



MOSEK Command Line Tools

*Release 8.0.0.83*

MOSEK ApS

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## INTRODUCTION

The **MOSEK** Optimization Suite 8.0.0.83 is a powerful software package capable of solving large-scale optimization problems of the following kind:

- linear,
- convex quadratic,
- conic quadratic (also known as second-order cone),
- semidefinite,
- and general convex.

Integer constrained variables are supported for all problem classes except for semidefinite and general convex problems. In order to obtain an overview of features in the **MOSEK** Optimization Suite consult the [product introduction](#) guide.

### 1.1 Why the Command Line Tools?

The **MOSEK** capabilities can be accessed from the command line without the need to use any programming language. The user can input optimization problems using files in a variety of *formats*, or via the AMPL language shell.

### 1.2 License agreement

Before using the **MOSEK** software, please read the license agreement available in the distribution at <MSKHOME>/mosek/8/mosek-eula.pdf or on the **MOSEK** website <https://mosek.com/sales/license-agreement>.

**MOSEK** uses some third-party open-source libraries. Their license details follows.

#### ***zlib***

**MOSEK** includes the *zlib* library obtained from the [zlib website](#). The license agreement for *zlib* is shown in [Listing 1.1](#).

Listing 1.1: *zlib* license.

```
zlib.h -- interface of the 'zlib' general purpose compression library
version 1.2.7, May 2nd, 2012

Copyright (C) 1995-2012 Jean-loup Gailly and Mark Adler

This software is provided 'as-is', without any express or implied
warranty. In no event will the authors be held liable for any damages
```

arising from the use of this software.

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3. This notice may not be removed or altered from any source distribution.

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### *fplib*

MOSEK includes the floating point formatting library developed by David M. Gay obtained from the [netlib website](#). The license agreement for *fplib* is shown in [Listing 1.2](#).

Listing 1.2: *fplib* license.

```
/*
 *
 * The author of this software is David M. Gay.
 *
 * Copyright (c) 1991, 2000, 2001 by Lucent Technologies.
 *
 * Permission to use, copy, modify, and distribute this software for any
 * purpose without fee is hereby granted, provided that this entire notice
 * is included in all copies of any software which is or includes a copy
 * or modification of this software and in all copies of the supporting
 * documentation for such software.
 *
 * THIS SOFTWARE IS BEING PROVIDED "AS IS", WITHOUT ANY EXPRESS OR IMPLIED
 * WARRANTY. IN PARTICULAR, NEITHER THE AUTHOR NOR LUCENT MAKES ANY
 * REPRESENTATION OR WARRANTY OF ANY KIND CONCERNING THE MERCHANTABILITY
 * OF THIS SOFTWARE OR ITS FITNESS FOR ANY PARTICULAR PURPOSE.
 *
 */
```

## INSTALLATION

After installing **MOSEK** Optimization Suite as described in the [Installation Guide](#) then the command line tool is ready for use.





## THE COMMAND LINE TOOL

### 3.1 Introduction

The **MOSEK** command line tool is used to solve optimization problems from the operating system command line. It is invoked as follows

```
mosek [options] [filename]
```

where both [options] and [filename] are optional arguments:

- [options] consists of command line arguments that modify the behavior of **MOSEK**. They are listed in Section 3.3.
- filename is a file describing the optimization problem. The **MOSEK** command line accepts files in any of the *supported file formats* or in the AMPL *nl* file.

If no arguments are given, **MOSEK** will return its version and platform, i.e.

```
andrea@Bistrup:~$ mosek/8/tools/platform/linux64x86/bin/mosek

MOSEK Version 8.0.0.32(BETA) (Build date: 2016-7-12 10:29:26)
Copyright (c) MOSEK ApS, Denmark. WWW: mosek.com
Platform: Linux/64-X86

*** No input file specified. No optimization is performed.

Return code - 0 [MSK_RES_OK]
```

### 3.2 Command Line Example

In this section there are some examples on how to use the **MOSEK** command line. Please refer to Section 3.3 for the complete list of available command line options.

#### 3.2.1 Solve an Optimization Problem

The simplest case is to solve a problem stored in file, say `lo1.mps`:

```
mosek lo1.mps
```

The solver will

- read `lo1.mps` from disk,
- solve the problem and
- store the relevant solution files (see 12.8) if any solution exists.

These steps are clear from the solver output in the following listing.

```

MOSEK Version 8.0.0.34(BETA) (Build date: 2016-8-24 00:51:13)
Copyright (c) MOSEK ApS, Denmark. WWW: mosek.com
Platform: Linux/64-X86

Open file '/home/andrea/mosek/8/tools/examples/data/lo1.mps'
Reading started.
Using 'obj' as objective vector
Read 13 number of A nonzeros in 0.00 seconds.
Using 'rhs' as rhs vector
Using 'bound' as bound vector
Reading terminated. Time: 0.00

Read summary
  Type           : LO (linear optimization problem)
  Objective sense : max
  Scalar variables : 4
  Matrix variables : 0
  Constraints      : 3
  Cones           : 0
  Time            : 0.0

Problem
  Name           : lo1
  Objective sense : max
  Type           : LO (linear optimization problem)
  Constraints      : 3
  Cones           : 0
  Scalar variables : 4
  Matrix variables : 0
  Integer variables : 0

Optimizer started.
Interior-point optimizer started.
Presolve started.
Linear dependency checker started.
Linear dependency checker terminated.
Eliminator started.
Freed constraints in eliminator : 0
Eliminator terminated.
Eliminator - tries          : 1           time           : 0.00
Lin. dep. - tries          : 1           time           : 0.00
Lin. dep. - number         : 0
Presolve terminated. Time: 0.00
Optimizer - threads        : 2
Optimizer - solved problem : the primal
Optimizer - Constraints     : 3
Optimizer - Cones          : 0
Optimizer - Scalar variables : 6           conic           : 0
Optimizer - Semi-definite variables: 0       scalarized        : 0
Factor - setup time        : 0.00          dense det. time   : 0.00
Factor - ML order time     : 0.00          GP order time     : 0.00
Factor - nonzeros before factor : 6         after factor      : 6
Factor - dense dim.        : 0             flops             : 1.06e+02
ITE PFEAS   DFEAS   GFEAS   PRSTATUS   POBJ          DOBJ          MU          TIME
0  8.0e+00  3.2e+00  3.5e+00  1.00e+00  1.000000000e+01  0.000000000e+00  1.0e+00  0.01
1  4.2e+00  2.5e+00  4.7e-01  0.00e+00  3.093970927e+01  2.766058702e+01  2.6e+00  0.01
2  4.2e-01  2.5e-01  4.6e-02  -1.82e-02  6.511676243e+01  6.308843559e+01  2.6e-01  0.01
3  3.6e-02  2.1e-02  3.9e-03  5.84e-01  8.096141239e+01  8.061962333e+01  2.2e-02  0.01
4  1.5e-05  9.1e-06  1.7e-06  9.43e-01  8.333280389e+01  8.333241803e+01  9.2e-06  0.01
5  1.5e-09  9.1e-10  1.7e-10  1.00e+00  8.333333328e+01  8.333333324e+01  9.2e-10  0.01
Basis identification started.

```

```

Primal basis identification phase started.
ITER      TIME
0         0.00
Primal basis identification phase terminated. Time: 0.00
Dual basis identification phase started.
ITER      TIME
0         0.00
Dual basis identification phase terminated. Time: 0.00
Basis identification terminated. Time: 0.00
Interior-point optimizer terminated. Time: 0.01.

Optimizer terminated. Time: 0.02

Interior-point solution summary
  Problem status : PRIMAL_AND_DUAL_FEASIBLE
  Solution status : OPTIMAL
  Primal.  obj: 8.3333333280e+01    nrm: 5e+01    Viol.  con: 1e-08    var: 0e+00
  Dual.    obj: 8.3333333242e+01    nrm: 4e+00    Viol.  con: 2e-10    var: 5e-09

Basic solution summary
  Problem status : PRIMAL_AND_DUAL_FEASIBLE
  Solution status : OPTIMAL
  Primal.  obj: 8.3333333333e+01    nrm: 5e+01    Viol.  con: 7e-15    var: 0e+00
  Dual.    obj: 8.3333333245e+01    nrm: 4e+00    Viol.  con: 2e-10    var: 5e-09

Optimizer summary
Optimizer              -                time: 0.02
  Interior-point        - iterations : 5      time: 0.01
    Basis identification -                time: 0.00
      Primal            - iterations : 0      time: 0.00
      Dual              - iterations : 0      time: 0.00
      Clean primal      - iterations : 0      time: 0.00
      Clean dual        - iterations : 0      time: 0.00
    Simplex             -                time: 0.00
      Primal simplex    - iterations : 0      time: 0.00
      Dual simplex      - iterations : 0      time: 0.00
      Mixed integer     - relaxations: 0      time: 0.00

Open file '/home/andrea/mosek/8/tools/examples/data/lo1.sol'
Start writing.
done writing. Time: 0.00

Open file '/home/andrea/mosek/8/tools/examples/data/lo1.bas'
Start writing.
done writing. Time: 0.00

Return code - 0  [MSK_RES_OK]

```

### 3.2.2 Change a Solver Parameter

Using the `-d` option it is possible to set the solver parameters. The next command shows how to switch off the presolver and solve a problem stored in a file called `lo1.opf`.

```
mosek -d MSK_IPAR_PRESOLVE_USE MSK_OFF lo1.opf
```

If multiple parameters must be specified, option `-d` must be repeated for each one. For instance say also the time limit must be set:

```
mosek -d MSK_IPAR_PRESOLVE_USE MSK_OFF -d MSK_DPAR_OPTIMIZER_MAX_TIME 1.0 lo1.opf
```

Please refer to [11.1.1](#) for the complete list of available solver parameters.

### 3.2.3 Convert a File

The **MOSEK** command line can also be used to convert between two file formats supported by **MOSEK**. This can be achieved using the `-out` option. Moreover using `-x` the solver will not actually solve the problem.

**Warning:** The target file type must support the problem type of the source file, otherwise the conversion will be partial.

