LP format are the following:

- Quadratic terms in the constraints are not allowed.
- Names can be only 16 characters long.
- Lines must not exceed 255 characters in length.

If an LP formatted file created by **MOSEK** should satisfy the strict definition, then the parameter

- *MSK_IPAR_WRITE_LP_STRICT_FORMAT*

should be set; note, however, that some problems cannot be written correctly as a strict LP formatted file. For instance, all names are truncated to 16 characters and hence they may loose their uniqueness and change the problem.

To get around some of the inconveniences converting from other problem formats, **MOSEK** allows lines to contain 1024 characters and names may have any length (shorter than the 1024 characters).

Internally in **MOSEK** names may contain any (printable) character, many of which cannot be used in LP names. Setting the parameters

- *MSK_IPAR_READ_LP_QUOTED_NAMES* and
- *MSK_IPAR_WRITE_LP_QUOTED_NAMES*

allows **MOSEK** to use quoted names. The first parameter tells **MOSEK** to remove quotes from quoted names e.g, `"x1"`, when reading LP formatted files. The second parameter tells **MOSEK** to put quotes around any semi-illegal name (names beginning with a number or a period) and fully illegal name (containing illegal characters). As double quote is a legal character in the LP format, quoting semi-illegal names makes them legal in the pure LP format as long as they are still shorter than 16 characters. Fully illegal names are still illegal in a pure LP file.

14.1.4 The strict LP format

The LP format is not a formal standard and different vendors have slightly different interpretations of the LP format. To make **MOSEK**'s definition of the LP format more compatible with the definitions of other vendors, use the parameter setting

- *MSK_IPAR_WRITE_LP_STRICT_FORMAT* = *MSK_ON*

This setting may lead to truncation of some names and hence to an invalid LP file. The simple solution to this problem is to use the parameter setting

- *MSK_IPAR_WRITE_GENERIC_NAMES* = *MSK_ON*

which will cause all names to be renamed systematically in the output file.

14.1.5 Formatting of an LP File

A few parameters control the visual formatting of LP files written by **MOSEK** in order to make it easier to read the files. These parameters are

- *MSK_IPAR_WRITE_LP_LINE_WIDTH*
- *MSK_IPAR_WRITE_LP_TERMS_PER_LINE*

The first parameter sets the maximum number of characters on a single line. The default value is 80 corresponding roughly to the width of a standard text document.

The second parameter sets the maximum number of terms per line; a term means a sign, a coefficient, and a name (for example `+ 42 elephants`). The default value is 0, meaning that there is no maximum.

Unnamed Constraints

Reading and writing an LP file with **MOSEK** may change it superficially. If an LP file contains unnamed constraints or objective these are given their generic names when the file is read (however unnamed constraints in **MOSEK** are written without names).

14.2 The MPS File Format

MOSEK supports the standard MPS format with some extensions. For a detailed description of the MPS format see the book by Nazareth *[Naz87]*.

14.2.1 MPS File Structure

The version of the MPS format supported by **MOSEK** allows specification of an optimization problem of the form

$$\begin{array}{rcccl} l^c & \leq & Ax + q(x) & \leq & u^c, \\ l^x & \leq & x & \leq & u^x, \\ & & x \in \mathcal{K}, & & \\ & & x_{\mathcal{J}} \ \text{integer}, & & \end{array} \tag{14.2}$$

where

- $x \in \mathbb{R}^n$ is the vector of decision variables.
- $A \in \mathbb{R}^{m \times n}$ is the constraint matrix.
- $l^c \in \mathbb{R}^m$ is the lower limit on the activity for the constraints.
- $u^c \in \mathbb{R}^m$ is the upper limit on the activity for the constraints.
- $l^x \in \mathbb{R}^n$ is the lower limit on the activity for the variables.
- $u^x \in \mathbb{R}^n$ is the upper limit on the activity for the variables.
- $q : \mathbb{R}^n \to \mathbb{R}$ is a vector of quadratic functions. Hence,

$$q_i(x) = \frac{1}{2} x^T Q^i x$$

where it is assumed that

$$Q^i = (Q^i)^T.$$

Please note the explicit $\frac{1}{2}$ in the quadratic term and that Q^i is required to be symmetric.

- $\mathcal{K}$ is a convex cone.
- $\mathcal{J} \subseteq \{1, 2, \ldots, n\}$ is an index set of the integer-constrained variables.

An MPS file with one row and one column can be illustrated like this:

```
*        1         2         3         4         5         6
*2345678901234567890123456789012345678901234567890123456789012345678901234567890
NAME          [name]
OBJSENSE
[objsense]
OBJNAME
[objname]
ROWS
?  [cname1]
COLUMNS
[vname1]  [cname1]    [value1]     [vname3]  [value2]
RHS
[name]    [cname1]    [value1]     [cname2]  [value2]
RANGES
[name]    [cname1]    [value1]     [cname2]  [value2]
QSECTION      [cname1]
[vname1]  [vname2]    [value1]     [vname3]  [value2]
QMATRIX
[vname1]  [vname2]    [value1]
QUADOBJ
[vname1]  [vname2]    [value1]
QCMATRIX      [cname1]
[vname1]  [vname2]    [value1]
BOUNDS
?? [name]    [vname1]    [value1]
CSECTION      [kname1]    [value1]     [ktype]
[vname1]
ENDATA
```

Here the names in capitals are keywords of the MPS format and names in brackets are custom defined names or values. A couple of notes on the structure:

- Fields: All items surrounded by brackets appear in *fields*. The fields named "`valueN`" are numerical values. Hence, they must have the format

```
  [+|-]XXXXXXX.XXXXXX[[e|E][+|-]XXX]


where
```

```
.. code-block:: text

   X = [0|1|2|3|4|5|6|7|8|9].
```

- Sections: The MPS file consists of several sections where the names in capitals indicate the beginning of a new section. For example, `COLUMNS` denotes the beginning of the columns section.
- Comments: Lines starting with an `*` are comment lines and are ignored by **MOSEK**.
- Keys: The question marks represent keys to be specified later.
- Extensions: The sections `QSECTION` and `CSECTION` are specific **MOSEK** extensions of the MPS format. The sections `QMATRIX`, `QUADOBJ` and `QCMATRIX` are included for sake of compatibility with other vendors extensions to the MPS format.

The standard MPS format is a fixed format, i.e. everything in the MPS file must be within certain fixed positions. **MOSEK** also supports a *free format*. See Section *14.2.9* for details.

Linear example `lo1.mps`

A concrete example of a MPS file is presented below:

```
* File: lo1.mps
NAME          lo1
OBJSENSE
    MAX
ROWS
 N  obj
 E  c1
 G  c2
 L  c3
COLUMNS
    x1        obj       3
    x1        c1        3
    x1        c2        2
    x2        obj       1
    x2        c1        1
    x2        c2        1
    x2        c3        2
    x3        obj       5
    x3        c1        2
    x3        c2        3
    x4        obj       1
    x4        c2        1
    x4        c3        3
RHS
    rhs       c1        30
    rhs       c2        15
    rhs       c3        25
RANGES
BOUNDS
 UP bound     x2        10
ENDATA
```

Subsequently each individual section in the MPS format is discussed.

Section `NAME`

In this section a name (`[name]`) is assigned to the problem.

OBJSENSE (optional)

This is an optional section that can be used to specify the sense of the objective function. The OBJSENSE section contains one line at most which can be one of the following

```
MIN
MINIMIZE
MAX
MAXIMIZE
```

It should be obvious what the implication is of each of these four lines.

OBJNAME (optional)

This is an optional section that can be used to specify the name of the row that is used as objective function. The OBJNAME section contains one line at most which has the form

```
objname
```

objname should be a valid row name.

ROWS

A record in the ROWS section has the form

```
?  [cname1]
```

where the requirements for the fields are as follows:

Field	Starting Position	Max Width	required	Description
?	2	1	Yes	Constraint key
[cname1]	5	8	Yes	Constraint name

Hence, in this section each constraint is assigned an unique name denoted by [cname1]. Please note that [cname1] starts in position 5 and the field can be at most 8 characters wide. An initial key ? must be present to specify the type of the constraint. The key can have the values E, G, L, or N with the following interpretation:

Constraint type	l_i^c	u_i^c
E	finite	l_i^c
G	finite	∞
L	$-\infty$	finite
N	$-\infty$	∞

In the MPS format an objective vector is not specified explicitly, but one of the constraints having the key N will be used as the objective vector c . In general, if multiple N type constraints are specified, then the first will be used as the objective vector c.

COLUMNS

In this section the elements of A are specified using one or more records having the form:

```
[vname1]  [cname1]    [value1]     [cname2]  [value2]
```

where the requirements for each field are as follows:

Field	Starting Position	Max Width	required	Description
[vname1]	5	8	Yes	Variable name
[cname1]	15	8	Yes	Constraint name
[value1]	25	12	Yes	Numerical value
[cname2]	40	8	No	Constraint name
[value2]	50	12	No	Numerical value

Hence, a record specifies one or two elements a_{ij} of A using the principle that [vname1] and [cname1] determines j and i respectively. Please note that [cname1] must be a constraint name specified in the ROWS section. Finally, [value1] denotes the numerical value of a_{ij} . Another optional element is specified by [cname2], and [value2] for the variable specified by [vname1]. Some important comments are:

- All elements belonging to one variable must be grouped together.
- Zero elements of A should not be specified.
- At least one element for each variable should be specified.

RHS (optional)

A record in this section has the format

```
[name]    [cname1]    [value1]    [cname2]  [value2]
```

where the requirements for each field are as follows:

Field	Starting Position	Max Width	required	Description
[name]	5	8	Yes	Name of the RHS vector
[cname1]	15	8	Yes	Constraint name
[value1]	25	12	Yes	Numerical value
[cname2]	40	8	No	Constraint name
[value2]	50	12	No	Numerical value

The interpretation of a record is that [name] is the name of the RHS vector to be specified. In general, several vectors can be specified. [cname1] denotes a constraint name previously specified in the ROWS section. Now, assume that this name has been assigned to the i th constraint and v_1 denotes the value specified by [value1], then the interpretation of v_1 is:

Constraint	l_i^c	u_i^c
type		
E	v_1	v_1
G	v_1	
L		v_1
N		

An optional second element is specified by [cname2] and [value2] and is interpreted in the same way. Please note that it is not necessary to specify zero elements, because elements are assumed to be zero.

RANGES (optional)

A record in this section has the form

```
[name]    [cname1]    [value1]    [cname2]  [value2]
```

where the requirements for each fields are as follows:

Field	Starting Position	Max Width	required	Description
[name]	5	8	Yes	Name of the RANGE vector
[cname1]	15	8	Yes	Constraint name
[value1]	25	12	Yes	Numerical value
[cname2]	40	8	No	Constraint name
[value2]	50	12	No	Numerical value

The records in this section are used to modify the bound vectors for the constraints, i.e. the values in l^c and u^c . A record has the following interpretation: `[name]` is the name of the `RANGE` vector and `[cname1]` is a valid constraint name. Assume that `[cname1]` is assigned to the i th constraint and let v_1 be the value specified by `[value1]`, then a record has the interpretation:

Constraint type	Sign of v_1	l_i^c	u_i^c
E	$-$	$u_i^c + v_1$	
E	$+$		$l_i^c + v_1$
G	$-$ or $+$	$l_i^c + \|v_1\|$	
L	$-$ or $+$	$u_i^c - \|v_1\|$	
N			

QSECTION (optional)

Within the `QSECTION` the label `[cname1]` must be a constraint name previously specified in the `ROWS` section. The label `[cname1]` denotes the constraint to which the quadratic term belongs. A record in the `QSECTION` has the form

```
[vname1]   [vname2]     [value1]      [vname3]   [value2]
```

where the requirements for each field are:

Field	Starting Position	Max Width	required	Description
`[vname1]`	5	8	Yes	Variable name
`[vname2]`	15	8	Yes	Variable name
`[value1]`	25	12	Yes	Numerical value
`[vname3]`	40	8	No	Variable name
`[value2]`	50	12	No	Numerical value

A record specifies one or two elements in the lower triangular part of the Q^i matrix where `[cname1]` specifies the i . Hence, if the names `[vname1]` and `[vname2]` have been assigned to the k th and j th variable, then Q^i_{kj} is assigned the value given by `[value1]` An optional second element is specified in the same way by the fields `[vname1]`, `[vname3]`, and `[value2]`.

The example

$$\begin{array}{lcll} \text{minimize} & -x_2 + \frac{1}{2}(2x_1^2 - 2x_1x_3 + 0.2x_2^2 + 2x_3^2) & & \\ \text{subject to} & x_1 + x_2 + x_3 & \geq & 1, \\ & x \geq 0 & & \end{array}$$

has the following MPS file representation

```
* File: qo1.mps
NAME          qo1
ROWS
N  obj
G  c1
COLUMNS
x1        c1        1.0
x2        obj       -1.0
x2        c1        1.0
x3        c1        1.0
RHS
rhs       c1        1.0
QSECTION      obj
x1        x1        2.0
x1        x3        -1.0
x2        x2        0.2
x3        x3        2.0
ENDATA
```

Regarding the `QSECTION`s please note that:

- Only one `QSECTION` is allowed for each constraint.
- The `QSECTION`s can appear in an arbitrary order after the `COLUMNS` section.
- All variable names occurring in the `QSECTION` must already be specified in the `COLUMNS` section.
- All entries specified in a `QSECTION` are assumed to belong to the lower triangular part of the quadratic term of Q .

`QMATRIX/QUADOBJ` (optional)

The `QMATRIX` and `QUADOBJ` sections allow to define the quadratic term of the objective function. They differ in how the quadratic term of the objective function is stored:

- `QMATRIX` It stores all the nonzeros coefficients, withouot taking advantage of the symmetry of the Q matrix.
- `QUADOBJ` It only store the upper diagonal nonzero elements of the Q matrix.

A record in both sections has the form:

```
[vname1]   [vname2]     [value1]
```

where the requirements for each field are:

Field	Starting Position	Max Width	required	Description
`[vname1]`	5	8	Yes	Variable name
`[vname2]`	15	8	Yes	Variable name
`[value1]`	25	12	Yes	Numerical value

A record specifies one elements of the Q matrix in the objective function . Hence, if the names `[vname1]` and `[vname2]` have been assigned to the k th and j th variable, then Q_{kj} is assigned the value given by `[value1]`. Note that a line must apper for each off-diagonal coefficient if using a `QMATRIX` section, while only one entry is required in a `QUADOBJ` section. The quadratic part of the objective function will be evaluated as $1/2x^TQx$.