For instance in case a MPS file must be converted in a more readable OPF format, the following line can be used

```
mosek -x -out lo1.opf lo1.mps
```

The output produced is

```
MOSEK Version 8.0.0.34(BETA) (Build date: 2016-8-24 00:51:13)
Copyright (c) MOSEK ApS, Denmark. WWW: mosek.com
Platform: Linux/64-X86

Open file '/home/andrea/mosek/8/tools/examples/data/lo1.mps'
Reading started.
Using 'obj' as objective vector
Read 13 number of A nonzeros in 0.00 seconds.
Using 'rhs' as rhs vector
Using 'bound' as bound vector
Reading terminated. Time: 0.01

Read summary
  Type           : LO (linear optimization problem)
  Objective sense : max
  Scalar variables : 4
  Matrix variables : 0
  Constraints      : 3
  Cones           : 0
  Time            : 0.0

Open file 'lo1.opf'
Start writing.
done writing. Time: 0.00

Return code - 0  [MSK_RES_OK]
```

---

**Note:** The output clearly shows how the solver does not actually solve the given problem.

---

## 3.3 Command Line Arguments

The following list shows the available command-line arguments for **MOSEK**:

- `-anapro`  
Analyze the problem data.
- `-anasoli <name>`  
Analyze the initial solution name e.g. `-anasoli bas`.
- `-anasolo <name>`  
Analyze the final solution name e.g. `-anasolo itg`.

- a  
    **MOSEK** is started in AMPL mode.
- basi <name>  
    Input basis solution file name.
- baso <name>  
    Output basis solution file name.
- d <name> <value>  
    Define the value **value** for the **MOSEK** parameter **name**.
- dbgmem <name>  
    Name of memory debug file.
- f  
    Complete license information is printed.
- h, -?  
    Help.
- inti <name>  
    Input integer solution file name.
- into <name>  
    Output integer solution file name.
- itri <name>  
    Input interior point solution file name.
- itro <name>  
    Output interior point solution file name.
- info <name>  
    Infeasible subproblem output file name.
- infrepo <name>  
    Feasibility reparation output file.
- l, -L <dir>  
    **dir** is the directory where the **MOSEK** license file is located (typically named `mosek.lic`).
- max  
    The problem is maximized.
- min  
    The problem is minimized.
- n  
    Ignore errors in subsequent parameter settings.
- out <name>  
    Write the task to a data file named *name*. See Section 12.
- p <name>, -pari <name>  
    Name of the input parameter file.
- paro <name>  
    Name of the output parameter file.
- r  
    If the option is present, the program returns *-1* if an error occurred otherwise *0*.
- removeitg  
    Removes all integer constraints after reading the problem.
- rout <name>  
    If the option is present, the program writes the return code to file *name*.

`-q <name>`  
Name of a optional log file.

`-sen <file>`  
Perform sensitivity analysis based on file.

`-silent`  
As little information as possible is send to the terminal.

`-toconic`  
Translate to conic form after reading.

`-v`  
**MOSEK** version is printed and no optimization is performed.

`-w`  
If this options is on, then **MOSEK** will wait for a license.

`-x`  
Do not run the optimizer. Useful for converting between file formats.

`--`  
List all possible parameters.

## 3.4 The Parameter File

Occasionally system or algorithmic parameters in **MOSEK** should be changed be the user. One way of changing parameters is to use a so-called parameter file which is a plain text file. It can for example can have the format

```
BEGIN MOSEK
% This is a comment.
% The subsequent line tells MOSEK that an optimal
% basis should be computed by the interior-point optimizer.
MSK_IPAR_INTPNT_BASIS      MSK_BI_ALWAYS
MSK_DPAR_INTPNT_TOL_PFEAS  1.0e-9
END MOSEK
```

Note that the file begins with the line `BEGIN MOSEK` and is terminated with the line `END MOSEK`, this is required. Moreover, everything that appears after an `%` is considered to be a comment and is ignored. Similarly, empty lines are ignored. The important lines are those which begins with a valid **MOSEK** parameter name such as `MSK_IPAR_INTPNT_BASIS`. Immediately after parameter name follows the new value for the parameter. All the **MOSEK** parameter names are listed in Section 11.1.

### Using the parameter file

The parameter file can be given any name, but let us assume it has the name `mosek.par`. If **MOSEK** should use the parameter settings in that file, then `-p` should be on the command line when **MOSEK** is invoked. An example of such a command line is

```
mosek -p mosek.par afiro.mps
```

Command-line parameters override those from the parameter file in case of repetition. For instance

```
mosek -p mosek.par -d MSK_IPAR_NUM_THREAD 1 -d MSK_DPAR_INTPNT_TOL_PFEAS 1.0e-8 afiro.mps
```

will set the `MSK_IPAR_NUM_THREADS` parameter to one, while the the `MSK_DPAR_INTPNT_TOL_PFEAS` will be set to  $10^{-8}$ , using the value provided on the command line.

f.. `_doc.cmd.ampl`:

## THE MOSEK-BUNDLED AMPL SHELL

AMPL is a modeling language for specifying linear and nonlinear optimization models in a natural way. AMPL also makes it easy to solve the problem and e.g. display the solution or part of it.

We will not discuss the specifics of the AMPL language here but instead refer the reader to [FGK03], <http://ampl.com/BOOK/download.html> and the AMPL website <http://www.ampl.com>.

AMPL cannot solve optimization problems by itself but requires a link to an appropriate optimizer such as **MOSEK**. The **MOSEK** distribution includes

- an AMPL link which makes it possible to use **MOSEK** as an optimizer within AMPL,
- the official AMPL interpreter repackaged **mampl** that uses the **MOSEK** license manager instead of the standard AMPL one.

**Warning:** It is possible to specify problems in AMPL that cannot be solved by **MOSEK**. The optimization problem must be a smooth convex optimization problem as discussed in Section 5.

---

**Note:** To use **MOSEK** from AMPL you need to correctly setup the system path to the **MOSEK** command line tool.

---

### 4.1 Invoking the AMPL shell

The **MOSEK** distribution by default comes with the AMPL shell included. Assuming **MSKHOME** is the folder in which **MOSEK** has been installed, it is located under

```
{MSKHOME}/mosek/8/tools/platform/{PLATFORM}/bin/
```

for Linux and OSX users (**PLATFORM** must be among `linux64x86`, `osx64x86`), and under

```
{MSKHOME}\mosek\8\tools\platform\{PLATFORM}\bin\
```

for Windows users (**PLATFORM** must be among `win32x86`, `win64x86`).

To invoke the AMPL shell included in the **MOSEK** distribution type:

```
mampl
```

### 4.2 An example

In many instances, you can successfully apply **MOSEK** simply by specifying the model and data, setting the solver option to **MOSEK**, and typing `solve`.

The problem we want to solve is a simple linear optimization problem. The AMPL formulation is in [Listing 4.1](#).

Listing 4.1: An example of optimization problem using AMPL language.

```

set NUTR ordered;
set FOOD ordered;

param cost {FOOD} >= 0;
param f_min {FOOD} >= 0, default 0;
param f_max {j in FOOD} >= f_min[j], default Infinity;

param n_min {NUTR} >= 0, default 0;
param n_max {i in NUTR} >= n_min[i], default Infinity;

param amt {NUTR,FOOD} >= 0;

# -----

var Buy {j in FOOD} >= f_min[j], <= f_max[j];

# -----

minimize Total_Cost: sum {j in FOOD} cost[j] * Buy[j];

minimize Nutr_Amt {i in NUTR}: sum {j in FOOD} amt[i,j] * Buy[j];

# -----

subject to Diet {i in NUTR}:
    n_min[i] <= sum {j in FOOD} amt[i,j] * Buy[j] <= n_max[i];

```

We can specify the input data using an input file again following the AMPL language, as reported in [Listing 4.2](#).

Listing 4.2: An example of data for an optimization problem using AMPL language.

```

param:  FOOD:      cost  f_min  f_max :=
  "Quarter Pounder w/ Cheese"  1.84  .    .
  "McLean Deluxe w/ Cheese"    2.19  .    .
  "Big Mac"                     1.84  .    .
  "Filet-O-Fish"                1.44  .    .
  "McGrilled Chicken"          2.29  .    .
  "Fries, small"                .77   .    .
  "Sausage McMuffin"           1.29  .    .
  "1% Lowfat Milk"              .60   .    .
  "Orange Juice"               .72   .    . ;

param:  NUTR:      n_min  n_max :=
  Cal      2000    .
  Carbo    350     375
  Protein   55     .
  VitA     100     .
  VitC     100     .
  Calc     100     .
  Iron     100     . ;

param amt (tr):

```

	Cal	Carbo	Protein	VitA	VitC	Calc	Iron
"Quarter Pounder w/ Cheese"	510	34	28	15	6	30	20
"McLean Deluxe w/ Cheese"	370	35	24	15	10	20	20
"Big Mac"	500	42	25	6	2	25	20
"Filet-O-Fish"	370	38	14	2	0	15	10



"McGrilled Chicken"	400	42	31	8	15	15	8
"Fries, small"	220	26	3	0	15	0	2
"Sausage McMuffin"	345	27	15	4	0	20	15
"1% Lowfat Milk"	110	12	9	10	4	30	0
"Orange Juice"	80	20	1	2	120	2	2 ;

First to invoke the AMPL shell type:

```
mampl
```

when the AMPL shell has started type the commands:

```
ampl: model diet.mod;
ampl: data diet.dat;
ampl: option solver mosek;
ampl: solve;
```

The resulting output is:

```
MOSEK finished.
Problem status   - PRIMAL_AND_DUAL_FEASIBLE
Solution status  - OPTIMAL
Primal objective - 14.8557377
Dual objective   - 14.8557377

Objective = Total_Cost
```

## 4.3 Determining the outcome of an optimization

The AMPL parameter `solve_result_num` is used to indicate the outcome of the optimization process. It is used as follows

```
ampl: display solve_result_num
```

Please refer to table [Table 4.1](#) for possible values of this parameter.

Table 4.1: Interpretation of `solve_result_num`.

Value	Message
0	the solution is optimal.
100	suboptimal primal solution.
101	superoptimal (dual feasible) solution.
150	the solution is near optimal.
200	primal infeasible problem.
300	dual infeasible problem.
400	too many iterations.
500	solution status is unknown.
501	ill-posed problem, solution status is unknown.
> 501	Mapped <b>MOSEK</b> response code. See note below.

**Note:** **MOSEK** response codes are mapped on AMPL return code greater than 501. In order to get the actual response code the base value 501 must be subtracted. For example: say the AMPL return code is 502, then it corresponds to **MOSEK** response code 1.

## 4.4 Optimizer options

### 4.4.1 The MOSEK parameter database

The **MOSEK** optimizer has options and parameters controlling such things as the termination criterion and which optimizer is used. These parameters can be modified within AMPL as shown in the example below:

```
ampl: model diet.mod;
ampl: data diet.dat;
ampl: option solver mosek;
ampl: option mosek_options
ampl? 'msk_ipar_optimizer = msk_optimizer_primal_simplex \
ampl? msk_ipar_sim_max_iterations = 100000';
ampl: solve;
```

In the example above a string called `mosek_options` is created which contains the parameter settings. Each parameter setting has the format

```
parameter name = value
```

where `parameter name` can be any valid **MOSEK** parameter name. See Section 11.1 for a description of all valid **MOSEK** parameters.

An alternative way of specifying the options is

```
ampl: option mosek_options
ampl? 'msk_ipar_optimizer = msk_optimizer_primal_simplex'
ampl? 'msk_ipar_sim_max_iterations = 100000';
```

New options can also be appended to an existing option string as shown below

```
ampl: option mosek_options $mosek_options
ampl? ' msk_ipar_sim_print_freq = 0 msk_ipar_sim_max_iterations = 1000';
```

The expression `$mosek_options` expands to the current value of the option. Line two in the example appends an additional value `msk_ipar_sim_max_iterations` to the option string.

### 4.4.2 Options

#### outlev

Controls the amount of printed output. 0 means no printed output and a higher value means more printed output. An example of setting `outlev` is as follows:

```
ampl: option mosek_options 'outlev=2';
```

#### wantsol

We refer the reader to the AMPL manual [\[FGK03\]](#) for details about this option.

## 4.5 Constraint and variable names

AMPL assigns meaningful names to all the constraints and variables. Since **MOSEK** uses item names in error and log messages, it may be useful to pass the AMPL names to **MOSEK**.

Using the command

```
ampl: option auxfiles rc;
```

before the

```
ampl: solve;
```

command makes **MOSEK** obtain the constraint and variable names automatically.

## 4.6 Which solution is returned to AMPL

The **MOSEK** optimizer can produce three types of solutions: basic, integer, and interior point solutions. For nonlinear problems only an interior solution is available. For linear optimization problems optimized by the interior-point optimizer with basis identification turned on both a basic and an interior point solution are calculated. The simplex algorithm produces only a basic solution. Whenever both an interior and a basic solution are available, the basic solution is returned. For problems containing integer variables, the integer solution is returned to AMPL.

## 4.7 Hot-start

Frequently, a sequence of optimization problems is solved where each problem differs only slightly from the previous problem. In that case it may be advantageous to use the previous optimal solution to warm-start the optimizer. Such a facility is available in **MOSEK** only when the simplex optimizer is used.

The warm-start facility exploits the AMPL variable suffix `sstatus` to communicate the optimal basis back to AMPL, and AMPL uses this facility to communicate an initial basis to **MOSEK**. The following example demonstrates this feature.

```
ampl: model diet.mod;
ampl: data diet.dat;
ampl: option solver mosek;
ampl: option mosek_options
ampl? 'msk_ipar_optimizer = msk_optimizer_primal_simplex outlev=2';
ampl: solve;
ampl: display Buy.sstatus;
ampl: solve;
```

The resulting output is:

```
Accepted: msk_ipar_optimizer          = MSK_OPTIMIZER_PRIMAL_SIMPLEX
Accepted: outlev                      = 2

Computer  - Platform                  : Linux/64-X86
Computer  - CPU type                  : Intel-P4
MOSEK     - task name                  :
MOSEK     - objective sense            : min
MOSEK     - problem type               : LO (linear optimization problem)
MOSEK     - constraints                : 7                variables          : 9
MOSEK     - integer variables          : 0

Optimizer started.
Simplex optimizer started.
Presolve started.
Linear dependency checker started.
Linear dependency checker terminated.
Presolve   - Stk. size (kb) : 0
Eliminator - tries          : 0                time                  : 0.00
```

```

Eliminator - elim's          : 0
Lin. dep. - tries           : 1          time          : 0.00
Lin. dep. - number          : 0
Presolve terminated. Time: 0.00
Primal simplex optimizer started.
Primal simplex optimizer setup started.
Primal simplex optimizer setup terminated.
Optimizer - solved problem   : the primal
Optimizer - constraints      : 7          variables      : 9
Optimizer - hotstart        : no
ITER    DEGITER(%)  PFEAS    DFEAS    POBJ          DOBJ          TIME
→      TOTTIME
0       0.00        1.40e+03   NA       1.2586666667e+01   NA          0.00
→      0.01
3       0.00        0.00e+00   NA       1.4855737705e+01   NA          0.00
→      0.01
Primal simplex optimizer terminated.
Simplex optimizer terminated. Time: 0.00.
Optimizer terminated. Time: 0.01
Return code - 0 [MSK_RES_OK]
MOSEK finished.
Problem status   : PRIMAL_AND_DUAL_FEASIBLE
Solution status  : OPTIMAL
Primal objective : 14.8557377
Dual objective   : 14.8557377

Objective = Total_Cost
Buy.sstatus [*] :=
'Quarter Pounder w/ Cheese' bas
'McLean Deluxe w/ Cheese' low
'Big Mac' low
Filet-O-Fish low
'McGrilled Chicken' low
'Fries, small' bas
'Sausage McMuffin' low
'1% Lowfat Milk' bas
'Orange Juice' low
;
Accepted: msk_ipar_optimizer          = MSK_OPTIMIZER_PRIMAL_SIMPLEX
Accepted: outlev                      = 2
Basic solution
Problem status : UNKNOWN
Solution status : UNKNOWN
Primal - objective: 1.4855737705e+01 eq. infeas.: 3.97e+03 max bound infeas.: 2.00e+03
Dual   - objective: 0.0000000000e+00 eq. infeas.: 7.14e-01 max bound infeas.: 0.00e+00

Computer - Platform          : Linux/64-X86
Computer - CPU type         : Intel-P4
MOSEK    - task name        :
MOSEK    - objective sense   : min
MOSEK    - problem type      : LO (linear optimization problem)
MOSEK    - constraints       : 7          variables      : 9
MOSEK    - integer variables : 0
Optimizer started.
Simplex optimizer started.
Presolve started.
Presolve - Stk. size (kb) : 0
Eliminator - tries         : 0          time          : 0.00
Eliminator - elim's        : 0
Lin. dep. - tries         : 0          time          : 0.00
Lin. dep. - number        : 0
Presolve terminated. Time: 0.00
Primal simplex optimizer started.

```

```

Primal simplex optimizer setup started.
Primal simplex optimizer setup terminated.
Optimizer - solved problem      : the primal
Optimizer - constraints         : 7          variables           : 9
Optimizer - hotstart           : yes
Optimizer - Num. basic         : 7          Basis rank           : 7
Optimizer - Valid bas. fac.    : no
ITER      DEGITER(%)  PFEAS      DFEAS      POBJ      DOBJ      TIME
↪      TOTTIME
0         0.00        0.00e+00   NA        1.4855737705e+01   NA        0.00
↪      0.01
0         0.00        0.00e+00   NA        1.4855737705e+01   NA        0.00
↪      0.01
Primal simplex optimizer terminated.
Simplex optimizer terminated. Time: 0.00.
Optimizer terminated. Time: 0.01
Return code - 0 [MSK_RES_OK]
MOSEK finished.
Problem status   : PRIMAL_AND_DUAL_FEASIBLE
Solution status  : OPTIMAL
Primal objective : 14.8557377
Dual objective   : 14.8557377

Objective = Total_Cost

```

Please note that the second solve takes fewer iterations since the previous optimal basis is reused.

## 4.8 The infeasibility report

For linear optimization problems without any integer constrained variables **MOSEK** can generate an infeasibility report automatically. The report provides important information about the infeasibility.

The generation of the infeasibility report is turned on using the parameter setting

```

option auxfiles rc;
option mosek_options 'msk_ipar_infeas_report_auto=msk_on';

```

For further details about infeasibility report see Section 9.

## 4.9 Sensitivity analysis

**MOSEK** can calculate sensitivity information for the objective and constraints. To enable sensitivity information set the option:

```
sensitivity = 1
```

Results are returned in variable/constraint suffixes as follows:

- **.down** Smallest value of objective coefficient/right hand side before the optimal basis changes.
- **.up** Largest value of objective coefficient/right hand side before the optimal basis changes.
- **.current** Current value of objective coefficient/right hand side.

For ranged constraints sensitivity information is returned only for the lower bound.