The example

$$\begin{array}{lcc} \text{minimize} & -x_2 + \frac{1}{2}(2x_1^2 - 2x_1x_3 + 0.2x_2^2 + 2x_3^2) & \\ \text{subject to} & x_1 + x_2 + x_3 & \geq \quad 1, \\ & x \geq 0 & \end{array}$$

has the following MPS file representation using `QMATRIX`

```
* File: qo1_matrix.mps
NAME          qo1_qmatrix
ROWS
 N  obj
 G  c1
COLUMNS
    x1        c1        1.0
    x2        obj       -1.0
    x2        c1        1.0
    x3        c1        1.0
RHS
    rhs       c1        1.0
QMATRIX
    x1        x1        2.0
    x1        x3        -1.0
    x3        x1        -1.0
    x2        x2        0.2
    x3        x3        2.0
ENDATA
```

or the following using QUADOBJ

```
* File: qo1_quadobj.mps
NAME          qo1_quadobj
ROWS
 N  obj
 G  c1
COLUMNS
    x1        c1        1.0
    x2        obj       -1.0
    x2        c1        1.0
    x3        c1        1.0
RHS
    rhs       c1        1.0
QUADOBJ
    x1        x1        2.0
    x1        x3        -1.0
    x2        x2        0.2
    x3        x3        2.0
ENDATA
```

Please also note that:

- A QMATRIX/QUADOBJ section can appear in an arbitrary order after the COLUMNS section.
- All variable names occurring in the QMATRIX/QUADOBJ section must already be specified in the COLUMNS section.

14.2.2 QCMATRIX (optional)

A QCMATRIX section allows to specify the quadratic part of a given constraints. Within the QCMATRIX the label [cname1] must be a constraint name previously specified in the ROWS section. The label [cname1] denotes the constraint to which the quadratic term belongs. A record in the QSECTION has the form

```
[vname1]  [vname2]    [value1]
```

where the requirements for each field are:

Field	Starting Position	Max Width	required	Description
[vname1]	5	8	Yes	Variable name
[vname2]	15	8	Yes	Variable name
[value1]	25	12	Yes	Numerical value

A record specifies an entry of the Q^i matrix where [cname1] specifies the i. Hence, if the names [vname1] and [vname2] have been assigned to the k th and j th variable, then Q^i_{kj} is assigned the value given by [value1]. Moreover, the quadratic term is represented as $1/2x^TQx$.

The example

$$\begin{array}{lcll} \text{minimize} & x_2 & & \\ \text{subject to} & x_1+x_2+x_3 & \geq & 1, \\ & \frac{1}{2}(-2x_1x_3+0.2x_2^2+2x_3^2) & \leq & 10, \\ & x \geq 0 & & \end{array}$$

has the following MPS file representation

```
* File: qo1.mps
NAME          qo1
ROWS
 N  obj
 G  c1
 L  q1
COLUMNS
```

```
    x1        c1        1.0
    x2        obj       -1.0
    x2        c1        1.0
    x3        c1        1.0
RHS
    rhs       c1        1.0
    rhs       q1        10.0
QCMATRIX      q1
    x1        x1        2.0
    x1        x3        -1.0
    x3        x1        -1.0
    x2        x2        0.2
    x3        x3        2.0
ENDATA
```

Regarding the `QCMATRIX`s please note that:

- Only one `QCMATRIX` is allowed for each constraint.
- The `QCMATRIX`s can appear in an arbitrary order after the `COLUMNS` section.
- All variable names occurring in the `QSECTION` must already be specified in the `COLUMNS` section.
- A `QCMATRIX` does not exploit the symmetry of Q: an off-diagonal entry (i, j) should apperas twice.

14.2.3 BOUNDS (optional)

In the `BOUNDS` section changes to the default bounds vectors l^x and u^x are specified. The default bounds vectors are $l^x = 0$ and $u^x = \infty$. Moreover, it is possible to specify several sets of bound vectors. A record in this section has the form

```
?? [name]     [vname1]     [value1]
```

where the requirements for each field are:

Field	Starting Position	Max Width	Required	Description
`??`	2	2	Yes	Bound key
`[name]`	5	8	Yes	Name of the `BOUNDS` vector
`[vname1]`	15	8	Yes	Variable name
`[value1]`	25	12	No	Numerical value

Hence, a record in the `BOUNDS` section has the following interpretation: `[name]` is the name of the bound vector and `[vname1]` is the name of the variable which bounds are modified by the record. `??` and `[value1]` are used to modify the bound vectors according to the following table:

`??`	l_j^x	u_j^x	Made integer (added to $\mathcal{J}$)
`FR`	$-\infty$	∞	No
`FX`	v_1	v_1	No
`LO`	v_1	unchanged	No
`MI`	$-\infty$	unchanged	No
`PL`	unchanged	∞	No
`UP`	unchanged	v_1	No
`BV`	0	1	Yes
`LI`	$\lceil v_1 \rceil$	unchanged	Yes
`UI`	unchanged	$\lfloor v_1 \rfloor$	Yes

v_ 1 is the value specified by `[value1]`.

14.2.4 CSECTION (optional)

The purpose of the CSECTION is to specify the constraint

$$x \in \mathcal{K}.$$

in (14.2). It is assumed that $\mathcal{K}$ satisfies the following requirements. Let

$$x^t \in \mathbb{R}^{n^t}, \quad t = 1, \ldots, k$$

be vectors comprised of parts of the decision variables x so that each decision variable is a member of exactly **one** vector x^t, for example

$$x^1 = \begin{bmatrix} x_1 \\ x_4 \\ x_7 \end{bmatrix} \quad \text{and} \quad x^2 = \begin{bmatrix} x_6 \\ x_5 \\ x_3 \\ x_2 \end{bmatrix}.$$

Next define

$$\mathcal{K} := \left\{ x \in \mathbb{R}^n : \quad x^t \in \mathcal{K}_t, \quad t = 1, \ldots, k \right\}$$

where $\mathcal{K}_t$ must have one of the following forms

- $\mathbb{R}$ set:

$$\mathcal{K}_t = \left\{ x \in \mathbb{R}^{n^t} \right\}.$$

- Quadratic cone:

$$\mathcal{K}_t = \left\{ x \in \mathbb{R}^{n^t} : x_1 \geq \sqrt{\sum_{j=2}^{n^t} x_j^2} \right\}. \tag{14.3}$$

- Rotated quadratic cone:

$$\mathcal{K}_t = \left\{ x \in \mathbb{R}^{n^t} : 2x_1 x_2 \geq \sum_{j=3}^{n^t} x_j^2, \quad x_1, x_2 \geq 0 \right\}. \tag{14.4}$$

In general, only quadratic and rotated quadratic cones are specified in the MPS file whereas membership of the $\mathbb{R}$ set is not. If a variable is not a member of any other cone then it is assumed to be a member of an $\mathbb{R}$ cone.

Next, let us study an example. Assume that the quadratic cone

$$x_4 \geq \sqrt{x_5^2 + x_8^2}$$

and the rotated quadratic cone

$$x_3 x_7 \geq x_1^2 + x_0^2, \quad x_3, x_7 \geq 0,$$

should be specified in the MPS file. One CSECTION is required for each cone and they are specified as follows:

```
*        1         2         3         4         5         6
*2345678901234567890123456789012345678901234567890123456789012345678901234567890
CSECTION       konea        0.0           QUAD
x4
x5
x8
CSECTION       koneb        0.0           RQUAD
x7
x3
x1
x0
```

This first `CSECTION` specifies the cone (14.3) which is given the name `konea`. This is a quadratic cone which is specified by the keyword `QUAD` in the `CSECTION` header. The 0.0 value in the `CSECTION` header is not used by the `QUAD` cone.

The second `CSECTION` specifies the rotated quadratic cone (14.4). Please note the keyword `RQUAD` in the `CSECTION` which is used to specify that the cone is a rotated quadratic cone instead of a quadratic cone. The 0.0 value in the `CSECTION` header is not used by the `RQUAD` cone.

In general, a `CSECTION` header has the format

```
CSECTION       [kname1]     [value1]     [ktype]
```

where the requirement for each field are as follows:

Field	Starting Position	Max Width	Required	Description
`[kname1]`	5	8	Yes	Name of the cone
`[value1]`	15	12	No	Cone parameter
`[ktype]`	25		Yes	Type of the cone.

The possible cone type keys are:

Cone type key	Members	Interpretation.
`QUAD`	≤ 1	Quadratic cone i.e. (14.3).
`RQUAD`	≤ 2	Rotated quadratic cone i.e. (14.4).

Please note that a quadratic cone must have at least one member whereas a rotated quadratic cone must have at least two members. A record in the `CSECTION` has the format

```
[vname1]
```

where the requirements for each field are

Field	Starting Position	Max Width	required	Description
`[vname1]`	2	8	Yes	A valid variable name

The most important restriction with respect to the `CSECTION` is that a variable must occur in only one `CSECTION`.

14.2.5 ENDATA

This keyword denotes the end of the MPS file.

14.2.6 Integer Variables

Using special bound keys in the `BOUNDS` section it is possible to specify that some or all of the variables should be integer-constrained i.e. be members of $\mathcal{J}$. However, an alternative method is available.

This method is available only for backward compatibility and we recommend that it is not used. This method requires that markers are placed in the `COLUMNS` section as in the example:

```
COLUMNS
x1        obj       -10.0          c1        0.7
x1        c2        0.5            c3        1.0
x1        c4        0.1
* Start of integer-constrained variables.
MARK000   'MARKER'                 'INTORG'
x2        obj       -9.0           c1        1.0
x2        c2        0.8333333333   c3        0.66666667
x2        c4        0.25
x3        obj       1.0            c6        2.0
MARK001   'MARKER'                 'INTEND'
```

- End of integer-constrained variables.

Please note that special marker lines are used to indicate the start and the end of the integer variables. Furthermore be aware of the following

- IMPORTANT: All variables between the markers are assigned a default lower bound of 0 and a default upper bound of 1. **This may not be what is intended.** If it is not intended, the correct bounds should be defined in the `BOUNDS` section of the MPS formatted file.
- **MOSEK** ignores field 1, i.e. `MARK0001` and `MARK001`, however, other optimization systems require them.
- Field 2, i.e. `MARKER`, must be specified including the single quotes. This implies that no row can be assigned the name `MARKER`.
- Field 3 is ignored and should be left blank.
- Field 4, i.e. `INTORG` and `INTEND`, must be specified.
- It is possible to specify several such integer marker sections within the `COLUMNS` section.

14.2.7 General Limitations

- An MPS file should be an ASCII file.

14.2.8 Interpretation of the MPS Format

Several issues related to the MPS format are not well-defined by the industry standard. However, **MOSEK** uses the following interpretation:

- If a matrix element in the `COLUMNS` section is specified multiple times, then the multiple entries are added together.
- If a matrix element in a `QSECTION` section is specified multiple times, then the multiple entries are added together.

14.2.9 The Free MPS Format

MOSEK supports a free format variation of the MPS format. The free format is similar to the MPS file format but less restrictive, e.g. it allows longer names. However, it also presents two main limitations:

- A name must not contain any blanks.
- By default a line in the MPS file must not contain more than 1024 characters. However, by modifying the parameter *MSK_IPAR_READ_MPS_WIDTH* an arbitrary large line width will be accepted.

To use the free MPS format instead of the default MPS format the **MOSEK** parameter *MSK_IPAR_READ_MPS_FORMAT* should be changed.

14.3 The OPF Format

The *Optimization Problem Format (OPF)* is an alternative to LP and MPS files for specifying optimization problems. It is row-oriented, inspired by the CPLEX LP format.

Apart from containing objective, constraints, bounds etc. it may contain complete or partial solutions, comments and extra information relevant for solving the problem. It is designed to be easily read and modified by hand and to be forward compatible with possible future extensions.

Intended use

The OPF file format is meant to replace several other files:

- The LP file format: Any problem that can be written as an LP file can be written as an OPF file too; furthermore it naturally accommodates ranged constraints and variables as well as arbitrary characters in names, fixed expressions in the objective, empty constraints, and conic constraints.
- Parameter files: It is possible to specify integer, double and string parameters along with the problem (or in a separate OPF file).
- Solution files: It is possible to store a full or a partial solution in an OPF file and later reload it.

14.3.1 The File Format

The format uses tags to structure data. A simple example with the basic sections may look like this:

```
[comment]
This is a comment. You may write almost anything here...
[/comment]

# This is a single-line comment.

[objective min 'myobj']
x + 3 y + x^2 + 3 y^2 + z + 1
[/objective]

[constraints]
[con 'con01'] 4 <= x + y  [/con]
[/constraints]

[bounds]
[b] -10 <= x,y <= 10  [/b]

[cone quad] x,y,z [/cone]
[/bounds]
```

A scope is opened by a tag of the form `[tag]` and closed by a tag of the form `[/tag]`. An opening tag may accept a list of unnamed and named arguments, for examples:

```
[tag value] tag with one unnamed argument [/tag]
[tag arg=value] tag with one named argument in quotes [/tag]
```

Unnamed arguments are identified by their order, while named arguments may appear in any order, but never before an unnamed argument. The `value` can be a quoted, single-quoted or double-quoted text string, i.e.

```
[tag 'value']     single-quoted value [/tag]
[tag arg='value'] single-quoted value [/tag]
[tag "value"]     double-quoted value [/tag]
[tag arg="value"] double-quoted value [/tag]
```

Sections

The recognized tags are

[comment]

A comment section. This can contain *almost* any text: Between single quotes (') or double quotes (") any text may appear. Outside quotes the markup characters ([and]) must be prefixed by backslashes. Both single and double quotes may appear alone or inside a pair of quotes if it is prefixed by a backslash.

[objective]

The objective function: This accepts one or two parameters, where the first one (in the above example `min`) is either `min` or `max` (regardless of case) and defines the objective sense, and the second one (above `myobj`), if present, is the objective name. The section may contain linear and quadratic expressions. If several objectives are specified, all but the last are ignored.

[constraints]

This does not directly contain any data, but may contain the subsection `con` defining a linear constraint.

`[con]` defines a single constraint; if an argument is present (`[con NAME]`) this is used as the name of the constraint, otherwise it is given a null-name. The section contains a constraint definition written as linear and quadratic expressions with a lower bound, an upper bound, with both or with an equality. Examples:

```
[constraints]
[con 'con1'] 0 <= x + y       [/con]
[con 'con2'] 0 >= x + y       [/con]
[con 'con3'] 0 <= x + y <= 10 [/con]
[con 'con4']      x + y  = 10 [/con]
[/constraints]
```

Constraint names are unique. If a constraint is specified which has the same name as a previously defined constraint, the new constraint replaces the existing one.

[bounds]

This does not directly contain any data, but may contain the subsections `b` (linear bounds on variables) and `cone` (quadratic cone).