The example below returns sensitivity information on the `diet` model.

```
ampl: model diet.mod;
ampl: data diet.dat;
ampl: option solver mosek;
ampl: option mosek_options 'sensitivity=1';

ampl: solve;
#display sensitivity information and current solution.
ampl: display _var.down,_var.current,_var.up,_var;
#display sensitivity information and optimal dual values.
ampl: display _con.down,_con.current,_con.up,_con;
```

The resulting output is:

```
Return code - 0 [MSK_RES_OK]
MOSEK finished.
Problem status : PRIMAL_AND_DUAL_FEASIBLE
Solution status : OPTIMAL
Primal objective : 14.8557377
Dual objective : 14.8557377

suffix up OUT;
suffix down OUT;
suffix current OUT;
Objective = Total_Cost
:  _var.down _var.current      _var.up      _var      :=
1  1.37385   1.84             1.86075    4.38525
2  1.8677    2.19             Infinity    0
3  1.82085   1.84             Infinity    0
4  1.35466   1.44             Infinity    0
5  1.57633   2.29             Infinity    0
6  0.094     0.77             0.794851   6.14754
7  1.22759   1.29             Infinity    0
8  0.57559   0.6              0.910769   3.42213
9  0.657279  0.72             Infinity    0
;
ampl: display _con.down,_con.current,_con.up,_con;
:  _con.down _con.current _con.up _con      :=
1  -Infinity 2000        3965.37 0
2  297.6     350        375     0.0277049
3  -Infinity 55         172.029 0
4  63.0531   100        195.388 0.0267541
5  -Infinity 100        132.213 0
6  -Infinity 100        234.221 0
7  17.6923   100        142.821 0.0248361
;
```

## 4.10 Using the command line version of the AMPL interface

AMPL can generate a data file containing all the optimization problem and all relevant information which can then be read and solved by the **MOSEK** command line tool.

When the problem has been loaded into AMPL, the commands

```
ampl: option auxfiles rc;
ampl: write bprob;
```

will make AMPL write the appropriate data files, i.e.

```
prob.nl  
prob.col  
prob.row
```

Then the problem can be solved using the command line version of **MOSEK** as follows

```
mosek prob.nl outlev=10 -a
```

The *-a* command line option indicates that **MOSEK** is invoked in AMPL mode. When **MOSEK** is invoked in AMPL mode the normal **MOSEK** command line options should appear *after* the *-a* option except for the file name which should be the first argument. As the above example demonstrates **MOSEK** accepts command line options as specified by the AMPL **convention**. Which command line arguments **MOSEK** accepts in AMPL mode can be viewed by executing

```
mosek -- -a
```

For linear, quadratic and quadratic constrained problems a text file representation of the problem can be obtained using one of the commands

```
mosek prob.nl -a -x -out prob.mps  
mosek prob.nl -a -x -out prob.opf  
mosek prob.nl -a -x -out prob.lp
```





## PROBLEM FORMULATION AND SOLUTIONS

In this chapter we will discuss the following issues:

- The formal definitions of the problem types that **MOSEK** can solve.
- The solution information produced by **MOSEK**.
- The information produced by **MOSEK** if the problem is infeasible.

### 5.1 Linear Optimization

A linear optimization problem can be written as

$$\begin{array}{ll} \text{minimize} & c^T x + c^f \\ \text{subject to} & l^c \leq Ax \leq u^c, \\ & l^x \leq x \leq u^x, \end{array} \quad (5.1)$$

where

- $m$  is the number of constraints.
- $n$  is the number of decision variables.
- $x \in \mathbb{R}^n$  is a vector of decision variables.
- $c \in \mathbb{R}^n$  is the linear part of the objective function.
- $A \in \mathbb{R}^{m \times n}$  is the constraint matrix.
- $l^c \in \mathbb{R}^m$  is the lower limit on the activity for the constraints.
- $u^c \in \mathbb{R}^m$  is the upper limit on the activity for the constraints.
- $l^x \in \mathbb{R}^n$  is the lower limit on the activity for the variables.
- $u^x \in \mathbb{R}^n$  is the upper limit on the activity for the variables.

A primal solution  $(x)$  is *(primal) feasible* if it satisfies all constraints in (5.1). If (5.1) has at least one primal feasible solution, then (5.1) is said to be (primal) feasible.

In case (5.1) does not have a feasible solution, the problem is said to be *(primal) infeasible*.

#### 5.1.1 Duality for Linear Optimization

Corresponding to the primal problem (5.1), there is a dual problem

$$\begin{array}{ll} \text{maximize} & (l^c)^T s_l^c - (u^c)^T s_u^c + (l^x)^T s_l^x - (u^x)^T s_u^x + c^f \\ \text{subject to} & A^T y + s_l^c - s_u^c = c, \\ & -y + s_l^x - s_u^x = 0, \\ & s_l^c, s_u^c, s_l^x, s_u^x \geq 0. \end{array} \quad (5.2)$$

If a bound in the primal problem is plus or minus infinity, the corresponding dual variable is fixed at 0, and we use the convention that the product of the bound value and the corresponding dual variable is 0. E.g.

$$l_j^x = -\infty \quad \Rightarrow \quad (s_l^x)_j = 0 \text{ and } l_j^x \cdot (s_l^x)_j = 0.$$

This is equivalent to removing variable  $(s_l^x)_j$  from the dual problem. A solution

$$(y, s_l^c, s_u^c, s_l^x, s_u^x)$$

to the dual problem is feasible if it satisfies all the constraints in (5.2). If (5.2) has at least one feasible solution, then (5.2) is *(dual) feasible*, otherwise the problem is *(dual) infeasible*.

## A Primal-dual Feasible Solution

A solution

$$(x, y, s_l^c, s_u^c, s_l^x, s_u^x)$$

is denoted a *primal-dual feasible solution*, if  $(x)$  is a solution to the primal problem (5.1) and  $(y, s_l^c, s_u^c, s_l^x, s_u^x)$  is a solution to the corresponding dual problem (5.2).

## The Duality Gap

Let

$$(x^*, y^*, (s_l^c)^*, (s_u^c)^*, (s_l^x)^*, (s_u^x)^*)$$

be a primal-dual feasible solution, and let

$$(x^c)^* := Ax^*.$$

For a primal-dual feasible solution we define the *duality gap* as the difference between the primal and the dual objective value,

$$\begin{aligned} c^T x^* + c^f - \{ & (l^c)^T (s_l^c)^* - (u^c)^T (s_u^c)^* + (l^x)^T (s_l^x)^* - (u^x)^T (s_u^x)^* + c^f \} \\ &= \sum_{i=0}^{m-1} [(s_l^c)^* ((x_i^c)^* - l_i^c) + (s_u^c)^* (u_i^c - (x_i^c)^*)] \\ &+ \sum_{j=0}^{n-1} [(s_l^x)^* (x_j - l_j^x) + (s_u^x)^* (u_j^x - x_j^*)] \geq 0 \end{aligned} \quad (5.3)$$

where the first relation can be obtained by transposing and multiplying the dual constraints (5.2) by  $x^*$  and  $(x^c)^*$  respectively, and the second relation comes from the fact that each term in each sum is nonnegative. It follows that the primal objective will always be greater than or equal to the dual objective.

## An Optimal Solution

It is well-known that a linear optimization problem has an optimal solution if and only if there exist feasible primal and dual solutions so that the duality gap is zero, or, equivalently, that the *complementarity conditions*

$$\begin{aligned} (s_l^c)^* ((x_i^c)^* - l_i^c) &= 0, & i = 0, \dots, m-1, \\ (s_u^c)^* (u_i^c - (x_i^c)^*) &= 0, & i = 0, \dots, m-1, \\ (s_l^x)^* (x_j - l_j^x) &= 0, & j = 0, \dots, n-1, \\ (s_u^x)^* (u_j^x - x_j^*) &= 0, & j = 0, \dots, n-1, \end{aligned}$$

are satisfied.

If (5.1) has an optimal solution and **MOSEK** solves the problem successfully, both the primal and dual solution are reported, including a status indicating the exact state of the solution.

### 5.1.2 Infeasibility for Linear Optimization

#### Primal Infeasible Problems

If the problem (5.1) is infeasible (has no feasible solution), **MOSEK** will report a certificate of primal infeasibility: The dual solution reported is the certificate of infeasibility, and the primal solution is undefined.

A certificate of primal infeasibility is a feasible solution to the modified dual problem

$$\begin{aligned} & \text{maximize} && (l^c)^T s_l^c - (u^c)^T s_u^c + (l^x)^T s_l^x - (u^x)^T s_u^x \\ & \text{subject to} && A^T y + s_l^x - s_u^x = 0, \\ & && -y + s_l^c - s_u^c = 0, \\ & && s_l^c, s_u^c, s_l^x, s_u^x \geq 0, \end{aligned} \tag{5.4}$$

such that the objective value is strictly positive, i.e. a solution

$$(y^*, (s_l^c)^*, (s_u^c)^*, (s_l^x)^*, (s_u^x)^*)$$

to (5.4) so that

$$(l^c)^T (s_l^c)^* - (u^c)^T (s_u^c)^* + (l^x)^T (s_l^x)^* - (u^x)^T (s_u^x)^* > 0.$$

Such a solution implies that (5.4) is unbounded, and that its dual is infeasible. As the constraints to the dual of (5.4) are identical to the constraints of problem (5.1), we thus have that problem (5.1) is also infeasible.

#### Dual Infeasible Problems

If the problem (5.2) is infeasible (has no feasible solution), **MOSEK** will report a certificate of dual infeasibility: The primal solution reported is the certificate of infeasibility, and the dual solution is undefined.

A certificate of dual infeasibility is a feasible solution to the modified primal problem

$$\begin{aligned} & \text{minimize} && c^T x \\ & \text{subject to} && \hat{l}^c \leq Ax \leq \hat{u}^c, \\ & && \hat{l}^x \leq x \leq \hat{u}^x, \end{aligned} \tag{5.5}$$

where

$$\hat{l}_i^c = \begin{cases} 0 & \text{if } l_i^c > -\infty, \\ -\infty & \text{otherwise,} \end{cases} \quad \text{and} \quad \hat{u}_i^c := \begin{cases} 0 & \text{if } u_i^c < \infty, \\ \infty & \text{otherwise,} \end{cases}$$

and

$$\hat{l}_j^x = \begin{cases} 0 & \text{if } l_j^x > -\infty, \\ -\infty & \text{otherwise,} \end{cases} \quad \text{and} \quad \hat{u}_j^x := \begin{cases} 0 & \text{if } u_j^x < \infty, \\ \infty & \text{otherwise,} \end{cases}$$

such that

$$c^T x < 0.$$

Such a solution implies that (5.5) is unbounded, and that its dual is infeasible. As the constraints to the dual of (5.5) are identical to the constraints of problem (5.2), we thus have that problem (5.2) is also infeasible.