`[b]`. Bound definition on one or several variables separated by comma (`,`). An upper or lower bound on a variable replaces any earlier defined bound on that variable. If only one bound (upper or lower) is given only this bound is replaced. This means that upper and lower bounds can be specified separately. So the OPF bound definition:

```
[b]  x,y >= -10  [/b]
[b]  x,y <= 10   [/b]
```

results in the bound $-10 \leq x, y \leq 10$.

`[cone]`. currently supports the *quadratic cone* and the *rotated quadratic cone*.

A conic constraint is defined as a set of variables which belong to a single unique cone.

- A quadratic cone of n variables $x_1, \ldots, x_n$ defines a constraint of the form

$$x_1^2 \geq \sum_{i=2}^{n} x_i^2, \quad x_1 \geq 0.$$

- A rotated quadratic cone of n variables $x_1, \ldots, x_n$ defines a constraint of the form

$$2x_1 x_2 \geq \sum_{i=3}^{n} x_i^2, \quad x_1, x_2 \geq 0.$$

A `[bounds]`-section example:

```
[bounds]
[b]  0 <= x,y <= 10  [/b] # ranged bound
[b] 10 >= x,y >=  0  [/b] # ranged bound
[b]  0 <= x,y <= inf [/b] # using inf
[b]       x,y free   [/b] # free variables
# Let (x,y,z,w) belong to the cone K
[cone quad]  x,y,z,w  [/cone] # quadratic cone
[cone rquad] x,y,z,w  [/cone] # rotated quadratic cone
[/bounds]
```

By default all variables are free.

[variables]

This defines an ordering of variables as they should appear in the problem. This is simply a space-separated list of variable names. Optionally, an attribute can be added `[variables disallow_new_variables]` indicating that if any variable not listed here occurs later in the file it is an error.

[integer]

This contains a space-separated list of variables and defines the constraint that the listed variables must be integer values.

[hints]

This may contain only non-essential data; for example estimates of the number of variables, constraints and non-zeros. Placed before all other sections containing data this may reduce the time spent reading the file.

In the `hints` section, any subsection which is not recognized by **MOSEK** is simply ignored. In this section a hint in a subsection is defined as follows:

```
[hint ITEM] value [/hint]
```

where `ITEM` may be replaced by `numvar` (number of variables), `numcon` (number of linear/quadratic constraints), `numanz` (number of linear non-zeros in constraints) and `numqnz` (number of quadratic non-zeros in constraints).

[solutions]

This section can contain a set of full or partial solutions to a problem. Each solution must be specified using a [solution]-section, i.e.

```
[solutions]
[solution]...[/solution] #solution 1
[solution]...[/solution] #solution 2
#other solutions....
[solution]...[/solution] #solution n
[/solutions]
```

Note that a [solution]-section must be always specified inside a [solutions]-section. The syntax of a [solution]-section is the following:

```
[solution SOLTYPE status=STATUS]...[/solution]
```

where SOLTYPE is one of the strings

- interior, a non-basic solution,
- basic, a basic solution,
- integer, an integer solution,

and STATUS is one of the strings

- UNKNOWN,
- OPTIMAL,
- INTEGER_OPTIMAL,
- PRIM_FEAS,
- DUAL_FEAS,
- PRIM_AND_DUAL_FEAS,
- NEAR_OPTIMAL,
- NEAR_PRIM_FEAS,
- NEAR_DUAL_FEAS,
- NEAR_PRIM_AND_DUAL_FEAS,
- PRIM_INFEAS_CER,
- DUAL_INFEAS_CER,
- NEAR_PRIM_INFEAS_CER,
- NEAR_DUAL_INFEAS_CER,
- NEAR_INTEGER_OPTIMAL.

Most of these values are irrelevant for input solutions; when constructing a solution for simplex hot-start or an initial solution for a mixed integer problem the safe setting is UNKNOWN.

A [solution]-section contains [con] and [var] sections. Each [con] and [var] section defines solution information for a single variable or constraint, specified as list of KEYWORD/value pairs, in any order, written as

```
KEYWORD=value
```

Allowed keywords are as follows:

- sk. The status of the item, where the value is one of the following strings:
  - LOW, the item is on its lower bound.

  - `UPR`, the item is on its upper bound.
  - `FIX`, it is a fixed item.
  - `BAS`, the item is in the basis.
  - `SUPBAS`, the item is super basic.
  - `UNK`, the status is unknown.
  - `INF`, the item is outside its bounds (infeasible).
- `lvl` Defines the level of the item.
- `sl` Defines the level of the dual variable associated with its lower bound.
- `su` Defines the level of the dual variable associated with its upper bound.
- `sn` Defines the level of the variable associated with its cone.
- `y` Defines the level of the corresponding dual variable (for constraints only).

A `[var]` section should always contain the items `sk`, `lvl`, `sl` and `su`. Items `sl` and `su` are not required for `integer` solutions.

A `[con]` section should always contain `sk`, `lvl`, `sl`, `su` and `y`.

An example of a solution section

```
[solution basic status=UNKNOWN]
[var x0] sk=LOW    lvl=5.0      [/var]
[var x1] sk=UPR    lvl=10.0     [/var]
[var x2] sk=SUPBAS lvl=2.0  sl=1.5 su=0.0 [/var]

[con c0] sk=LOW    lvl=3.0 y=0.0 [/con]
[con c0] sk=UPR    lvl=0.0 y=5.0 [/con]
[/solution]
```

- `[vendor]` This contains solver/vendor specific data. It accepts one argument, which is a vendor ID – for **MOSEK** the ID is simply `mosek` – and the section contains the subsection `parameters` defining solver parameters. When reading a vendor section, any unknown vendor can be safely ignored. This is described later.

Comments using the `#` may appear anywhere in the file. Between the `#` and the following line-break any text may be written, including markup characters.

Numbers

Numbers, when used for parameter values or coefficients, are written in the usual way by the `printf` function. That is, they may be prefixed by a sign (`+` or `-`) and may contain an integer part, decimal part and an exponent. The decimal point is always `.` (a dot). Some examples are

```
1
1.0
.0
1.
1e10
1e+10
1e-10
```

Some *invalid* examples are

```
e10   # invalid, must contain either integer or decimal part
.     # invalid
.e10  # invalid
```

More formally, the following standard regular expression describes numbers as used:

```
[+|-]?([0-9]+[.][0-9]*|[.][0-9]+)([eE][+|-]?[0-9]+)?
```

Names

Variable names, constraint names and objective name may contain arbitrary characters, which in some cases must be enclosed by quotes (single or double) that in turn must be preceded by a backslash. Unquoted names must begin with a letter (`a-z` or `A-Z`) and contain only the following characters: the letters `a-z` and `A-Z`, the digits `0-9`, braces (`{` and `}`) and underscore (`_`).

Some examples of legal names:

```
an_unquoted_name
another_name{123}
'single quoted name'
"double quoted name"
"name with \\"quote\\" in it"
"name with []s in it"
```

14.3.2 Parameters Section

In the `vendor` section solver parameters are defined inside the `parameters` subsection. Each parameter is written as

```
[p PARAMETER_NAME] value [/p]
```

where `PARAMETER_NAME` is replaced by a **MOSEK** parameter name, usually of the form `MSK_IPAR_...`, `MSK_DPAR_...` or `MSK_SPAR_...`, and the `value` is replaced by the value of that parameter; both integer values and named values may be used. Some simple examples are

```
[vendor mosek]
[parameters]
[p MSK_IPAR_OPF_MAX_TERMS_PER_LINE] 10     [/p]
[p MSK_IPAR_OPF_WRITE_PARAMETERS]   MSK_ON [/p]
[p MSK_DPAR_DATA_TOL_BOUND_INF]     1.0e18 [/p]
[/parameters]
[/vendor]
```

14.3.3 Writing OPF Files from MOSEK

To write an OPF file set the parameter *MSK_IPAR_WRITE_DATA_FORMAT* to *MSK_DATA_FORMAT_OP* as this ensures that `OPF` format is used.

Then modify the following parameters to define what the file should contain:

MSK_IPAR_OPF_WRITE_SOL_BAS	Include basic solution, if defined.
MSK_IPAR_OPF_WRITE_SOL_ITG	Include integer solution, if defined.
MSK_IPAR_OPF_WRITE_SOL_ITR	Include interior solution, if defined.
MSK_IPAR_OPF_WRITE_SOLUTIONS	Include solutions if they are defined. If this is off, no solutions are included.
MSK_IPAR_OPF_WRITE_HEADER	Include a small header with comments.
MSK_IPAR_OPF_WRITE_PROBLEM	Include the problem itself — objective, constraints and bounds.
MSK_IPAR_OPF_WRITE_PARAMETERS	Include all parameter settings.
MSK_IPAR_OPF_WRITE_HINTS	Include hints about the size of the problem.

14.3.4 Examples

This section contains a set of small examples written in OPF and describing how to formulate linear, quadratic and conic problems.

Linear Example `lo1.opf`

Consider the example:

$$\begin{array}{lccccccccc} \text{maximize} & 3x_0 & + & 1x_1 & + & 5x_2 & + & 1x_3 & & \\ \text{subject to} & 3x_0 & + & 1x_1 & + & 2x_2 & & & = & 30, \\ & 2x_0 & + & 1x_1 & + & 3x_2 & + & 1x_3 & \geq & 15, \\ & & & 2x_1 & & & + & 3x_3 & \leq & 25, \end{array}$$

having the bounds

$$\begin{array}{ccccc} 0 & \leq & x_0 & \leq & \infty, \\ 0 & \leq & x_1 & \leq & 10, \\ 0 & \leq & x_2 & \leq & \infty, \\ 0 & \leq & x_3 & \leq & \infty. \end{array}$$

In the `OPF` format the example is displayed as shown in Listing 14.1.

Listing 14.1: Example of an OPF file for a linear problem.

```
[comment]
  The lo1 example in OPF format
[/comment]

[hints]
  [hint NUMVAR] 4 [/hint]
  [hint NUMCON] 3 [/hint]
  [hint NUMANZ] 9 [/hint]
[/hints]

[variables disallow_new_variables]
  x1 x2 x3 x4
[/variables]

[objective maximize 'obj']
   3 x1 + x2 + 5 x3 + x4
[/objective]

[constraints]
  [con 'c1'] 3 x1 +   x2 + 2 x3         = 30 [/con]
  [con 'c2'] 2 x1 +   x2 + 3 x3 +   x4 >= 15 [/con]
  [con 'c3']        2 x2        + 3 x4 <= 25 [/con]
[/constraints]

[bounds]
  [b] 0 <= * [/b]
  [b] 0 <= x2 <= 10 [/b]
[/bounds]
```

Quadratic Example `qo1.opf`

An example of a quadratic optimization problem is

$$\begin{array}{lccc} \text{minimize} & & & x_1^2 + 0.1x_2^2 + x_3^2 - x_1x_3 - x_2 \\ \text{subject to} & 1 & \leq & x_1 + x_2 + x_3, \\ & & & x \geq 0. \end{array}$$

This can be formulated in `opf` as shown below.

Listing 14.2: Example of an OPF file for a quadratic problem.

```
[comment]
  The qo1 example in OPF format
[/comment]

[hints]
  [hint NUMVAR] 3 [/hint]
  [hint NUMCON] 1 [/hint]
  [hint NUMANZ] 3 [/hint]
  [hint NUMQNZ] 4 [/hint]
[/hints]

[variables disallow_new_variables]
  x1 x2 x3
[/variables]

[objective minimize 'obj']
  # The quadratic terms are often written with a factor of 1/2 as here,
  # but this is not required.

   - x2 + 0.5 ( 2.0 x1 ^ 2 - 2.0 x3 * x1 + 0.2 x2 ^ 2 + 2.0 x3 ^ 2 )
[/objective]

[constraints]
  [con 'c1'] 1.0 <= x1 + x2 + x3 [/con]
[/constraints]

[bounds]
  [b] 0 <= * [/b]
[/bounds]
```

Conic Quadratic Example `cqo1.opf`

Consider the example:

$$\begin{array}{lcll} \text{minimize} & x_3 + x_4 + x_5 & & \\ \text{subject to} & x_0 + x_1 + 2x_2 & = & 1, \\ & x_0, x_1, x_2 & \geq & 0, \\ & x_3 \geq \sqrt{x_0^2 + x_1^2}, & & \\ & 2x_4 x_5 \geq x_2^2. & & \end{array}$$

Please note that the type of the cones is defined by the parameter to `[cone ...]`; the content of the `cone`-section is the names of variables that belong to the cone. The resulting OPF file is in Listing 14.3.

Listing 14.3: Example of an OPF file for a conic quadratic problem.

```
[comment]
  The cqo1 example in OPF format.
[/comment]

[hints]
  [hint NUMVAR] 6 [/hint]
  [hint NUMCON] 1 [/hint]
  [hint NUMANZ] 3 [/hint]
[/hints]

[variables disallow_new_variables]
  x1 x2 x3 x4 x5 x6
[/variables]
```

```
[objective minimize 'obj']
   x4 + x5 + x6
[/objective]

[constraints]
  [con 'c1']  x1 + x2 + 2e+00 x3 = 1e+00 [/con]
[/constraints]

[bounds]
  # We let all variables default to the positive orthant
  [b] 0 <= * [/b]

  # ...and change those that differ from the default
  [b] x4,x5,x6 free [/b]

  # Define quadratic cone: x4 >= sqrt( x1^2 + x2^2 )
  [cone quad 'k1'] x4, x1, x2 [/cone]

  # Define rotated quadratic cone: 2 x5 x6 >= x3^2
  [cone rquad 'k2'] x5, x6, x3 [/cone]
[/bounds]
```

Mixed Integer Example `milo1.opf`

Consider the mixed integer problem:

$$\begin{array}{lrcl} \text{maximize} & x_0 + 0.64x_1 & & \\ \text{subject to} & 50x_0 + 31x_1 & \leq & 250, \\ & 3x_0 - 2x_1 & \geq & -4, \\ & x_0, x_1 \geq 0 & & \text{and integer} \end{array}$$

This can be implemented in `OPF` with the file in Listing 14.4.

Listing 14.4: Example of an OPF file for a mixed-integer linear problem.

```
[comment]
  The milo1 example in OPF format
[/comment]

[hints]
  [hint NUMVAR] 2 [/hint]
  [hint NUMCON] 2 [/hint]
  [hint NUMANZ] 4 [/hint]
[/hints]

[variables disallow_new_variables]
  x1 x2
[/variables]

[objective maximize 'obj']
   x1 + 6.4e-1 x2
[/objective]

[constraints]
  [con 'c1'] 5e+1 x1 + 3.1e+1 x2 <= 2.5e+2 [/con]
  [con 'c2'] -4 <= 3 x1 - 2 x2 [/con]
[/constraints]

[bounds]
  [b] 0 <= * [/b]
[/bounds]
```

```
[integer]
  x1 x2
[/integer]
```

14.4 The CBF Format

This document constitutes the technical reference manual of the *Conic Benchmark Format* with file extension: `.cbf` or `.CBF`. It unifies linear, second-order cone (also known as conic quadratic) and semidefinite optimization with mixed-integer variables. The format has been designed with benchmark libraries in mind, and therefore focuses on compact and easily parsable representations. The problem structure is separated from the problem data, and the format moreover facilitates benchmarking of hotstart capability through sequences of changes.