#### Primal and Dual Infeasible Case

In case that both the primal problem (5.1) and the dual problem (5.2) are infeasible, **MOSEK** will report only one of the two possible certificates — which one is not defined (**MOSEK** returns the first certificate found).

### Minimalization vs. Maximalization

When the objective sense of problem (5.1) is maximization, i.e.

$$\begin{array}{ll} \text{maximize} & c^T x + c^f \\ \text{subject to} & l^c \leq Ax \leq u^c, \\ & l^x \leq x \leq u^x, \end{array}$$

the objective sense of the dual problem changes to minimization, and the domain of all dual variables changes sign in comparison to (5.2). The dual problem thus takes the form

$$\begin{array}{ll} \text{minimize} & (l^c)^T s_l^c - (u^c)^T s_u^c + (l^x)^T s_l^x - (u^x)^T s_u^x + c^f \\ \text{subject to} & A^T y + s_l^x - s_u^x = c, \\ & -y + s_l^c - s_u^c = 0, \\ & s_l^c, s_u^c, s_l^x, s_u^x \leq 0. \end{array}$$

This means that the duality gap, defined in (5.3) as the primal minus the dual objective value, becomes nonpositive. It follows that the dual objective will always be greater than or equal to the primal objective. The primal infeasibility certificate will be reported by **MOSEK** as a solution to the system

$$\begin{array}{l} A^T y + s_l^x - s_u^x = 0, \\ -y + s_l^c - s_u^c = 0, \\ s_l^c, s_u^c, s_l^x, s_u^x \leq 0, \end{array} \quad (5.6)$$

such that the objective value is strictly negative

$$(l^c)^T (s_l^c)^* - (u^c)^T (s_u^c)^* + (l^x)^T (s_l^x)^* - (u^x)^T (s_u^x)^* < 0.$$

Similarly, the certificate of dual infeasibility is an  $x$  satisfying the requirements of (5.5) such that  $c^T x > 0$ .

## 5.2 Conic Quadratic Optimization

*Conic quadratic optimization* is an extension of linear optimization (see Section 5.1) allowing conic domains to be specified for subsets of the problem variables. A conic quadratic optimization problem can be written as

$$\begin{array}{ll} \text{minimize} & c^T x + c^f \\ \text{subject to} & l^c \leq Ax \leq u^c, \\ & l^x \leq x \leq u^x, \\ & x \in \mathcal{K}, \end{array} \quad (5.7)$$

where set  $\mathcal{K}$  is a Cartesian product of convex cones, namely  $\mathcal{K} = \mathcal{K}_1 \times \cdots \times \mathcal{K}_p$ . Having the domain restriction,  $x \in \mathcal{K}$ , is thus equivalent to

$$x^t \in \mathcal{K}_t \subseteq \mathbb{R}^{n_t},$$

where  $x = (x^1, \dots, x^p)$  is a partition of the problem variables. Please note that the  $n$ -dimensional Euclidean space  $\mathbb{R}^n$  is a cone itself, so simple linear variables are still allowed.

**MOSEK** supports only a limited number of cones, specifically:

- The  $\mathbb{R}^n$  set.
- The quadratic cone:

$$\mathcal{Q}^n = \left\{ x \in \mathbb{R}^n : x_1 \geq \sqrt{\sum_{j=2}^n x_j^2} \right\}.$$

- The rotated quadratic cone:

$$\mathcal{Q}_r^n = \left\{ x \in \mathbb{R}^n : 2x_1x_2 \geq \sum_{j=3}^n x_j^2, \quad x_1 \geq 0, \quad x_2 \geq 0 \right\}.$$

Although these cones may seem to provide only limited expressive power they can be used to model a wide range of problems as demonstrated in [\[MOSEKApS12\]](#).

### 5.2.1 Duality for Conic Quadratic Optimization

The dual problem corresponding to the conic quadratic optimization problem (5.7) is given by

$$\begin{aligned} & \text{maximize} && (l^c)^T s_l^c - (u^c)^T s_u^c + (l^x)^T s_l^x - (u^x)^T s_u^x + c^f \\ & \text{subject to} && \\ & && A^T y + s_l^x - s_u^x + s_n^x = c \\ & && -y + s_l^c - s_u^c = 0, \\ & && s_l^c, s_u^c, s_l^x, s_u^x \geq 0, \\ & && s_n^x \in \mathcal{K}^*, \end{aligned} \tag{5.8}$$

where the dual cone  $\mathcal{K}^*$  is a Cartesian product of the cones

$$\mathcal{K}^* = \mathcal{K}_1^* \times \cdots \times \mathcal{K}_p^*,$$

where each  $\mathcal{K}_t^*$  is the dual cone of  $\mathcal{K}_t$ . For the cone types **MOSEK** can handle, the relation between the primal and dual cone is given as follows:

- The  $\mathbb{R}^n$  set:

$$\mathcal{K}_t = \mathbb{R}^{n_t} \quad \Leftrightarrow \quad \mathcal{K}_t^* = \{s \in \mathbb{R}^{n_t} : s = 0\}.$$

- The quadratic cone:

$$\mathcal{K}_t = \mathcal{Q}^{n_t} \quad \Leftrightarrow \quad \mathcal{K}_t^* = \mathcal{Q}^{n_t} = \left\{ s \in \mathbb{R}^{n_t} : s_1 \geq \sqrt{\sum_{j=2}^{n_t} s_j^2} \right\}.$$

- The rotated quadratic cone:

$$\mathcal{K}_t = \mathcal{Q}_r^{n_t} \quad \Leftrightarrow \quad \mathcal{K}_t^* = \mathcal{Q}_r^{n_t} = \left\{ s \in \mathbb{R}^{n_t} : 2s_1s_2 \geq \sum_{j=3}^{n_t} s_j^2, \quad s_1 \geq 0, \quad s_2 \geq 0 \right\}.$$

Please note that the dual problem of the dual problem is identical to the original primal problem.

### 5.2.2 Infeasibility for Conic Quadratic Optimization

In case **MOSEK** finds a problem to be infeasible it reports a certificate of infeasibility. This works exactly as for linear problems (see Section 5.1.2).

#### Primal Infeasible Problems

If the problem (5.7) is infeasible, **MOSEK** will report a certificate of primal infeasibility: The dual solution reported is the certificate of infeasibility, and the primal solution is undefined.

A certificate of primal infeasibility is a feasible solution to the problem

$$\begin{aligned} & \text{maximize} && (l^c)^T s_l^c - (u^c)^T s_u^c + (l^x)^T s_l^x - (u^x)^T s_u^x \\ & \text{subject to} && \\ & && A^T y + s_l^x - s_u^x + s_n^x = 0, \\ & && -y + s_l^c - s_u^c = 0, \\ & && s_l^c, s_u^c, s_l^x, s_u^x \geq 0, \\ & && s_n^x \in \mathcal{K}^*, \end{aligned}$$

such that the objective value is strictly positive.

### Dual infeasible problems

If the problem (5.8) is infeasible, **MOSEK** will report a certificate of dual infeasibility: The primal solution reported is the certificate of infeasibility, and the dual solution is undefined.

A certificate of dual infeasibility is a feasible solution to the problem

$$\begin{aligned} & \text{minimize} && c^T x \\ & \text{subject to} && \hat{l}^c \leq Ax \leq \hat{u}^c, \\ & && \hat{l}^x \leq x \leq \hat{u}^x, \\ & && x \in \mathcal{K}, \end{aligned}$$

where

$$\hat{l}_i^c = \begin{cases} 0 & \text{if } l_i^c > -\infty, \\ -\infty & \text{otherwise,} \end{cases} \quad \text{and} \quad \hat{u}_i^c := \begin{cases} 0 & \text{if } u_i^c < \infty, \\ \infty & \text{otherwise,} \end{cases}$$

and

$$\hat{l}_j^x = \begin{cases} 0 & \text{if } l_j^x > -\infty, \\ -\infty & \text{otherwise,} \end{cases} \quad \text{and} \quad \hat{u}_j^x := \begin{cases} 0 & \text{if } u_j^x < \infty, \\ \infty & \text{otherwise,} \end{cases}$$

such that the objective value is strictly negative.

## 5.3 Semidefinite Optimization

*Semidefinite optimization* is an extension of conic quadratic optimization (see Section 5.2) allowing positive semidefinite matrix variables to be used in addition to the usual scalar variables. A semidefinite optimization problem can be written as

$$\begin{aligned} & \text{minimize} && \sum_{j=0}^{n-1} c_j x_j + \sum_{j=0}^{p-1} \langle \bar{C}_j, \bar{X}_j \rangle + c^f \\ & \text{subject to} && \begin{aligned} l_i^c &\leq && \sum_{j=0}^{n-1} a_{ij} x_j + \sum_{j=0}^{p-1} \langle \bar{A}_{ij}, \bar{X}_j \rangle &\leq u_i^c, & i = 0, \dots, m-1 \\ l_j^x &\leq && x_j &\leq u_j^x, & j = 0, \dots, n-1 \\ &&& x \in \mathcal{K}, \bar{X}_j \in \mathcal{S}_+^{r_j}, && j = 0, \dots, p-1 \end{aligned} \end{aligned} \quad (5.9)$$

where the problem has  $p$  symmetric positive semidefinite variables  $\bar{X}_j \in \mathcal{S}_+^{r_j}$  of dimension  $r_j$  with symmetric coefficient matrices  $\bar{C}_j \in \mathcal{S}^{r_j}$  and  $\bar{A}_{ij} \in \mathcal{S}^{r_j}$ . We use standard notation for the matrix inner product, i.e., for  $U, V \in \mathbb{R}^{m \times n}$  we have

$$\langle U, V \rangle := \sum_{i=0}^{m-1} \sum_{j=0}^{n-1} U_{ij} V_{ij}.$$

With semidefinite optimization we can model a wide range of problems as demonstrated in [MOSEKApS12].

### 5.3.1 Duality for Semidefinite Optimization

The dual problem corresponding to the semidefinite optimization problem (5.9) is given by

$$\begin{aligned} & \text{maximize} && (l^c)^T s_l^c - (u^c)^T s_u^c + (l^x)^T s_l^x - (u^x)^T s_u^x + c^f \\ & \text{subject to} && \begin{aligned} c - A^T y + s_u^x - s_l^x &= s_n^x, \\ \bar{C}_j - \sum_{i=0}^m y_i \bar{A}_{ij} &= \bar{S}_j, & j = 0, \dots, p-1 \\ s_l^c - s_u^c &= y, \\ s_l^c, s_u^c, s_l^x, s_u^x &\geq 0, \\ s_n^x &\in \mathcal{K}^*, \quad \bar{S}_j \in \mathcal{S}_+^{r_j}, & j = 0, \dots, p-1 \end{aligned} \end{aligned} \quad (5.10)$$

where  $A \in \mathbb{R}^{m \times n}$ ,  $A_{ij} = a_{ij}$ , which is similar to the dual problem for conic quadratic optimization (see Section 5.2.1), except for the addition of dual constraints

$$\left( \bar{C}_j - \sum_{i=0}^m y_i \bar{A}_{ij} \right) \in \mathcal{S}_+^{r_j}.$$

Note that the dual of the dual problem is identical to the original primal problem.

### 5.3.2 Infeasibility for Semidefinite Optimization

In case **MOSEK** finds a problem to be infeasible it reports a certificate of the infeasibility. This works exactly as for linear problems (see Section 5.1.2).

#### Primal Infeasible Problems

If the problem (5.9) is infeasible, **MOSEK** will report a certificate of primal infeasibility: The dual solution reported is a certificate of infeasibility, and the primal solution is undefined.

A certificate of primal infeasibility is a feasible solution to the problem

$$\begin{aligned} & \text{maximize} && (l^c)^T s_l^c - (u^c)^T s_u^c + (l^x)^T s_l^x - (u^x)^T s_u^x \\ & \text{subject to} && A^T y + s_l^x - s_u^x + s_n^x = 0, \\ & && \sum_{i=0}^{m-1} y_i \bar{A}_{ij} + \bar{S}_j = 0, && j = 0, \dots, p-1 \\ & && -y + s_l^c - s_u^c = 0, \\ & && s_l^c, s_u^c, s_l^x, s_u^x \geq 0, \\ & && s_n^x \in \mathcal{K}^*, \quad \bar{S}_j \in \mathcal{S}_+^{r_j}, && j = 0, \dots, p-1 \end{aligned}$$

such that the objective value is strictly positive.

#### Dual Infeasible Problems

If the problem (5.10) is infeasible, **MOSEK** will report a certificate of dual infeasibility: The primal solution reported is the certificate of infeasibility, and the dual solution is undefined.

A certificate of dual infeasibility is a feasible solution to the problem

$$\begin{aligned} & \text{minimize} && \sum_{j=0}^{n-1} c_j x_j + \sum_{j=0}^{p-1} \langle \bar{C}_j, \bar{X}_j \rangle \\ & \text{subject to} && \hat{l}_i^c \leq \sum_{j=1}^n a_{ij} x_j + \sum_{j=0}^{p-1} \langle \bar{A}_{ij}, \bar{X}_j \rangle \leq \hat{u}_i^c, \quad i = 0, \dots, m-1 \\ & && \hat{l}^x \leq \begin{matrix} x \\ \bar{X}_j \end{matrix} \leq \hat{u}^x, \\ & && x \in \mathcal{K}, \quad \bar{X}_j \in \mathcal{S}_+^{r_j}, && j = 0, \dots, p-1 \end{aligned}$$

where

$$\hat{l}_i^c = \begin{cases} 0 & \text{if } l_i^c > -\infty, \\ -\infty & \text{otherwise,} \end{cases} \quad \text{and} \quad \hat{u}_i^c := \begin{cases} 0 & \text{if } u_i^c < \infty, \\ \infty & \text{otherwise,} \end{cases}$$

and

$$\hat{l}_j^x = \begin{cases} 0 & \text{if } l_j^x > -\infty, \\ -\infty & \text{otherwise,} \end{cases} \quad \text{and} \quad \hat{u}_j^x := \begin{cases} 0 & \text{if } u_j^x < \infty, \\ \infty & \text{otherwise,} \end{cases}$$

such that the objective value is strictly negative.

## 5.4 Quadratic and Quadratically Constrained Optimization

A convex quadratic and quadratically constrained optimization problem is an optimization problem of the form

$$\begin{aligned} & \text{minimize} && \frac{1}{2}x^T Q^o x + c^T x + c^f \\ & \text{subject to} && \begin{aligned} l_k^c &\leq \frac{1}{2}x^T Q^k x + \sum_{j=0}^{n-1} a_{kj} x_j &\leq u_k^c, & k = 0, \dots, m-1, \\ l_j^x &\leq x_j &\leq u_j^x, & j = 0, \dots, n-1, \end{aligned} \end{aligned} \quad (5.11)$$

where  $Q^o$  and all  $Q^k$  are symmetric matrices. Moreover for convexity,  $Q^o$  must be a positive semidefinite matrix and  $Q^k$  must satisfy

$$\begin{aligned} -\infty < l_k^c &\Rightarrow Q^k \text{ is negative semidefinite,} \\ u_k^c < \infty &\Rightarrow Q^k \text{ is positive semidefinite,} \\ -\infty < l_k^c \leq u_k^c < \infty &\Rightarrow Q^k = 0. \end{aligned}$$

The convexity requirement is very important and **MOSEK** checks whether it is fulfilled.

### 5.4.1 A Recommendation

Any convex quadratic optimization problem can be reformulated as a conic quadratic optimization problem, see [MOSEKApS12] and in particular [And13]. In fact **MOSEK** does such conversion internally as a part of the solution process for the following reasons:

- the conic optimizer is numerically more robust than the one for quadratic problems.
- the conic optimizer is usually faster because quadratic cones are simpler than quadratic functions, even though the conic reformulation usually has more constraints and variables than the original quadratic formulation.
- it is easy to dualize the conic formulation if deemed worthwhile potentially leading to (huge) computational savings.

However, instead of relying on the automatic reformulation we recommend to formulate the problem as conic problem from scratch because:

- it saves the computational overhead of the reformulation including the convexity check. A conic problem is convex by construction and hence no convexity check is needed for conic problems.
- usually the modeller can do a better reformulation than the automatic method because the modeller can exploit the knowledge of what is being modelled.

To summarize we recommend to formulate quadratic problems and in particular quadratically constrained problems directly in conic form.

### 5.4.2 Duality for Quadratic and Quadratically Constrained Optimization

The dual problem corresponding to the quadratic and quadratically constrained optimization problem (5.11) is given by

$$\begin{aligned} & \text{maximize} && (l^c)^T s_l^c - (u^c)^T s_u^c + (l^x)^T s_l^x - (u^x)^T s_u^x + \frac{1}{2}x^T \left\{ \sum_{k=0}^{m-1} y_k Q^k - Q^o \right\} x + c^f \\ & \text{subject to} && \begin{aligned} A^T y + s_l^x - s_u^x + \left\{ \sum_{k=0}^{m-1} y_k Q^k - Q^o \right\} x &= c, \\ -y + s_l^c - s_u^c &= 0, \\ s_l^c, s_u^c, s_l^x, s_u^x &\geq 0. \end{aligned} \end{aligned} \quad (5.12)$$

The dual problem is related to the dual problem for linear optimization (see Section 5.1.1), but depends on the variable  $x$  which in general can not be eliminated. In the solutions reported by **MOSEK**, the value of  $x$  is the same for the primal problem (5.11) and the dual problem (5.12).



### 5.4.3 Infeasibility for Quadratic and Quadratically Constrained Optimization

In case **MOSEK** finds a problem to be infeasible it reports a certificate of infeasibility. This works exactly as for linear problems (see Section 5.1.2).

#### Primal Infeasible Problems

If the problem (5.11) with all  $Q^k = 0$  is infeasible, **MOSEK** will report a certificate of primal infeasibility. As the constraints are the same as for a linear problem, the certificate of infeasibility is the same as for linear optimization (see Section 5.1.2.1).

#### Dual Infeasible Problems

If the problem (5.12) with all  $Q^k = 0$  is infeasible, **MOSEK** will report a certificate of dual infeasibility. The primal solution reported is the certificate of infeasibility, and the dual solution is undefined.

A certificate of dual infeasibility is a feasible solution to the problem

$$\begin{array}{ll} \text{minimize} & c^T x \\ \text{subject to} & \hat{l}^c \leq Ax \leq \hat{u}^c, \\ & 0 \leq Q^o x \leq 0, \\ & \hat{l}^x \leq x \leq \hat{u}^x, \end{array}$$

where

$$\hat{l}_i^c = \begin{cases} 0 & \text{if } l_i^c > -\infty, \\ -\infty & \text{otherwise,} \end{cases} \quad \text{and} \quad \hat{u}_i^c := \begin{cases} 0 & \text{if } u_i^c < \infty, \\ \infty & \text{otherwise,} \end{cases}$$

and

$$\hat{l}_j^x = \begin{cases} 0 & \text{if } l_j^x > -\infty, \\ -\infty & \text{otherwise,} \end{cases} \quad \text{and} \quad \hat{u}_j^x := \begin{cases} 0 & \text{if } u_j^x < \infty, \\ \infty & \text{otherwise,} \end{cases}$$

such that the objective value is strictly negative.

## 5.5 General Convex Optimization

**MOSEK** is capable of solving smooth (twice differentiable) convex nonlinear optimization problems of the form

$$\begin{array}{ll} \text{minimize} & f(x) + c^T x + c^f \\ \text{subject to} & l^c \leq g(x) + Ax \leq u^c, \\ & l^x \leq x \leq u^x, \end{array}$$

where

- $m$  is the number of constraints.
- $n$  is the number of decision variables.
- $x \in \mathbb{R}^n$  is a vector of decision variables.
- $c \in \mathbb{R}^n$  is the linear part objective function.
- $A \in \mathbb{R}^{m \times n}$  is the constraint matrix.
- $l^c \in \mathbb{R}^m$  is the lower limit on the activity for the constraints.
- $u^c \in \mathbb{R}^m$  is the upper limit on the activity for the constraints.
- $l^x \in \mathbb{R}^n$  is the lower limit on the activity for the variables.