14.4.1 How Instances Are Specified

This section defines the spectrum of conic optimization problems that can be formulated in terms of the keywords of the CBF format.

In the CBF format, conic optimization problems are considered in the following form:

$$\begin{array}{lll} \min / \max & g^{obj} & \\ & g_i \in \mathcal{K}_i, & i \in \mathcal{I}, \\ \text{s.t.} & G_i \in \mathcal{K}_i, & i \in \mathcal{I}^{PSD}, \\ & x_j \in \mathcal{K}_j, & j \in \mathcal{J}, \\ & \overline{X}_j \in \mathcal{K}_j, & j \in \mathcal{J}^{PSD}. \end{array} \tag{14.5}$$

- **Variables** are either scalar variables, x_j for $j \in \mathcal{J}$, or variables, $\overline{X}_j$ for $j \in \mathcal{J}^{PSD}$. Scalar variables can also be declared as integer.
- **Constraints** are affine expressions of the variables, either scalar-valued g_i for $i \in \mathcal{I}$, or matrix-valued G_i for $i \in \mathcal{I}^{PSD}$

$$g_i = \sum_{j \in \mathcal{J}^{PSD}} \langle F_{ij}, X_j \rangle + \sum_{j \in \mathcal{J}} a_{ij} x_j + b_i,$$
$$G_i = \sum_{j \in \mathcal{J}} x_j H_{ij} + D_i.$$

- The **objective function** is a scalar-valued affine expression of the variables, either to be minimized or maximized. We refer to this expression as g^{obj}

$$g^{obj} = \sum_{j \in \mathcal{J}^{PSD}} \langle F_j^{obj}, X_j \rangle + \sum_{j \in \mathcal{J}} a_j^{obj} x_j + b^{obj}.$$

CBF format can represent the following cones $\mathcal{K}$:

- **Free domain** - A cone in the linear family defined by

$$\{x \in \mathbb{R}^n\}, \text{ for } n \geq 1.$$

- **Positive orthant** - A cone in the linear family defined by

$$\{x \in \mathbb{R}^n \mid x_j \geq 0 \text{ for } j = 1, \ldots, n\}, \text{ for } n \geq 1.$$

- **Negative orthant** - A cone in the linear family defined by

$$\{x \in \mathbb{R}^n \mid x_j \leq 0 \text{ for } j = 1, \ldots, n\}, \text{ for } n \geq 1.$$

- **Fixpoint zero** - A cone in the linear family defined by

$$\{x \in \mathbb{R}^n \mid x_j = 0 \text{ for } j = 1, \ldots, n\}, \text{ for } n \geq 1.$$

- **Quadratic cone** - A cone in the second-order cone family defined by

$$\left\{ \begin{pmatrix} p \\ x \end{pmatrix} \in \mathbb{R} \times \mathbb{R}^{n-1}, \; p^2 \geq x^T x, \; p \geq 0 \right\}, \text{ for } n \geq 2.$$

- **Rotated quadratic cone** - A cone in the second-order cone family defined by

$$\left\{ \begin{pmatrix} p \\ q \\ x \end{pmatrix} \in \mathbb{R} \times \mathbb{R} \times \mathbb{R}^{n-2}, \; 2pq \geq x^T x, \; p \geq 0, \; q \geq 0 \right\}, \text{ for } n \geq 3.$$

14.4.2 The Structure of CBF Files

This section defines how information is written in the CBF format, without being specific about the type of information being communicated.

All information items belong to exactly one of the three groups of information. These information groups, and the order they must appear in, are:

1. File format.
2. Problem structure.
3. Problem data.

The first group, file format, provides information on how to interpret the file. The second group, problem structure, provides the information needed to deduce the type and size of the problem instance. Finally, the third group, problem data, specifies the coefficients and constants of the problem instance.

Information items

The format is composed as a list of information items. The first line of an information item is the `KEYWORD`, revealing the type of information provided. The second line - of some keywords only - is the `HEADER`, typically revealing the size of information that follows. The remaining lines are the `BODY` holding the actual information to be specified.

```
KEYWORD
BODY

KEYWORD
HEADER
BODY
```

The `KEYWORD` determines how each line in the `HEADER` and `BODY` is structured. Moreover, the number of lines in the `BODY` follows either from the `KEYWORD`, the `HEADER`, or from another information item required to precede it.

Embedded hotstart-sequences

A sequence of problem instances, based on the same problem structure, is within a single file. This is facilitated via the `CHANGE` within the problem data information group, as a separator between the information items of each instance. The information items following a `CHANGE` keyword are appending to, or changing (e.g., setting coefficients back to their default value of zero), the problem data of the preceding instance.

The sequence is intended for benchmarking of hotstart capability, where the solvers can reuse their internal state and solution (subject to the achieved accuracy) as warmpoint for the succeeding instance. Whenever this feature is unsupported or undesired, the keyword `CHANGE` should be interpreted as the end of file.

File encoding and line width restrictions

The format is based on the US-ASCII printable character set with two extensions as listed below. Note, by definition, that none of these extensions can be misinterpreted as printable US-ASCII characters:

- A line feed marks the end of a line, carriage returns are ignored.
- Comment-lines may contain unicode characters in UTF-8 encoding.

The line width is restricted to 512 bytes, with 3 bytes reserved for the potential carriage return, line feed and null-terminator.

Integers and floating point numbers must follow the ISO C decimal string representation in the standard C locale. The format does not impose restrictions on the magnitude of, or number of significant digits in numeric data, but the use of 64-bit integers and 64-bit IEEE 754 floating point numbers should be sufficient to avoid loss of precision.

Comment-line and whitespace rules

The format allows single-line comments respecting the following rule:

- Lines having first byte equal to '`#`' (US-ASCII 35) are comments, and should be ignored. Comments are only allowed between information items.

Given that a line is not a comment-line, whitespace characters should be handled according to the following rules:

- Leading and trailing whitespace characters should be ignored.
  - The seperator between multiple pieces of information on one line, is either one or more whitespace characters.
- Lines containing only whitespace characters are empty, and should be ignored. Empty lines are only allowed between information items.

14.4.3 Problem Specification

The problem structure

The problem structure defines the objective sense, whether it is minimization and maximization. It also defines the index sets, $\mathcal{J}$, $\mathcal{J}^{PSD}$, $\mathcal{I}$ and $\mathcal{I}^{PSD}$, which are all numbered from zero, $\{0, 1, \ldots\}$, and empty until explicitly constructed.

- **Scalar variables** are constructed in vectors restricted to a conic domain, such as $(x_0, x_1) \in \mathbb{R}^2_+$, $(x_2, x_3, x_4) \in \mathcal{Q}^3$, etc. In terms of the Cartesian product, this generalizes to

$$x \in \mathcal{K}_1^{n_1} \times \mathcal{K}_2^{n_2} \times \cdots \times \mathcal{K}_k^{n_k}$$

which in the CBF format becomes:

```
VAR
n k
K1 n1
K2 n2
...
Kk nk
```

where $\sum_i n_i = n$ is the total number of scalar variables. The list of supported cones is found in Table 14.3. Integrality of scalar variables can be specified afterwards.

- **PSD variables** are constructed one-by-one. That is, $X_j \succeq \mathbf{0}^{n_j \times n_j}$ for $j \in \mathcal{J}^{PSD}$, constructs a matrix-valued variable of size $n_j \times n_j$ restricted to be symmetric positive semidefinite. In the CBF format, this list of constructions becomes:

```
PSDVAR
N
n1
n2
...
nN
```

where N is the total number of PSD variables.

- **Scalar constraints** are constructed in vectors restricted to a conic domain, such as $(g_0, g_1) \in \mathbb{R}^2_+$, $(g_2, g_3, g_4) \in \mathcal{Q}^3$, etc. In terms of the Cartesian product, this generalizes to

$$g \in \mathcal{K}_1^{m_1} \times \mathcal{K}_2^{m_2} \times \cdots \times \mathcal{K}_k^{m_k}$$

which in the CBF format becomes:

```
CON
m k
K1 m1
K2 m2
..
Kk mk
```

where $\sum_i m_i = m$ is the total number of scalar constraints. The list of supported cones is found in Table 14.3.

- **PSD constraints** are constructed one-by-one. That is, $G_i \succeq \mathbf{0}^{m_i \times m_i}$ for $i \in \mathcal{I}^{PSD}$, constructs a matrix-valued affine expressions of size $m_i \times m_i$ restricted to be symmetric positive semidefinite. In the CBF format, this list of constructions becomes

```
PSDCON
M
m1
m2
..
mM
```

where M is the total number of PSD constraints.

With the objective sense, variables (with integer indications) and constraints, the definitions of the many affine expressions follow in problem data.

Problem data

The problem data defines the coefficients and constants of the affine expressions of the problem instance. These are considered zero until explicitly defined, implying that instances with no keywords from this

information group are, in fact, valid. Duplicating or conflicting information is a failure to comply with the standard. Consequently, two coefficients written to the same position in a matrix (or to transposed positions in a symmetric matrix) is an error.

The affine expressions of the objective, g^{obj}, of the scalar constraints, g_i, and of the PSD constraints, G_i, are defined separately. The following notation uses the standard trace inner product for matrices, $\langle X, Y \rangle = \sum_{i,j} X_{ij} Y_{ij}$.

- The affine expression of the objective is defined as

$$g^{obj} = \sum_{j \in \mathcal{J}^{PSD}} \langle F_j^{obj}, X_j \rangle + \sum_{j \in \mathcal{J}} a_j^{obj} x_j + b^{obj},$$

  in terms of the symmetric matrices, F_j^{obj}, and scalars, a_j^{obj} and b^{obj}.

- The affine expressions of the scalar constraints are defined, for $i \in \mathcal{I}$, as

$$g_i = \sum_{j \in \mathcal{J}^{PSD}} \langle F_{ij}, X_j \rangle + \sum_{j \in \mathcal{J}} a_{ij} x_j + b_i,$$

  in terms of the symmetric matrices, F_{ij}, and scalars, a_{ij} and b_i.

- The affine expressions of the PSD constraints are defined, for $i \in \mathcal{I}^{PSD}$, as

$$G_i = \sum_{j \in \mathcal{J}} x_j H_{ij} + D_i,$$

  in terms of the symmetric matrices, H_{ij} and D_i.

List of cones

The format uses an explicit syntax for symmetric positive semidefinite cones as shown above. For scalar variables and constraints, constructed in vectors, the supported conic domains and their minimum sizes are given as follows.

Table 14.3: Cones available in the CBF format

Name	CBF keyword	Cone family
Free domain	`F`	linear
Positive orthant	`L+`	linear
Negative orthant	`L-`	linear
Fixpoint zero	`L=`	linear
Quadratic cone	`Q`	second-order
Rotated quadratic cone	`QR`	second-order

14.4.4 File Format Keywords

VER

Description: The version of the Conic Benchmark Format used to write the file.

`HEADER`: None

`BODY`: One line formatted as:

```
INT
```

This is the version number.

Must appear exactly once in a file, as the first keyword.

OBJSENSE

Description: Define the objective sense.

`HEADER`: None

`BODY`: One line formatted as:

```
STR
```

having `MIN` indicates minimize, and `MAX` indicates maximize. Capital letters are required.

Must appear exactly once in a file.

PSDVAR

Description: Construct the PSD variables.

`HEADER`: One line formatted as:

```
INT
```

This is the number of PSD variables in the problem.

`BODY`: A list of lines formatted as:

```
INT
```

This indicates the number of rows (equal to the number of columns) in the matrix-valued PSD variable. The number of lines should match the number stated in the header.

VAR

Description: Construct the scalar variables.

`HEADER`: One line formatted as:

```
INT INT
```

This is the number of scalar variables, followed by the number of conic domains they are restricted to.

`BODY`: A list of lines formatted as:

```
STR INT
```

This indicates the cone name (see Table 14.3), and the number of scalar variables restricted to this cone. These numbers should add up to the number of scalar variables stated first in the header. The number of lines should match the second number stated in the header.

INT

Description: Declare integer requirements on a selected subset of scalar variables.

`HEADER`: one line formatted as:

```
INT
```

This is the number of integer scalar variables in the problem.

`BODY`: a list of lines formatted as:

```
INT
```

This indicates the scalar variable index $j \in \mathcal{J}$. The number of lines should match the number stated in the header.

Can only be used after the keyword `VAR`.

PSDCON

Description: Construct the PSD constraints.

`HEADER`: One line formatted as:

```
INT
```

This is the number of PSD constraints in the problem.

`BODY`: A list of lines formatted as:

```
INT
```

This indicates the number of rows (equal to the number of columns) in the matrix-valued affine expression of the PSD constraint. The number of lines should match the number stated in the header.

Can only be used after these keywords: `PSDVAR`, `VAR`.

CON

Description: Construct the scalar constraints.

`HEADER`: One line formatted as:

```
INT INT
```

This is the number of scalar constraints, followed by the number of conic domains they restrict to.

`BODY`: A list of lines formatted as:

```
STR INT
```

This indicates the cone name (see Table 14.3), and the number of affine expressions restricted to this cone. These numbers should add up to the number of scalar constraints stated first in the header. The number of lines should match the second number stated in the header.

Can only be used after these keywords: `PSDVAR`, `VAR`

OBJFCOORD

Description: Input sparse coordinates (quadruplets) to define the symmetric matrices F_j^{obj}, as used in the objective.

`HEADER`: One line formatted as:

```
INT
```

This is the number of coordinates to be specified.

`BODY`: A list of lines formatted as:

```
INT INT INT REAL
```

This indicates the PSD variable index $j \in \mathcal{J}^{PSD}$, the row index, the column index and the coefficient value. The number of lines should match the number stated in the header.

OBJACOORD

Description: Input sparse coordinates (pairs) to define the scalars, a_j^{obj}, as used in the objective.

`HEADER`: One line formatted as:

```
INT
```

This is the number of coordinates to be specified.

`BODY`: A list of lines formatted as:

```
INT REAL
```

This indicates the scalar variable index $j \in \mathcal{J}$ and the coefficient value. The number of lines should match the number stated in the header.

OBJBCOORD

Description: Input the scalar, b^{obj}, as used in the objective.

`HEADER`: None.

`BODY`: One line formatted as:

```
REAL
```

This indicates the coefficient value.

FCOORD

Description: Input sparse coordinates (quintuplets) to define the symmetric matrices, F_{ij}, as used in the scalar constraints.