- $u^x \in \mathbb{R}^n$  is the upper limit on the activity for the variables.
- $f : \mathbb{R}^n \rightarrow \mathbb{R}$  is a nonlinear function.
- $g : \mathbb{R}^n \rightarrow \mathbb{R}^m$  is a nonlinear vector function.

This means that the  $i$ -th constraint has the form

$$l_i^c \leq g_i(x) + \sum_{j=1}^n a_{ij}x_j \leq u_i^c.$$

The linear term  $Ax$  is included in  $g(x)$  since it can be handled much more efficiently as a separate entity when optimizing.

The nonlinear functions  $f$  and  $g$  must be smooth in all  $x \in [l^x; u^x]$ . Moreover,  $f(x)$  must be a convex function and  $g_i(x)$  must satisfy

$$\begin{aligned} -\infty < l_i^c &\Rightarrow g_i(x) \text{ is concave,} \\ u_i^c < \infty &\Rightarrow g_i(x) \text{ is convex,} \\ -\infty < l_i^c \leq u_i^c < \infty &\Rightarrow g_i(x) = 0. \end{aligned}$$

### 5.5.1 Duality for General convex Optimization

Similar to the linear case, **MOSEK** reports dual information in the general nonlinear case. Indeed in this case the Lagrange function is defined by

$$\begin{aligned} L(x, s_l^c, s_u^c, s_l^x, s_u^x) &:= f(x) + c^T x + c^f \\ &\quad - (s_l^c)^T (g(x) + Ax - l^c) - (s_u^c)^T (u^c - g(x) - Ax) \\ &\quad - (s_l^x)^T (x - l^x) - (s_u^x)^T (u^x - x), \end{aligned}$$

and the dual problem is given by

$$\begin{aligned} &\text{maximize} && L(x, s_l^c, s_u^c, s_l^x, s_u^x) \\ &\text{subject to} && \nabla_x L(x, s_l^c, s_u^c, s_l^x, s_u^x)^T = 0, \\ &&& s_l^c, s_u^c, s_l^x, s_u^x \geq 0, \end{aligned}$$

which is equivalent to

$$\begin{aligned} &\text{maximize} && (l^c)^T s_l^c - (u^c)^T s_u^c + (l^x)^T s_l^x - (u^x)^T s_u^x + c^f \\ &&& + f(x) - g(x)^T y - (\nabla f(x)^T - \nabla g(x)^T y)^T x \\ &\text{subject to} && A^T y + s_l^x - s_u^x - (\nabla f(x)^T - \nabla g(x)^T y) = c, \\ &&& -y + s_l^c - s_u^c = 0, \\ &&& s_l^c, s_u^c, s_l^x, s_u^x \geq 0. \end{aligned}$$

In this context we use the following definition for scalar functions

$$\nabla f(x) = \left[ \frac{\partial f(x)}{\partial x_1}, \dots, \frac{\partial f(x)}{\partial x_n} \right],$$

and accordingly for vector functions

$$\nabla g(x) = \begin{bmatrix} \nabla g_1(x) \\ \vdots \\ \nabla g_m(x) \end{bmatrix}.$$

## THE OPTIMIZERS FOR CONTINUOUS PROBLEMS

The most essential part of **MOSEK** is the optimizers. Each optimizer is designed to solve a particular class of problems, i.e. linear, conic, or general nonlinear problems. The purpose of the present chapter is to discuss which optimizers are available for the continuous problem classes and how the performance of an optimizer can be tuned, if needed. This chapter deals with the optimizers for *continuous problems* with no integer variables.

When the optimizer is called, it roughly performs the following steps:

1. *Presolve*: Preprocessing to reduce the size of the problem.
2. *Dualizer*: Choosing whether to solve the primal or the dual form of the problem.
3. *Scaling*: Scaling the problem for better numerical stability.
4. *Optimize*: Solve the problem using selected method.

The first three preprocessing steps are transparent to the user, but useful to know about for tuning purposes. In general, the purpose of the preprocessing steps is to make the actual optimization more efficient and robust.

### Using multiple threads

The interior-point optimizers in **MOSEK** have been parallelized. This means that if you solve linear, quadratic, conic, or general convex optimization problem using the interior-point optimizer, you can take advantage of multiple CPU's.

By default **MOSEK** will automatically select the number of threads to be employed when solving the problem. However, the number of threads employed can be changed by setting the parameter `MSK_IPAR_NUM_THREADS`. This should never exceed the number of cores on the computer.

The speed-up obtained when using multiple threads is highly problem and hardware dependent, and consequently, it is advisable to compare single threaded and multi threaded performance for the given problem type to determine the optimal settings.

For small problems, using multiple threads is not be worthwhile and may even be counter productive.

## 6.1 Presolve

Before an optimizer actually performs the optimization the problem is preprocessed using the so-called presolve. The purpose of the presolve is to

1. remove redundant constraints,
2. eliminate fixed variables,
3. remove linear dependencies,
4. substitute out (implied) free variables, and

5. reduce the size of the optimization problem in general.

After the presolved problem has been optimized the solution is automatically postsolved so that the returned solution is valid for the original problem. Hence, the presolve is completely transparent. For further details about the presolve phase, please see [AA95] and [AGMX96].

It is possible to fine-tune the behavior of the presolve or to turn it off entirely. If presolve consumes too much time or memory compared to the reduction in problem size gained it may be disabled. This is done by setting the parameter `MSK_IPAR_PRESOLVE_USE` to `MSK_PRESOLVE_MODE_OFF`.

The two most time-consuming steps of the presolve are

- the eliminator, and
- the linear dependency check.

Therefore, in some cases it is worthwhile to disable one or both of these.

### Numerical issues in the presolve

During the presolve the problem is reformulated so that it hopefully solves faster. However, in rare cases the presolved problem may be harder to solve than the original problem. The presolve may also be infeasible although the original problem is not.

If it is suspected that presolved problem is much harder to solve than the original then it is suggested to first turn the eliminator off by setting the parameter `MSK_IPAR_PRESOLVE_ELIMINATOR_MAX_NUM_TRIES` to 0. If that does not help, then trying to turn presolve off may help.

Since all computations are done in finite precision then the presolve employs some tolerances when concluding a variable is fixed or constraint is redundant. If it happens that **MOSEK** incorrectly concludes a problem is primal or dual infeasible, then it is worthwhile to try to reduce the parameters `MSK_DPAR_PRESOLVE_TOL_X` and `MSK_DPAR_PRESOLVE_TOL_S`. However, if reducing the parameters actually helps then this should be taken as an indication that the problem is badly formulated.

### Eliminator

The purpose of the eliminator is to eliminate free and implied free variables from the problem using substitution. For instance, given the constraints

$$\begin{aligned} y &= \sum_j x_j, \\ y, x &\geq 0, \end{aligned}$$

$y$  is an implied free variable that can be substituted out of the problem, if deemed worthwhile. If the eliminator consumes too much time or memory compared to the reduction in problem size gained it may be disabled. This can be done by setting the parameter `MSK_IPAR_PRESOLVE_ELIMINATOR_MAX_NUM_TRIES` to 0. In rare cases the eliminator may cause that the problem becomes much hard to solve.

### Linear dependency checker

The purpose of the linear dependency check is to remove linear dependencies among the linear equalities. For instance, the three linear equalities

$$\begin{aligned} x_1 + x_2 + x_3 &= 1, \\ x_1 + 0.5x_2 &= 0.5, \\ 0.5x_2 + x_3 &= 0.5 \end{aligned}$$

contain exactly one linear dependency. This implies that one of the constraints can be dropped without changing the set of feasible solutions. Removing linear dependencies is in general a good idea since it reduces the size of the problem. Moreover, the linear dependencies are likely to introduce numerical problems in the optimization phase.

It is best practise to build models without linear dependencies. If the linear dependencies are removed at the modeling stage, the linear dependency check can safely be disabled by setting the parameter `MSK_IPAR_PRESOLVE_LINDEP_USE` to `MSK_OFF`.

## Dualizer

All linear, conic, and convex optimization problems have an equivalent dual problem associated with them. **MOSEK** has built-in heuristics to determine if it is most efficient to solve the primal or dual problem. The form (primal or dual) solved is displayed in the **MOSEK** log. Should the internal heuristics not choose the most efficient form of the problem it may be worthwhile to set the dualizer manually by setting the parameters:

- `MSK_IPAR_INTPNT_SOLVE_FORM`: In case of the interior-point optimizer.
- `MSK_IPAR_SIM_SOLVE_FORM`: In case of the simplex optimizer.

Note that currently only linear problems may be dualized.

## Scaling

Problems containing data with large and/or small coefficients, say  $1.0e + 9$  or  $1.0e - 7$ , are often hard to solve. Significant digits may be truncated in calculations with finite precision, which can result in the optimizer relying on inaccurate calculations. Since computers work in finite precision, extreme coefficients should be avoided. In general, data around the same *order of magnitude* is preferred, and we will refer to a problem, satisfying this loose property, as being *well-scaled*. If the problem is not well scaled, **MOSEK** will try to scale (multiply) constraints and variables by suitable constants. **MOSEK** solves the scaled problem to improve the numerical properties.

The scaling process is transparent, i.e. the solution to the original problem is reported. It is important to be aware that the optimizer terminates when the termination criterion is met on the scaled problem, therefore significant primal or dual infeasibilities may occur after unscaling for badly scaled problems. The best solution of this issue is to reformulate the problem, making it better scaled.

By default **MOSEK** heuristically chooses a suitable scaling. The scaling for interior-point and simplex optimizers can be controlled with the parameters `MSK_IPAR_INTPNT_SCALING` and `MSK_IPAR_SIM_SCALING` respectively.

## 6.2 Linear Optimization

### 6.2.1 Optimizer Selection

Two different types of optimizers are available for linear problems: The default is an interior-point method, and the alternatives are simplex methods. The optimizer can be selected using the parameter `MSK_IPAR_OPTIMIZER`.