`HEADER`: One line formatted as:

```
INT
```

This is the number of coordinates to be specified.

`BODY`: A list of lines formatted as:

```
INT INT INT INT REAL
```

This indicates the scalar constraint index $i \in \mathcal{I}$, the PSD variable index $j \in \mathcal{J}^{PSD}$, the row index, the column index and the coefficient value. The number of lines should match the number stated in the header.

ACOORD

Description: Input sparse coordinates (triplets) to define the scalars, a_{ij}, as used in the scalar constraints.

`HEADER`: One line formatted as:

```
INT
```

This is the number of coordinates to be specified.

`BODY`: A list of lines formatted as:

```
INT INT REAL
```

This indicates the scalar constraint index $i \in \mathcal{I}$, the scalar variable index $j \in \mathcal{J}$ and the coefficient value. The number of lines should match the number stated in the header.

BCOORD

Description: Input sparse coordinates (pairs) to define the scalars, b_i, as used in the scalar constraints.

`HEADER`: One line formatted as:

```
INT
```

This is the number of coordinates to be specified.

`BODY`: A list of lines formatted as:

```
INT REAL
```

This indicates the scalar constraint index $i \in \mathcal{I}$ and the coefficient value. The number of lines should match the number stated in the header.

HCOORD

Description: Input sparse coordinates (quintuplets) to define the symmetric matrices, H_{ij}, as used in the PSD constraints.

`HEADER`: One line formatted as:

```
INT
```

This is the number of coordinates to be specified.

`BODY`: A list of lines formatted as

```
INT INT INT INT REAL
```

This indicates the PSD constraint index $i \in \mathcal{I}^{PSD}$, the scalar variable index $j \in \mathcal{J}$, the row index, the column index and the coefficient value. The number of lines should match the number stated in the header.

DCOORD

Description: Input sparse coordinates (quadruplets) to define the symmetric matrices, D_i, as used in the PSD constraints.

`HEADER`: One line formatted as

```
INT
```

This is the number of coordinates to be specified.

`BODY`: A list of lines formatted as:

```
INT INT INT REAL
```

This indicates the PSD constraint index $i \in \mathcal{I}^{PSD}$, the row index, the column index and the coefficient value. The number of lines should match the number stated in the header.

CHANGE

Start of a new instance specification based on changes to the previous. Can be interpreted as the end of file when the hotstart-sequence is unsupported or undesired.

`BODY`: None

`Header`: None

14.4.5 CBF Format Examples

Minimal Working Example

The conic optimization problem (14.6) , has three variables in a quadratic cone - first one is integer - and an affine expression in domain 0 (equality constraint).

$$\begin{array}{ll} \text{minimize} & 5.1\,x_0 \\ \text{subject to} & 6.2\,x_1 + 7.3\,x_2 - 8.4 \in \{0\} \\ & x \in \mathcal{Q}^3,\ x_0 \in \mathbb{Z}. \end{array} \tag{14.6}$$

Its formulation in the Conic Benchmark Format begins with the version of the CBF format used, to safeguard against later revisions.

```
VER
1
```

Next follows the problem structure, consisting of the objective sense, the number and domain of variables, the indices of integer variables, and the number and domain of scalar-valued affine expressions (i.e., the equality constraint).

```
OBJSENSE
MIN

VAR
3 1
Q 3

INT
1
0

CON
1 1
L= 1
```

Finally follows the problem data, consisting of the coefficients of the objective, the coefficients of the constraints, and the constant terms of the constraints. All data is specified on a sparse coordinate form.

```
OBJACOORD
1
0 5.1

ACOORD
2
0 1 6.2
0 2 7.3

BCOORD
1
0 -8.4
```

This concludes the example.

Mixing Linear, Second-order and Semidefinite Cones

The conic optimization problem (14.7), has a semidefinite cone, a quadratic cone over unordered subindices, and two equality constraints.

$$\begin{array}{lll} \text{minimize} & \left\langle \begin{bmatrix} 2 & 1 & 0 \\ 1 & 2 & 1 \\ 0 & 1 & 2 \end{bmatrix}, X_1 \right\rangle + x_1 & \\ \text{subject to} & \left\langle \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}, X_1 \right\rangle + x_1 & = \quad 1.0\,, \\ & \left\langle \begin{bmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{bmatrix}, X_1 \right\rangle + x_0 + x_2 & = \quad 0.5\,, \\ & x_1 \geq \sqrt{x_0^2 + x_2^2}\,, & \\ & X_1 \succeq \mathbf{0}\,. & \end{array} \tag{14.7}$$

The equality constraints are easily rewritten to the conic form, $(g_0, g_1) \in \{0\}^2$, by moving constants such that the right-hand-side becomes zero. The quadratic cone does not fit under the `VAR` keyword in this variable permutation. Instead, it takes a scalar constraint $(g_2, g_3, g_4) = (x_1, x_0, x_2) \in \mathcal{Q}^3$, with scalar variables constructed as $(x_0, x_1, x_2) \in \mathbb{R}^3$. Its formulation in the CBF format is reported in the following list

```
# File written using this version of the Conic Benchmark Format:
#     | Version 1.
VER
1

# The sense of the objective is:
#     | Minimize.
OBJSENSE
MIN

# One PSD variable of this size:
#     | Three times three.
PSDVAR
1
3

# Three scalar variables in this one conic domain:
#     | Three are free.
VAR
3 1
F 3

# Five scalar constraints with affine expressions in two conic domains:
#     | Two are fixed to zero.
#     | Three are in conic quadratic domain.
CON
5 2
L= 2
Q 3

# Five coordinates in F^{obj}_j coefficients:
#     | F^{obj}[0][0,0] = 2.0
#     | F^{obj}[0][1,0] = 1.0
#     | and more...
OBJFCOORD
5
0 0 0 2.0
0 1 0 1.0
0 1 1 2.0
```

```
0 2 1 1.0
0 2 2 2.0

# One coordinate in a^{obj}_j coefficients:
#     | a^{obj}[1] = 1.0
OBJACOORD
1
1 1.0

# Nine coordinates in F_ij coefficients:
#     | F[0,0][0,0] = 1.0
#     | F[0,0][1,1] = 1.0
#     | and more...
FCOORD
9
0 0 0 0 1.0
0 0 1 1 1.0
0 0 2 2 1.0
1 0 0 0 1.0
1 0 1 0 1.0
1 0 2 0 1.0
1 0 1 1 1.0
1 0 2 1 1.0
1 0 2 2 1.0

# Six coordinates in a_ij coefficients:
#     | a[0,1] = 1.0
#     | a[1,0] = 1.0
#     | and more...
ACOORD
6
0 1 1.0
1 0 1.0
1 2 1.0
2 1 1.0
3 0 1.0
4 2 1.0

# Two coordinates in b_i coefficients:
#     | b[0] = -1.0
#     | b[1] = -0.5
BCOORD
2
0 -1.0
1 -0.5
```

Mixing Semidefinite Variables and Linear Matrix Inequalities

The standard forms in semidefinite optimization are usually based either on semidefinite variables or linear matrix inequalities. In the CBF format, both forms are supported and can even be mixed as shown in.

$$\begin{array}{lll} \text{minimize} & \left\langle \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}, X_1 \right\rangle + x_1 + x_2 + 1 & \\ \text{subject to} & \left\langle \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix}, X_1 \right\rangle - x_1 - x_2 & \geq \quad 0.0\,, \\ & x_1 \begin{bmatrix} 0 & 1 \\ 1 & 3 \end{bmatrix} + x_2 \begin{bmatrix} 3 & 1 \\ 1 & 0 \end{bmatrix} - \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} & \succeq \quad \mathbf{0}\,, \\ & X_1 \succeq \mathbf{0}\,. & \end{array} \tag{14.8}$$

Its formulation in the CBF format is written in what follows

```
# File written using this version of the Conic Benchmark Format:
#     | Version 1.
VER
1

# The sense of the objective is:
#     | Minimize.
OBJSENSE
MIN

# One PSD variable of this size:
#     | Two times two.
PSDVAR
1
2

# Two scalar variables in this one conic domain:
#     | Two are free.
VAR
2 1
F 2

# One PSD constraint of this size:
#     | Two times two.
PSDCON
1
2

# One scalar constraint with an affine expression in this one conic domain:
#     | One is greater than or equal to zero.
CON
1 1
L+ 1

# Two coordinates in F^{obj}_j coefficients:
#     | F^{obj}[0][0,0] = 1.0
#     | F^{obj}[0][1,1] = 1.0
OBJFCOORD
2
0 0 0 1.0
0 1 1 1.0

# Two coordinates in a^{obj}_j coefficients:
#     | a^{obj}[0] = 1.0
#     | a^{obj}[1] = 1.0
OBJACOORD
2
0 1.0
1 1.0

# One coordinate in b^{obj} coefficient:
#     | b^{obj} = 1.0
OBJBCOORD
1.0

# One coordinate in F_ij coefficients:
#     | F[0,0][1,0] = 1.0
FCOORD
1
0 0 1 0 1.0

# Two coordinates in a_ij coefficients:
#     | a[0,0] = -1.0
```

```
#     | a[0,1] = -1.0
ACOORD
2
0 0 -1.0
0 1 -1.0

# Four coordinates in H_ij coefficients:
#     | H[0,0][1,0] = 1.0
#     | H[0,0][1,1] = 3.0
#     | and more...
HCOORD
4
0 0 1 0 1.0
0 0 1 1 3.0
0 1 0 0 3.0
0 1 1 0 1.0

# Two coordinates in D_i coefficients:
#     | D[0][0,0] = -1.0
#     | D[0][1,1] = -1.0
DCOORD
2
0 0 0 -1.0
0 1 1 -1.0
```

Optimization Over a Sequence of Objectives

The linear optimization problem (14.9), is defined for a sequence of objectives such that hotstarting from one to the next might be advantages.

$$\begin{array}{lll} \text{maximize}_k & g_k^{obj} & \\ \text{subject to} & 50\,x_0 + 31 & \leq \quad 250\,, \\ & 3\,x_0 - 2x_1 & \geq \quad -4\,, \\ & x \in \mathbb{R}^2_+, & \end{array} \tag{14.9}$$

given,

1. $g_0^{obj} = x_0 + 0.64x_1$.
2. $g_1^{obj} = 1.11x_0 + 0.76x_1$.
3. $g_2^{obj} = 1.11x_0 + 0.85x_1$.

Its formulation in the CBF format is reported in Listing 14.5.

Listing 14.5: Problem (14.9) in CBF format.

```
# File written using this version of the Conic Benchmark Format:
#     | Version 1.
VER
1

# The sense of the objective is:
#     | Maximize.
OBJSENSE
MAX

# Two scalar variables in this one conic domain:
#     | Two are nonnegative.
VAR
2 1
L+ 2
```

```
# Two scalar constraints with affine expressions in these two conic domains:
#     | One is in the nonpositive domain.
#     | One is in the nonnegative domain.
CON
2 2
L- 1
L+ 1

# Two coordinates in a^{obj}_j coefficients:
#     | a^{obj}[0] = 1.0
#     | a^{obj}[1] = 0.64
OBJACOORD
2
0 1.0
1 0.64

# Four coordinates in a_ij coefficients:
#     | a[0,0] = 50.0
#     | a[1,0] = 3.0
#     | and more...
ACOORD
4
0 0 50.0
1 0 3.0
0 1 31.0
1 1 -2.0

# Two coordinates in b_i coefficients:
#     | b[0] = -250.0
#     | b[1] = 4.0
BCOORD
2
0 -250.0
1 4.0

# New problem instance defined in terms of changes.
CHANGE

# Two coordinate changes in a^{obj}_j coefficients. Now it is:
#     | a^{obj}[0] = 1.11
#     | a^{obj}[1] = 0.76
OBJACOORD
2
0 1.11
1 0.76

# New problem instance defined in terms of changes.
CHANGE

# One coordinate change in a^{obj}_j coefficients. Now it is:
#     | a^{obj}[0] = 1.11
#     | a^{obj}[1] = 0.85
OBJACOORD
1
1 0.85
```

14.5 The XML (OSiL) Format

MOSEK can write data in the standard OSiL xml format. For a definition of the OSiL format please see http://www.optimizationservices.org/.

Only linear constraints (possibly with integer variables) are supported. By default output files with the extension `.xml` are written in the OSiL format.

The parameter *MSK_IPAR_WRITE_XML_MODE* controls if the linear coefficients in the A matrix are written in row or column order.

14.6 The Task Format

The Task format is **MOSEK**'s native binary format. It contains a complete image of a **MOSEK** task, i.e.

- Problem data: Linear, conic quadratic, semidefinite and quadratic data
- Problem item names: Variable names, constraints names, cone names etc.
- Parameter settings
- Solutions

There are a few things to be aware of:

- The task format *does not* support General Convex problems since these are defined by arbitrary user-defined functions.
- Status of a solution read from a file will *always* be unknown.

The format is based on the *TAR* (USTar) file format. This means that the individual pieces of data in a `.task` file can be examined by unpacking it as a *TAR* file. Please note that the inverse may not work: Creating a file using *TAR* will most probably not create a valid **MOSEK** Task file since the order of the entries is important.

14.7 The JSON Format

MOSEK provides the possibility to read/write problems in valid JSON format.

> JSON (JavaScript Object Notation) is a lightweight data-interchange format. It is easy for humans to read and write. It is easy for machines to parse and generate. It is based on a subset of the JavaScript Programming Language, Standard ECMA-262 3rd Edition - December 1999. JSON is a text format that is completely language independent but uses conventions that are familiar to programmers of the C-family of languages, including C, C++, C#, Java, JavaScript, Perl, Python, and many others. These properties make JSON an ideal data-interchange language.

The official JSON website http://www.json.org provides plenty of information along with the format definition.

MOSEK defines two JSON-like formats:

- *jtask*
- *jsol*

Warning: Despite being text-based human-readable formats, *jtask* and *jsol* files will include no indentation and no new-lines, in order to keep the files as compact as possible. We therefore strongly advise to use JSON viewer tools to inspect *jtask* and *jsol* files.

14.7.1 *jtask* format

It stores a problem instance. The *jtask* format contains the same information as a *task format*.

Even though a *jtask* file is human-readable, we do not recommend users to create it by hand, but to rely on **MOSEK**.

14.7.2 *jsol* format

It stores a problem solution. The *jsol* format contains all solutions and information items.

14.7.3 A *jtask* example

In Listing 14.6 we present a file in the *jtask* format that corresponds to the sample problem from `lo1.lp`. The listing has been formatted for readability.

Listing 14.6: A formatted *jtask* file for the `lo1.lp` example.

```
{
    "$schema":"http://mosek.com/json/schema#",
    "Task/INFO":{
        "taskname":"lo1",
        "numvar":4,
        "numcon":3,
        "numcone":0,
        "numbarvar":0,
        "numanz":9,
        "numsymmat":0,
        "mosekver":[
            8,
            0,
            0,
            9
        ]
    },
    "Task/data":{
        "var":{
            "name":[
                "x1",
                "x2",
                "x3",
                "x4"
            ],
            "bk":[
                "lo",
                "ra",
                "lo",
                "lo"
            ],
            "bl":[
                0.0,
                0.0,
                0.0,
                0.0
            ],
            "bu":[
                1e+30,
                1e+1,
                1e+30,
                1e+30
            ],
```

```
            "type":[
                "cont",
                "cont",
                "cont",
                "cont"
            ]
        },
        "con":{
            "name":[
                "c1",
                "c2",
                "c3"
            ],
            "bk":[
                "fx",
                "lo",
                "up"
            ],
            "bl":[
                3e+1,
                1.5e+1,
                    -1e+30
            ],
            "bu":[
                3e+1,
                1e+30,
                2.5e+1
            ]
        },
        "objective":{
            "sense":"max",
            "name":"obj",
            "c":{
                "subj":[
                    0,
                    1,
                    2,
                    3
                ],
                "val":[
                    3e+0,
                    1e+0,
                    5e+0,
                    1e+0
                ]
            },
            "cfix":0.0
        },
        "A":{
            "subi":[
                0,
                0,
                0,
                1,
                1,
                1,
                1,
                2,
                2
            ],
            "subj":[
                0,
                1,
```

```
                2,
                0,
                1,
                2,
                3,
                1,
                3
            ],
            "val":[
                3e+0,
                1e+0,
                2e+0,
                2e+0,
                1e+0,
                3e+0,
                1e+0,
                2e+0,
                3e+0
            ]
        }
    },
    "Task/parameters":{
        "iparam":{
            "ANA_SOL_BASIS":"ON",
            "ANA_SOL_PRINT_VIOLATED":"OFF",
            "AUTO_SORT_A_BEFORE_OPT":"OFF",
            "AUTO_UPDATE_SOL_INFO":"OFF",
            "BASIS_SOLVE_USE_PLUS_ONE":"OFF",
            "BI_CLEAN_OPTIMIZER":"OPTIMIZER_FREE",
            "BI_IGNORE_MAX_ITER":"OFF",
            "BI_IGNORE_NUM_ERROR":"OFF",
            "BI_MAX_ITERATIONS":1000000,
            "CACHE_LICENSE":"ON",
            "CHECK_CONVEXITY":"CHECK_CONVEXITY_FULL",
            "COMPRESS_STATFILE":"ON",
            "CONCURRENT_NUM_OPTIMIZERS":2,
            "CONCURRENT_PRIORITY_DUAL_SIMPLEX":2,
            "CONCURRENT_PRIORITY_FREE_SIMPLEX":3,
            "CONCURRENT_PRIORITY_INTPNT":4,
            "CONCURRENT_PRIORITY_PRIMAL_SIMPLEX":1,
            "FEASREPAIR_OPTIMIZE":"FEASREPAIR_OPTIMIZE_NONE",
            "INFEAS_GENERIC_NAMES":"OFF",
            "INFEAS_PREFER_PRIMAL":"ON",
            "INFEAS_REPORT_AUTO":"OFF",
            "INFEAS_REPORT_LEVEL":1,
            "INTPNT_BASIS":"BI_ALWAYS",
            "INTPNT_DIFF_STEP":"ON",
            "INTPNT_FACTOR_DEBUG_LVL":0,
            "INTPNT_FACTOR_METHOD":0,
            "INTPNT_HOTSTART":"INTPNT_HOTSTART_NONE",
            "INTPNT_MAX_ITERATIONS":400,
            "INTPNT_MAX_NUM_COR":-1,
            "INTPNT_MAX_NUM_REFINEMENT_STEPS":-1,
            "INTPNT_OFF_COL_TRH":40,
            "INTPNT_ORDER_METHOD":"ORDER_METHOD_FREE",
            "INTPNT_REGULARIZATION_USE":"ON",
            "INTPNT_SCALING":"SCALING_FREE",
            "INTPNT_SOLVE_FORM":"SOLVE_FREE",
            "INTPNT_STARTING_POINT":"STARTING_POINT_FREE",
            "LIC_TRH_EXPIRY_WRN":7,
            "LICENSE_DEBUG":"OFF",
            "LICENSE_PAUSE_TIME":0,
            "LICENSE_SUPPRESS_EXPIRE_WRNS":"OFF",
```

```
            "LICENSE_WAIT":"OFF",
            "LOG":10,
            "LOG_ANA_PRO":1,
            "LOG_BI":4,
            "LOG_BI_FREQ":2500,
            "LOG_CHECK_CONVEXITY":0,
            "LOG_CONCURRENT":1,
            "LOG_CUT_SECOND_OPT":1,
            "LOG_EXPAND":0,
            "LOG_FACTOR":1,
            "LOG_FEAS_REPAIR":1,
            "LOG_FILE":1,
            "LOG_HEAD":1,
            "LOG_INFEAS_ANA":1,
            "LOG_INTPNT":4,
            "LOG_MIO":4,
            "LOG_MIO_FREQ":1000,
            "LOG_OPTIMIZER":1,
            "LOG_ORDER":1,
            "LOG_PRESOLVE":1,
            "LOG_RESPONSE":0,
            "LOG_SENSITIVITY":1,
            "LOG_SENSITIVITY_OPT":0,
            "LOG_SIM":4,
            "LOG_SIM_FREQ":1000,
            "LOG_SIM_MINOR":1,
            "LOG_STORAGE":1,
            "MAX_NUM_WARNINGS":10,
            "MIO_BRANCH_DIR":"BRANCH_DIR_FREE",
            "MIO_CONSTRUCT_SOL":"OFF",
            "MIO_CUT_CLIQUE":"ON",
            "MIO_CUT_CMIR":"ON",
            "MIO_CUT_GMI":"ON",
            "MIO_CUT_KNAPSACK_COVER":"OFF",
            "MIO_HEURISTIC_LEVEL":-1,
            "MIO_MAX_NUM_BRANCHES":-1,
            "MIO_MAX_NUM_RELAXS":-1,
            "MIO_MAX_NUM_SOLUTIONS":-1,
            "MIO_MODE":"MIO_MODE_SATISFIED",
            "MIO_MT_USER_CB":"ON",
            "MIO_NODE_OPTIMIZER":"OPTIMIZER_FREE",
            "MIO_NODE_SELECTION":"MIO_NODE_SELECTION_FREE",
            "MIO_PERSPECTIVE_REFORMULATE":"ON",
            "MIO_PROBING_LEVEL":-1,
            "MIO_RINS_MAX_NODES":-1,
            "MIO_ROOT_OPTIMIZER":"OPTIMIZER_FREE",
            "MIO_ROOT_REPEAT_PRESOLVE_LEVEL":-1,
            "MT_SPINCOUNT":0,
            "NUM_THREADS":0,
            "OPF_MAX_TERMS_PER_LINE":5,
            "OPF_WRITE_HEADER":"ON",
            "OPF_WRITE_HINTS":"ON",
            "OPF_WRITE_PARAMETERS":"OFF",
            "OPF_WRITE_PROBLEM":"ON",
            "OPF_WRITE_SOL_BAS":"ON",
            "OPF_WRITE_SOL_ITG":"ON",
            "OPF_WRITE_SOL_ITR":"ON",
            "OPF_WRITE_SOLUTIONS":"OFF",
            "OPTIMIZER":"OPTIMIZER_FREE",
            "PARAM_READ_CASE_NAME":"ON",
            "PARAM_READ_IGN_ERROR":"OFF",
            "PRESOLVE_ELIMINATOR_MAX_FILL":-1,
            "PRESOLVE_ELIMINATOR_MAX_NUM_TRIES":-1,
```

```
            "PRESOLVE_LEVEL":-1,
            "PRESOLVE_LINDEP_ABS_WORK_TRH":100,
            "PRESOLVE_LINDEP_REL_WORK_TRH":100,
            "PRESOLVE_LINDEP_USE":"ON",
            "PRESOLVE_MAX_NUM_REDUCTIONS":-1,
            "PRESOLVE_USE":"PRESOLVE_MODE_FREE",
            "PRIMAL_REPAIR_OPTIMIZER":"OPTIMIZER_FREE",
            "QO_SEPARABLE_REFORMULATION":"OFF",
            "READ_DATA_COMPRESSED":"COMPRESS_FREE",
            "READ_DATA_FORMAT":"DATA_FORMAT_EXTENSION",
            "READ_DEBUG":"OFF",
            "READ_KEEP_FREE_CON":"OFF",
            "READ_LP_DROP_NEW_VARS_IN_BOU":"OFF",
            "READ_LP_QUOTED_NAMES":"ON",
            "READ_MPS_FORMAT":"MPS_FORMAT_FREE",
            "READ_MPS_WIDTH":1024,
            "READ_TASK_IGNORE_PARAM":"OFF",
            "SENSITIVITY_ALL":"OFF",
            "SENSITIVITY_OPTIMIZER":"OPTIMIZER_FREE_SIMPLEX",
            "SENSITIVITY_TYPE":"SENSITIVITY_TYPE_BASIS",
            "SIM_BASIS_FACTOR_USE":"ON",
            "SIM_DEGEN":"SIM_DEGEN_FREE",
            "SIM_DUAL_CRASH":90,
            "SIM_DUAL_PHASEONE_METHOD":0,
            "SIM_DUAL_RESTRICT_SELECTION":50,
            "SIM_DUAL_SELECTION":"SIM_SELECTION_FREE",
            "SIM_EXPLOIT_DUPVEC":"SIM_EXPLOIT_DUPVEC_OFF",
            "SIM_HOTSTART":"SIM_HOTSTART_FREE",
            "SIM_HOTSTART_LU":"ON",
            "SIM_INTEGER":0,
            "SIM_MAX_ITERATIONS":10000000,
            "SIM_MAX_NUM_SETBACKS":250,
            "SIM_NON_SINGULAR":"ON",
            "SIM_PRIMAL_CRASH":90,
            "SIM_PRIMAL_PHASEONE_METHOD":0,
            "SIM_PRIMAL_RESTRICT_SELECTION":50,
            "SIM_PRIMAL_SELECTION":"SIM_SELECTION_FREE",
            "SIM_REFACTOR_FREQ":0,
            "SIM_REFORMULATION":"SIM_REFORMULATION_OFF",
            "SIM_SAVE_LU":"OFF",
            "SIM_SCALING":"SCALING_FREE",
            "SIM_SCALING_METHOD":"SCALING_METHOD_POW2",
            "SIM_SOLVE_FORM":"SOLVE_FREE",
            "SIM_STABILITY_PRIORITY":50,
            "SIM_SWITCH_OPTIMIZER":"OFF",
            "SOL_FILTER_KEEP_BASIC":"OFF",
            "SOL_FILTER_KEEP_RANGED":"OFF",
            "SOL_READ_NAME_WIDTH":-1,
            "SOL_READ_WIDTH":1024,
            "SOLUTION_CALLBACK":"OFF",
            "TIMING_LEVEL":1,
            "WRITE_BAS_CONSTRAINTS":"ON",
            "WRITE_BAS_HEAD":"ON",
            "WRITE_BAS_VARIABLES":"ON",
            "WRITE_DATA_COMPRESSED":0,
            "WRITE_DATA_FORMAT":"DATA_FORMAT_EXTENSION",
            "WRITE_DATA_PARAM":"OFF",
            "WRITE_FREE_CON":"OFF",
            "WRITE_GENERIC_NAMES":"OFF",
            "WRITE_GENERIC_NAMES_IO":1,
            "WRITE_IGNORE_INCOMPATIBLE_CONIC_ITEMS":"OFF",
            "WRITE_IGNORE_INCOMPATIBLE_ITEMS":"OFF",
            "WRITE_IGNORE_INCOMPATIBLE_NL_ITEMS":"OFF",
```

```
            "WRITE_IGNORE_INCOMPATIBLE_PSD_ITEMS":"OFF",
            "WRITE_INT_CONSTRAINTS":"ON",
            "WRITE_INT_HEAD":"ON",
            "WRITE_INT_VARIABLES":"ON",
            "WRITE_LP_FULL_OBJ":"ON",
            "WRITE_LP_LINE_WIDTH":80,
            "WRITE_LP_QUOTED_NAMES":"ON",
            "WRITE_LP_STRICT_FORMAT":"OFF",
            "WRITE_LP_TERMS_PER_LINE":10,
            "WRITE_MPS_FORMAT":"MPS_FORMAT_FREE",
            "WRITE_MPS_INT":"ON",
            "WRITE_PRECISION":15,
            "WRITE_SOL_BARVARIABLES":"ON",
            "WRITE_SOL_CONSTRAINTS":"ON",
            "WRITE_SOL_HEAD":"ON",
            "WRITE_SOL_IGNORE_INVALID_NAMES":"OFF",
            "WRITE_SOL_VARIABLES":"ON",
            "WRITE_TASK_INC_SOL":"ON",
            "WRITE_XML_MODE":"WRITE_XML_MODE_ROW"
        },
        "dparam":{
            "ANA_SOL_INFEAS_TOL":1e-6,
            "BASIS_REL_TOL_S":1e-12,
            "BASIS_TOL_S":1e-6,
            "BASIS_TOL_X":1e-6,
            "CHECK_CONVEXITY_REL_TOL":1e-10,
            "DATA_TOL_AIJ":1e-12,
            "DATA_TOL_AIJ_HUGE":1e+20,
            "DATA_TOL_AIJ_LARGE":1e+10,
            "DATA_TOL_BOUND_INF":1e+16,
            "DATA_TOL_BOUND_WRN":1e+8,
            "DATA_TOL_C_HUGE":1e+16,
            "DATA_TOL_CJ_LARGE":1e+8,
            "DATA_TOL_QIJ":1e-16,
            "DATA_TOL_X":1e-8,
            "FEASREPAIR_TOL":1e-10,
            "INTPNT_CO_TOL_DFEAS":1e-8,
            "INTPNT_CO_TOL_INFEAS":1e-10,
            "INTPNT_CO_TOL_MU_RED":1e-8,
            "INTPNT_CO_TOL_NEAR_REL":1e+3,
            "INTPNT_CO_TOL_PFEAS":1e-8,
            "INTPNT_CO_TOL_REL_GAP":1e-7,
            "INTPNT_NL_MERIT_BAL":1e-4,
            "INTPNT_NL_TOL_DFEAS":1e-8,
            "INTPNT_NL_TOL_MU_RED":1e-12,
            "INTPNT_NL_TOL_NEAR_REL":1e+3,
            "INTPNT_NL_TOL_PFEAS":1e-8,
            "INTPNT_NL_TOL_REL_GAP":1e-6,
            "INTPNT_NL_TOL_REL_STEP":9.95e-1,
            "INTPNT_QO_TOL_DFEAS":1e-8,
            "INTPNT_QO_TOL_INFEAS":1e-10,
            "INTPNT_QO_TOL_MU_RED":1e-8,
            "INTPNT_QO_TOL_NEAR_REL":1e+3,
            "INTPNT_QO_TOL_PFEAS":1e-8,
            "INTPNT_QO_TOL_REL_GAP":1e-8,
            "INTPNT_TOL_DFEAS":1e-8,
            "INTPNT_TOL_DSAFE":1e+0,
            "INTPNT_TOL_INFEAS":1e-10,
            "INTPNT_TOL_MU_RED":1e-16,
            "INTPNT_TOL_PATH":1e-8,
            "INTPNT_TOL_PFEAS":1e-8,
            "INTPNT_TOL_PSAFE":1e+0,
            "INTPNT_TOL_REL_GAP":1e-8,
```

```
            "INTPNT_TOL_REL_STEP":9.999e-1,
            "INTPNT_TOL_STEP_SIZE":1e-6,
            "LOWER_OBJ_CUT":-1e+30,
            "LOWER_OBJ_CUT_FINITE_TRH":-5e+29,
            "MIO_DISABLE_TERM_TIME":-1e+0,
            "MIO_MAX_TIME":-1e+0,
            "MIO_MAX_TIME_APRX_OPT":6e+1,
            "MIO_NEAR_TOL_ABS_GAP":0.0,
            "MIO_NEAR_TOL_REL_GAP":1e-3,
            "MIO_REL_GAP_CONST":1e-10,
            "MIO_TOL_ABS_GAP":0.0,
            "MIO_TOL_ABS_RELAX_INT":1e-5,
            "MIO_TOL_FEAS":1e-6,
            "MIO_TOL_REL_DUAL_BOUND_IMPROVEMENT":0.0,
            "MIO_TOL_REL_GAP":1e-4,
            "MIO_TOL_X":1e-6,
            "OPTIMIZER_MAX_TIME":-1e+0,
            "PRESOLVE_TOL_ABS_LINDEP":1e-6,
            "PRESOLVE_TOL_AIJ":1e-12,
            "PRESOLVE_TOL_REL_LINDEP":1e-10,
            "PRESOLVE_TOL_S":1e-8,
            "PRESOLVE_TOL_X":1e-8,
            "QCQO_REFORMULATE_REL_DROP_TOL":1e-15,
            "SEMIDEFINITE_TOL_APPROX":1e-10,
            "SIM_LU_TOL_REL_PIV":1e-2,
            "SIMPLEX_ABS_TOL_PIV":1e-7,
            "UPPER_OBJ_CUT":1e+30,
            "UPPER_OBJ_CUT_FINITE_TRH":5e+29
        },
        "sparam":{
            "BAS_SOL_FILE_NAME":"",
            "DATA_FILE_NAME":"examples/tools/data/lo1.mps",
            "DEBUG_FILE_NAME":"",
            "INT_SOL_FILE_NAME":"",
            "ITR_SOL_FILE_NAME":"",
            "MIO_DEBUG_STRING":"",
            "PARAM_COMMENT_SIGN":"%%",
            "PARAM_READ_FILE_NAME":"",
            "PARAM_WRITE_FILE_NAME":"",
            "READ_MPS_BOU_NAME":"",
            "READ_MPS_OBJ_NAME":"",
            "READ_MPS_RAN_NAME":"",
            "READ_MPS_RHS_NAME":"",
            "SENSITIVITY_FILE_NAME":"",
            "SENSITIVITY_RES_FILE_NAME":"",
            "SOL_FILTER_XC_LOW":"",
            "SOL_FILTER_XC_UPR":"",
            "SOL_FILTER_XX_LOW":"",
            "SOL_FILTER_XX_UPR":"",
            "STAT_FILE_NAME":"",
            "STAT_KEY":"",
            "STAT_NAME":"",
            "WRITE_LP_GEN_VAR_NAME":"XMSKGEN"
        }
    }
}
```


14.8 The Solution File Format

MOSEK provides several solution files depending on the problem type and the optimizer used:

- *basis solution file* (extension `.bas`) if the problem is optimized using the simplex optimizer or basis identification is performed,
- *interior solution file* (extension `.sol`) if a problem is optimized using the interior-point optimizer and no basis identification is required,
- *integer solution file* (extension `.int`) if the problem contains integer constrained variables.

All solution files have the format:

```
NAME                : <problem name>
PROBLEM STATUS      : <status of the problem>
SOLUTION STATUS     : <status of the solution>
OBJECTIVE NAME      : <name of the objective function>
PRIMAL OBJECTIVE    : <primal objective value corresponding to the solution>
DUAL OBJECTIVE      : <dual objective value corresponding to the solution>
CONSTRAINTS
INDEX  NAME     AT ACTIVITY    LOWER LIMIT   UPPER LIMIT   DUAL LOWER   DUAL UPPER
?      <name>   ?? <a value>   <a value>     <a value>     <a value>    <a value>
VARIABLES
INDEX  NAME     AT ACTIVITY    LOWER LIMIT   UPPER LIMIT   DUAL LOWER   DUAL UPPER    CONIC␣
↪DUAL
?      <name>   ?? <a value>   <a value>     <a value>     <a value>    <a value>     <a value>
```

In the example the fields `?` and `<>` will be filled with problem and solution specific information. As can be observed a solution report consists of three sections, i.e.

- `HEADER` In this section, first the name of the problem is listed and afterwards the problem and solution status are shown. Next the primal and dual objective values are displayed.
- `CONSTRAINTS` For each constraint i of the form

$$l_i^c \leq \sum_{j=1}^{n} a_{ij} x_j \leq u_i^c, \tag{14.10}$$

  the following information is listed:

  - `INDEX`: A sequential index assigned to the constraint by **MOSEK**
  - `NAME`: The name of the constraint assigned by the user.
  - `AT`: The status of the constraint. In Table 14.4 the possible values of the status keys and their interpretation are shown.

Table 14.4: Status keys.

Status key	Interpretation
`UN`	Unknown status
`BS`	Is basic
`SB`	Is superbasic
`LL`	Is at the lower limit (bound)
`UL`	Is at the upper limit (bound)
`EQ`	Lower limit is identical to upper limit
`**`	Is infeasible i.e. the lower limit is greater than the upper limit.

  - `ACTIVITY`: the quantity $\sum_{j=1}^{n} a_{ij} x_j^*$, where x^* is the value of the primal solution.
  - `LOWER LIMIT`: the quantity l_i^c (see (14.10).)
  - `UPPER LIMIT`: the quantity u_i^c (see (14.10).)
  - `DUAL LOWER`: the dual multiplier corresponding to the lower limit on the constraint.
  - `DUAL UPPER`: the dual multiplier corresponding to the upper limit on the constraint.

- `VARIABLES` The last section of the solution report lists information about the variables. This information has a similar interpretation as for the constraints. However, the column with the header `CONIC DUAL` is included for problems having one or more conic constraints. This column shows the dual variables corresponding to the conic constraints.

Example: `lo1.sol`

In Listing 14.7 we show the solution file for the `lo1.opf` problem.

Listing 14.7: An example of `.sol` file.

```
NAME                 :
PROBLEM STATUS       : PRIMAL_AND_DUAL_FEASIBLE
SOLUTION STATUS      : OPTIMAL
OBJECTIVE NAME       : obj
PRIMAL OBJECTIVE     : 8.33333333e+01
DUAL OBJECTIVE       : 8.33333332e+01

CONSTRAINTS
INDEX      NAME           AT ACTIVITY                LOWER LIMIT        UPPER LIMIT       ␣
 ↪DUAL LOWER              DUAL UPPER
0          c1             EQ 3.00000000000000e+01    3.00000000e+01     3.00000000e+01     -0.
 ↪00000000000000e+00    -2.49999999741654e+00
1          c2             SB 5.33333333049188e+01    1.50000000e+01     NONE               2.
 ↪09157603759397e-10     -0.00000000000000e+00
2          c3             UL 2.49999999842049e+01    NONE               2.50000000e+01     -0.
 ↪00000000000000e+00    -3.33333332895110e-01

VARIABLES
INDEX      NAME           AT ACTIVITY                LOWER LIMIT        UPPER LIMIT       ␣
 ↪DUAL LOWER              DUAL UPPER
0          x1             LL 1.67020427073508e-09    0.00000000e+00     NONE               -4.
 ↪49999999528055e+00    -0.00000000000000e+00
1          x2             LL 2.93510446280504e-09    0.00000000e+00     1.00000000e+01     -2.
 ↪16666666494916e+00    6.20863861687316e-10
2          x3             SB 1.49999999899425e+01    0.00000000e+00     NONE               -8.
 ↪79123177454657e-10    -0.00000000000000e+00
3          x4             SB 8.33333332273116e+00    0.00000000e+00     NONE               -1.
 ↪69795978899185e-09    -0.00000000000000e+00
```

CHAPTER

FIFTEEN

LIST OF EXAMPLES

List of examples shipped in the distribution of Command Line Tools:

Table 15.1: List of distributed examples

File	Description
`25fv47.mps`	A large linear problem from the Netlib library
`ampl1.res`	Interfacing **MOSEK** from AMPL
`ampl2.res`	Interfacing **MOSEK** from AMPL
`ampl3.res`	Interfacing **MOSEK** from AMPL
`cqo1.mps`	A simple conic quadratic problem
`dgo.f`	Nonlinear part of a geometric optimization example `dgo.mps`
`dgo.mps`	Linear part of a geometric optimization example
`diet.dat`	Data for the diet example `diet.mod`
`diet.mod`	A diet balancing AMPL example
`dinfeas.lp`	A simple dual infeasible linear problem
`expopt1.eo`	Data file with an exponential optimization problem
`feasrepair.lp`	An example demonstrating repair of infeasible problems
`infeas.lp`	A simple primal infeasible problem
`lo1.mps`	A simple linear problem
`qo1.mps`	A simple quadratic problem
`sensitivity.ssp`	Sensitivity analysis specification for `transport.lp`
`transport.lp`	A linear problem in the sensitivity analysis example

Additional examples can be found on the **MOSEK** website and in other **MOSEK** publications.

CHAPTER

SIXTEEN

INTERFACE CHANGES

The section show interface-specific changes to the **MOSEK** Command Line Tools in version 8. See the release notes for general changes and new features of the **MOSEK** Optimization Suite.

16.1 Compatibility

16.2 Parameters

Added

- *MSK_DPAR_DATA_SYM_MAT_TOL*
- *MSK_DPAR_DATA_SYM_MAT_TOL_HUGE*
- *MSK_DPAR_DATA_SYM_MAT_TOL_LARGE*
- *MSK_DPAR_INTPNT_QO_TOL_DFEAS*
- *MSK_DPAR_INTPNT_QO_TOL_INFEAS*
- *MSK_DPAR_INTPNT_QO_TOL_MU_RED*
- *MSK_DPAR_INTPNT_QO_TOL_NEAR_REL*
- *MSK_DPAR_INTPNT_QO_TOL_PFEAS*
- *MSK_DPAR_INTPNT_QO_TOL_REL_GAP*
- *MSK_DPAR_SEMIDEFINITE_TOL_APPROX*
- *MSK_IPAR_INTPNT_MULTI_THREAD*
- *MSK_IPAR_LICENSE_TRH_EXPIRY_WRN*
- *MSK_IPAR_LOG_ANA_PRO*
- *MSK_IPAR_MIO_CUT_CLIQUE*
- *MSK_IPAR_MIO_CUT_GMI*
- *MSK_IPAR_MIO_CUT_IMPLIED_BOUND*
- *MSK_IPAR_MIO_CUT_KNAPSACK_COVER*
- *MSK_IPAR_MIO_CUT_SELECTION_LEVEL*
- *MSK_IPAR_MIO_PERSPECTIVE_REFORMULATE*
- *MSK_IPAR_MIO_ROOT_REPEAT_PRESOLVE_LEVEL*
- *MSK_IPAR_MIO_VB_DETECTION_LEVEL*
- *MSK_IPAR_PRESOLVE_ELIMINATOR_MAX_FILL*

- *MSK_IPAR_REMOVE_UNUSED_SOLUTIONS*
- *MSK_IPAR_WRITE_LP_FULL_OBJ*
- *MSK_IPAR_WRITE_MPS_FORMAT*
- *MSK_SPAR_REMOTE_ACCESS_TOKEN*

Removed

- MSK_DPAR_FEASREPAIR_TOL
- MSK_DPAR_MIO_HEURISTIC_TIME
- MSK_DPAR_MIO_MAX_TIME_APRX_OPT
- MSK_DPAR_MIO_REL_ADD_CUT_LIMITED
- MSK_DPAR_MIO_TOL_MAX_CUT_FRAC_RHS
- MSK_DPAR_MIO_TOL_MIN_CUT_FRAC_RHS
- MSK_DPAR_MIO_TOL_REL_RELAX_INT
- MSK_DPAR_MIO_TOL_X
- MSK_DPAR_NONCONVEX_TOL_FEAS
- MSK_DPAR_NONCONVEX_TOL_OPT
- MSK_IPAR_ALLOC_ADD_QNZ
- MSK_IPAR_CONCURRENT_NUM_OPTIMIZERS
- MSK_IPAR_CONCURRENT_PRIORITY_DUAL_SIMPLEX
- MSK_IPAR_CONCURRENT_PRIORITY_FREE_SIMPLEX
- MSK_IPAR_CONCURRENT_PRIORITY_INTPNT
- MSK_IPAR_CONCURRENT_PRIORITY_PRIMAL_SIMPLEX
- MSK_IPAR_FEASREPAIR_OPTIMIZE
- MSK_IPAR_INTPNT_FACTOR_DEBUG_LVL
- MSK_IPAR_INTPNT_FACTOR_METHOD
- MSK_IPAR_LIC_TRH_EXPIRY_WRN
- MSK_IPAR_LOG_CONCURRENT
- MSK_IPAR_LOG_FACTOR
- MSK_IPAR_LOG_HEAD
- MSK_IPAR_LOG_NONCONVEX
- MSK_IPAR_LOG_OPTIMIZER
- MSK_IPAR_LOG_PARAM
- MSK_IPAR_LOG_SIM_NETWORK_FREQ
- MSK_IPAR_MIO_BRANCH_PRIORITIES_USE
- MSK_IPAR_MIO_CONT_SOL
- MSK_IPAR_MIO_CUT_CG
- MSK_IPAR_MIO_CUT_LEVEL_ROOT
- MSK_IPAR_MIO_CUT_LEVEL_TREE
- MSK_IPAR_MIO_FEASPUMP_LEVEL

- MSK_IPAR_MIO_HOTSTART
- MSK_IPAR_MIO_KEEP_BASIS
- MSK_IPAR_MIO_LOCAL_BRANCH_NUMBER
- MSK_IPAR_MIO_OPTIMIZER_MODE
- MSK_IPAR_MIO_PRESOLVE_AGGREGATE
- MSK_IPAR_MIO_PRESOLVE_PROBING
- MSK_IPAR_MIO_PRESOLVE_USE
- MSK_IPAR_MIO_STRONG_BRANCH
- MSK_IPAR_MIO_USE_MULTITHREADED_OPTIMIZER
- MSK_IPAR_NONCONVEX_MAX_ITERATIONS
- MSK_IPAR_PRESOLVE_ELIM_FILL
- MSK_IPAR_PRESOLVE_ELIMINATOR_USE
- MSK_IPAR_QO_SEPARABLE_REFORMULATION
- MSK_IPAR_READ_ANZ
- MSK_IPAR_READ_CON
- MSK_IPAR_READ_CONE
- MSK_IPAR_READ_MPS_KEEP_INT
- MSK_IPAR_READ_MPS_OBJ_SENSE
- MSK_IPAR_READ_MPS_RELAX
- MSK_IPAR_READ_QNZ
- MSK_IPAR_READ_VAR
- MSK_IPAR_SIM_INTEGER
- MSK_IPAR_WARNING_LEVEL
- MSK_IPAR_WRITE_IGNORE_INCOMPATIBLE_CONIC_ITEMS
- MSK_IPAR_WRITE_IGNORE_INCOMPATIBLE_NL_ITEMS
- MSK_IPAR_WRITE_IGNORE_INCOMPATIBLE_PSD_ITEMS
- MSK_SPAR_FEASREPAIR_NAME_PREFIX
- MSK_SPAR_FEASREPAIR_NAME_SEPARATOR
- MSK_SPAR_FEASREPAIR_NAME_WSUMVIOL

16.3 Constants

Added

- *MSK_BRANCH_DIR_FAR*
- *MSK_BRANCH_DIR_GUIDED*
- *MSK_BRANCH_DIR_NEAR*
- *MSK_BRANCH_DIR_PSEUDOCOST*
- *MSK_BRANCH_DIR_ROOT_LP*

- *MSK_CALLBACK_BEGIN_ROOT_CUTGEN*
- *MSK_CALLBACK_BEGIN_TO_CONIC*
- *MSK_CALLBACK_END_ROOT_CUTGEN*
- *MSK_CALLBACK_END_TO_CONIC*
- *MSK_CALLBACK_IM_ROOT_CUTGEN*
- *MSK_CALLBACK_SOLVING_REMOTE*
- *MSK_DATA_FORMAT_JSON_TASK*
- *MSK_DINF_MIO_CLIQUE_SEPARATION_TIME*
- *MSK_DINF_MIO_CMIR_SEPARATION_TIME*
- *MSK_DINF_MIO_GMI_SEPARATION_TIME*
- *MSK_DINF_MIO_IMPLIED_BOUND_TIME*
- *MSK_DINF_MIO_KNAPSACK_COVER_SEPARATION_TIME*
- *MSK_DINF_QCQO_REFORMULATE_MAX_PERTURBATION*
- *MSK_DINF_QCQO_REFORMULATE_WORST_CHOLESKY_COLUMN_SCALING*
- *MSK_DINF_QCQO_REFORMULATE_WORST_CHOLESKY_DIAG_SCALING*
- *MSK_DINF_SOL_BAS_NRM_BARX*
- *MSK_DINF_SOL_BAS_NRM_SLC*
- *MSK_DINF_SOL_BAS_NRM_SLX*
- *MSK_DINF_SOL_BAS_NRM_SUC*
- *MSK_DINF_SOL_BAS_NRM_SUX*
- *MSK_DINF_SOL_BAS_NRM_XC*
- *MSK_DINF_SOL_BAS_NRM_XX*
- *MSK_DINF_SOL_BAS_NRM_Y*
- *MSK_DINF_SOL_ITG_NRM_BARX*
- *MSK_DINF_SOL_ITG_NRM_XC*
- *MSK_DINF_SOL_ITG_NRM_XX*
- *MSK_DINF_SOL_ITR_NRM_BARS*
- *MSK_DINF_SOL_ITR_NRM_BARX*
- *MSK_DINF_SOL_ITR_NRM_SLC*
- *MSK_DINF_SOL_ITR_NRM_SLX*
- *MSK_DINF_SOL_ITR_NRM_SNX*
- *MSK_DINF_SOL_ITR_NRM_SUC*
- *MSK_DINF_SOL_ITR_NRM_SUX*
- *MSK_DINF_SOL_ITR_NRM_XC*
- *MSK_DINF_SOL_ITR_NRM_XX*
- *MSK_DINF_SOL_ITR_NRM_Y*
- *MSK_DINF_TO_CONIC_TIME*
- *MSK_IINF_MIO_ABSGAP_SATISFIED*
- *MSK_IINF_MIO_CLIQUE_TABLE_SIZE*

- *MSK_IINF_MIO_NEAR_ABSGAP_SATISFIED*
- *MSK_IINF_MIO_NEAR_RELGAP_SATISFIED*
- *MSK_IINF_MIO_NODE_DEPTH*
- *MSK_IINF_MIO_NUM_CMIR_CUTS*
- *MSK_IINF_MIO_NUM_IMPLIED_BOUND_CUTS*
- *MSK_IINF_MIO_NUM_KNAPSACK_COVER_CUTS*
- *MSK_IINF_MIO_NUM_REPEATED_PRESOLVE*
- *MSK_IINF_MIO_PRESOLVED_NUMBIN*
- *MSK_IINF_MIO_PRESOLVED_NUMCON*
- *MSK_IINF_MIO_PRESOLVED_NUMCONT*
- *MSK_IINF_MIO_PRESOLVED_NUMINT*
- *MSK_IINF_MIO_PRESOLVED_NUMVAR*
- *MSK_IINF_MIO_RELGAP_SATISFIED*
- *MSK_LIINF_MIO_PRESOLVED_ANZ*
- *MSK_LIINF_MIO_SIM_MAXITER_SETBACKS*
- *MSK_MPS_FORMAT_CPLEX*
- *MSK_SOL_STA_DUAL_ILLPOSED_CER*
- *MSK_SOL_STA_PRIM_ILLPOSED_CER*

Changed

- *MSK_SOL_STA_INTEGER_OPTIMAL*
- *MSK_SOL_STA_NEAR_DUAL_FEAS*
- *MSK_SOL_STA_NEAR_DUAL_INFEAS_CER*
- *MSK_SOL_STA_NEAR_INTEGER_OPTIMAL*
- *MSK_SOL_STA_NEAR_OPTIMAL*
- *MSK_SOL_STA_NEAR_PRIM_AND_DUAL_FEAS*
- *MSK_SOL_STA_NEAR_PRIM_FEAS*
- *MSK_SOL_STA_NEAR_PRIM_INFEAS_CER*
- *MSK_LICENSE_BUFFER_LENGTH*

Removed

- MSK_CALLBACKCODE_BEGIN_CONCURRENT
- MSK_CALLBACKCODE_BEGIN_NETWORK_DUAL_SIMPLEX
- MSK_CALLBACKCODE_BEGIN_NETWORK_PRIMAL_SIMPLEX
- MSK_CALLBACKCODE_BEGIN_NETWORK_SIMPLEX
- MSK_CALLBACKCODE_BEGIN_NONCONVEX
- MSK_CALLBACKCODE_BEGIN_PRIMAL_DUAL_SIMPLEX
- MSK_CALLBACKCODE_BEGIN_PRIMAL_DUAL_SIMPLEX_BI

- MSK_CALLBACKCODE_BEGIN_SIMPLEX_NETWORK_DETECT
- MSK_CALLBACKCODE_END_CONCURRENT
- MSK_CALLBACKCODE_END_NETWORK_DUAL_SIMPLEX
- MSK_CALLBACKCODE_END_NETWORK_PRIMAL_SIMPLEX
- MSK_CALLBACKCODE_END_NETWORK_SIMPLEX
- MSK_CALLBACKCODE_END_NONCONVEX
- MSK_CALLBACKCODE_END_PRIMAL_DUAL_SIMPLEX
- MSK_CALLBACKCODE_END_PRIMAL_DUAL_SIMPLEX_BI
- MSK_CALLBACKCODE_END_SIMPLEX_NETWORK_DETECT
- MSK_CALLBACKCODE_IM_MIO_PRESOLVE
- MSK_CALLBACKCODE_IM_NETWORK_DUAL_SIMPLEX
- MSK_CALLBACKCODE_IM_NETWORK_PRIMAL_SIMPLEX
- MSK_CALLBACKCODE_IM_NONCONVEX
- MSK_CALLBACKCODE_IM_PRIMAL_DUAL_SIMPLEX
- MSK_CALLBACKCODE_NONCOVEX
- MSK_CALLBACKCODE_UPDATE_NETWORK_DUAL_SIMPLEX
- MSK_CALLBACKCODE_UPDATE_NETWORK_PRIMAL_SIMPLEX
- MSK_CALLBACKCODE_UPDATE_NONCONVEX
- MSK_CALLBACKCODE_UPDATE_PRIMAL_DUAL_SIMPLEX
- MSK_CALLBACKCODE_UPDATE_PRIMAL_DUAL_SIMPLEX_BI
- MSK_DINFITEM_BI_CLEAN_PRIMAL_DUAL_TIME
- MSK_DINFITEM_CONCURRENT_TIME
- MSK_DINFITEM_MIO_CG_SEPERATION_TIME
- MSK_DINFITEM_MIO_CMIR_SEPERATION_TIME
- MSK_DINFITEM_SIM_NETWORK_DUAL_TIME
- MSK_DINFITEM_SIM_NETWORK_PRIMAL_TIME
- MSK_DINFITEM_SIM_NETWORK_TIME
- MSK_DINFITEM_SIM_PRIMAL_DUAL_TIME
- MSK_FEATURE_PTOM
- MSK_FEATURE_PTOX
- MSK_IINFITEM_CONCURRENT_FASTEST_OPTIMIZER
- MSK_IINFITEM_MIO_NUM_BASIS_CUTS
- MSK_IINFITEM_MIO_NUM_CARDGUB_CUTS
- MSK_IINFITEM_MIO_NUM_COEF_REDC_CUTS
- MSK_IINFITEM_MIO_NUM_CONTRA_CUTS
- MSK_IINFITEM_MIO_NUM_DISAGG_CUTS
- MSK_IINFITEM_MIO_NUM_FLOW_COVER_CUTS
- MSK_IINFITEM_MIO_NUM_GCD_CUTS
- MSK_IINFITEM_MIO_NUM_GUB_COVER_CUTS

- MSK_IINFITEM_MIO_NUM_KNAPSUR_COVER_CUTS
- MSK_IINFITEM_MIO_NUM_LATTICE_CUTS
- MSK_IINFITEM_MIO_NUM_LIFT_CUTS
- MSK_IINFITEM_MIO_NUM_OBJ_CUTS
- MSK_IINFITEM_MIO_NUM_PLAN_LOC_CUTS
- MSK_IINFITEM_SIM_NETWORK_DUAL_DEG_ITER
- MSK_IINFITEM_SIM_NETWORK_DUAL_HOTSTART
- MSK_IINFITEM_SIM_NETWORK_DUAL_HOTSTART_LU
- MSK_IINFITEM_SIM_NETWORK_DUAL_INF_ITER
- MSK_IINFITEM_SIM_NETWORK_DUAL_ITER
- MSK_IINFITEM_SIM_NETWORK_PRIMAL_DEG_ITER
- MSK_IINFITEM_SIM_NETWORK_PRIMAL_HOTSTART
- MSK_IINFITEM_SIM_NETWORK_PRIMAL_HOTSTART_LU
- MSK_IINFITEM_SIM_NETWORK_PRIMAL_INF_ITER
- MSK_IINFITEM_SIM_NETWORK_PRIMAL_ITER
- MSK_IINFITEM_SIM_PRIMAL_DUAL_DEG_ITER
- MSK_IINFITEM_SIM_PRIMAL_DUAL_HOTSTART
- MSK_IINFITEM_SIM_PRIMAL_DUAL_HOTSTART_LU
- MSK_IINFITEM_SIM_PRIMAL_DUAL_INF_ITER
- MSK_IINFITEM_SIM_PRIMAL_DUAL_ITER
- MSK_IINFITEM_SOL_INT_PROSTA
- MSK_IINFITEM_SOL_INT_SOLSTA
- MSK_IINFITEM_STO_NUM_A_CACHE_FLUSHES
- MSK_IINFITEM_STO_NUM_A_TRANSPOSES
- MSK_LIINFITEM_BI_CLEAN_PRIMAL_DUAL_DEG_ITER
- MSK_LIINFITEM_BI_CLEAN_PRIMAL_DUAL_ITER
- MSK_LIINFITEM_BI_CLEAN_PRIMAL_DUAL_SUB_ITER
- MSK_MIOMODE_LAZY
- MSK_OPTIMIZERTYPE_CONCURRENT
- MSK_OPTIMIZERTYPE_MIXED_INT_CONIC
- MSK_OPTIMIZERTYPE_NETWORK_PRIMAL_SIMPLEX
- MSK_OPTIMIZERTYPE_NONCONVEX
- MSK_OPTIMIZERTYPE_PRIMAL_DUAL_SIMPLEX

16.4 Response Codes

Added

- *MSK_RES_ERR_CBF_DUPLICATE_PSDVAR*

- *MSK_RES_ERR_CBF_INVALID_PSDVAR_DIMENSION*
- *MSK_RES_ERR_CBF_TOO_FEW_PSDVAR*
- *MSK_RES_ERR_DUPLICATE_AIJ*
- *MSK_RES_ERR_FINAL_SOLUTION*
- *MSK_RES_ERR_JSON_DATA*
- *MSK_RES_ERR_JSON_FORMAT*
- *MSK_RES_ERR_JSON_MISSING_DATA*
- *MSK_RES_ERR_JSON_NUMBER_OVERFLOW*
- *MSK_RES_ERR_JSON_STRING*
- *MSK_RES_ERR_JSON_SYNTAX*
- *MSK_RES_ERR_LAU_INVALID_LOWER_TRIANGULAR_MATRIX*
- *MSK_RES_ERR_LAU_INVALID_SPARSE_SYMMETRIC_MATRIX*
- *MSK_RES_ERR_LAU_NOT_POSITIVE_DEFINITE*
- *MSK_RES_ERR_MIXED_CONIC_AND_NL*
- *MSK_RES_ERR_SERVER_CONNECT*
- *MSK_RES_ERR_SERVER_PROTOCOL*
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