### 6.2.2 The Interior-point Optimizer

The purpose of this section is to provide information about the algorithm employed in **MOSEK** interior-point optimizer.

In order to keep the discussion simple it is assumed that **MOSEK** solves linear optimization problems of standard form

$$\begin{aligned} &\text{minimize} && c^T x \\ &\text{subject to} && Ax = b, \\ &&& x \geq 0. \end{aligned} \tag{6.1}$$

This is in fact what happens inside **MOSEK**; for efficiency reasons **MOSEK** converts the problem to standard form before solving, then converts it back to the input form when reporting the solution.

Since it is not known beforehand whether problem (6.1) has an optimal solution, is primal infeasible or is dual infeasible, the optimization algorithm must deal with all three situations. This is the reason that **MOSEK** solves the so-called homogeneous model

$$\begin{aligned} Ax - b\tau &= 0, \\ A^T y + s - c\tau &= 0, \\ -c^T x + b^T y - \kappa &= 0, \\ x, s, \tau, \kappa &\geq 0, \end{aligned} \tag{6.2}$$

where  $y$  and  $s$  correspond to the dual variables in (6.1), and  $\tau$  and  $\kappa$  are two additional scalar variables. Note that the homogeneous model (6.2) always has solution since

$$(x, y, s, \tau, \kappa) = (0, 0, 0, 0, 0)$$

is a solution, although not a very interesting one.

Any solution

$$(x^*, y^*, s^*, \tau^*, \kappa^*)$$

to the homogeneous model (6.2) satisfies

$$x_j^* s_j^* = 0 \text{ and } \tau^* \kappa^* = 0.$$

Moreover, there is always a solution that has the property

$$\tau^* + \kappa^* > 0.$$

First, assume that  $\tau^* > 0$ . It follows that

$$\begin{aligned} A \frac{x^*}{\tau^*} &= b, \\ A^T \frac{y^*}{\tau^*} + \frac{s^*}{\tau^*} &= c, \\ -c^T \frac{x^*}{\tau^*} + b^T \frac{y^*}{\tau^*} &= 0, \\ x^*, s^*, \tau^*, \kappa^* &\geq 0. \end{aligned}$$

This shows that  $\frac{x^*}{\tau^*}$  is a primal optimal solution and  $(\frac{y^*}{\tau^*}, \frac{s^*}{\tau^*})$  is a dual optimal solution; this is reported as the optimal interior-point solution since

$$(x, y, s) = \left\{ \frac{x^*}{\tau^*}, \frac{y^*}{\tau^*}, \frac{s^*}{\tau^*} \right\}$$

is a primal-dual optimal solution.

On other hand, if  $\kappa^* > 0$  then

$$\begin{aligned} Ax^* &= 0, \\ A^T y^* + s^* &= 0, \\ -c^T x^* + b^T y^* &= \kappa^*, \\ x^*, s^*, \tau^*, \kappa^* &\geq 0. \end{aligned}$$

This implies that at least one of

$$-c^T x^* > 0 \tag{6.3}$$

or

$$b^T y^* > 0 \tag{6.4}$$

is satisfied. If (6.3) is satisfied then  $x^*$  is a certificate of dual infeasibility, whereas if (6.4) is satisfied then  $y^*$  is a certificate of dual infeasibility.

In summary, by computing an appropriate solution to the homogeneous model, all information required for a solution to the original problem is obtained. A solution to the homogeneous model can be computed using a primal-dual interior-point algorithm [And09].

### Interior-point Termination Criterion

For efficiency reasons it is not practical to solve the homogeneous model exactly. Hence, an exact optimal solution or an exact infeasibility certificate cannot be computed and a reasonable termination criterion has to be employed.

In every iteration,  $k$ , of the interior-point algorithm a trial solution

$$(x^k, y^k, s^k, \tau^k, \kappa^k)$$

to homogeneous model is generated where

$$x^k, s^k, \tau^k, \kappa^k > 0.$$

Whenever the trial solution satisfies the criterion

$$\begin{aligned} \left\| A \frac{x^k}{\tau^k} - b \right\|_{\infty} &\leq \epsilon_p (1 + \|b\|_{\infty}), \\ \left\| A^T \frac{y^k}{\tau^k} + \frac{s^k}{\tau^k} - c \right\|_{\infty} &\leq \epsilon_d (1 + \|c\|_{\infty}), \text{ and} \\ \min \left( \frac{(x^k)^T s^k}{(\tau^k)^2}, \left| \frac{c^T x^k}{\tau^k} - \frac{b^T y^k}{\tau^k} \right| \right) &\leq \epsilon_g \max \left( 1, \frac{\min(|c^T x^k|, |b^T y^k|)}{\tau^k} \right), \end{aligned} \quad (6.5)$$

the interior-point optimizer is terminated and

$$\frac{(x^k, y^k, s^k)}{\tau^k}$$

is reported as the primal-dual optimal solution. The interpretation of (6.5) is that the optimizer is terminated if

- $\frac{x^k}{\tau^k}$  is approximately primal feasible,
- $\left\{ \frac{y^k}{\tau^k}, \frac{s^k}{\tau^k} \right\}$  is approximately dual feasible, and
- the duality gap is almost zero.

On the other hand, if the trial solution satisfies

$$-\epsilon_i c^T x^k > \frac{\|c\|_{\infty}}{\max(1, \|b\|_{\infty})} \|Ax^k\|_{\infty}$$

then the problem is declared dual infeasible and  $x^k$  is reported as a certificate of dual infeasibility. The motivation for this stopping criterion is as follows: First assume that  $\|Ax^k\|_{\infty} = 0$ ; then  $x^k$  is an exact certificate of dual infeasibility. Next assume that this is not the case, i.e.

$$\|Ax^k\|_{\infty} > 0,$$

and define

$$\bar{x} := \epsilon_i \frac{\max(1, \|b\|_{\infty})}{\|Ax^k\|_{\infty} \|c\|_{\infty}} x^k.$$

It is easy to verify that

$$\|A\bar{x}\|_{\infty} = \epsilon_i \frac{\max(1, \|b\|_{\infty})}{\|c\|_{\infty}} \text{ and } -c^T \bar{x} > 1,$$

which shows  $\bar{x}$  is an approximate certificate of dual infeasibility where  $\epsilon_i$  controls the quality of the approximation. A smaller value means a better approximation.

Finally, if

$$\epsilon_i b^T y^k > \frac{\|b\|_{\infty}}{\max(1, \|c\|_{\infty})} \|A^T y^k + s^k\|_{\infty}$$

then  $y^k$  is reported as a certificate of primal infeasibility.

It is possible to adjust the tolerances  $\varepsilon_p$ ,  $\varepsilon_d$ ,  $\varepsilon_g$  and  $\varepsilon_i$  using parameters; see Table 6.1 for details.

Table 6.1: Parameters employed in termination criterion

ToleranceParameter	name
$\varepsilon_p$	<i>MSK_DPAR_INTPNT_TOL_PFEAS</i>
$\varepsilon_d$	<i>MSK_DPAR_INTPNT_TOL_DFEAS</i>
$\varepsilon_g$	<i>MSK_DPAR_INTPNT_TOL_REL_GAP</i>
$\varepsilon_i$	<i>MSK_DPAR_INTPNT_TOL_INFEAS</i>

The default values of the termination tolerances are chosen such that for a majority of problems appearing in practice it is not possible to achieve much better accuracy. Therefore, tightening the tolerances usually is not worthwhile. However, an inspection of (6.5) reveals that quality of the solution is dependent on  $\|b\|_\infty$  and  $\|c\|_\infty$ ; the smaller the norms are, the better the solution accuracy.

The interior-point method as implemented by **MOSEK** will converge toward optimality and primal and dual feasibility at the same rate [And09]. This means that if the optimizer is stopped prematurely then it is very unlikely that either the primal or dual solution is feasible. Another consequence is that in most cases all the tolerances,  $\varepsilon_p$ ,  $\varepsilon_d$  and  $\varepsilon_g$ , have to be relaxed together to achieve an effect.

In some cases the interior-point method terminates having found a solution not too far from meeting the optimality condition (6.5). A solution is defined as *near optimal* if scaling  $\varepsilon_p$ ,  $\varepsilon_d$  and  $\varepsilon_g$  by any number  $\varepsilon_n \in [1.0, +\infty]$  conditions (6.5) are satisfied.

A near optimal solution is therefore of lower quality but still potentially valuable. If for instance the solver stalls, i.e. it can make no more significant progress towards the optimal solution, a near optimal solution could be available and be good enough for the user.

The basis identification discussed in Section 6.2.2.2 requires an optimal solution to work well; hence basis identification should be turned off if the termination criterion is relaxed.

To conclude the discussion in this section, relaxing the termination criterion is usually not worthwhile.

## Basis Identification

An interior-point optimizer does not return an optimal basic solution unless the problem has a unique primal and dual optimal solution. Therefore, the interior-point optimizer has an optional post-processing step that computes an optimal basic solution starting from the optimal interior-point solution. More information about the basis identification procedure may be found in [AY96]. In the following we provide an overall idea of the procedure.

There are some cases in which a basic solution could be more valuable:

- a basic solution is often more accurate than an interior-point solution,
- a basic solution can be used to warm-start the simplex algorithm in case of reoptimization,
- a basic solution is in general more sparse, i.e. more variables are fixed to zero. This is particularly appealing when solving continuous relaxation of mixed integer problems, as well as in all applications in which sparser solutions are preferred.

To illustrate how the basis identification routine works, we use the following trivial example:

$$\begin{array}{ll} \text{minimize} & x + y \\ \text{subject to} & x + y = 1, \\ & x, y \geq 0. \end{array}$$

It is easy to see that all feasible solutions are also optimal. In particular, there are two basic solutions namely

$$\begin{array}{ll} (x_1^*, y_1^*) &= (1, 0), \\ (x_2^*, y_2^*) &= (0, 1). \end{array}$$



The interior point algorithm will actually converge to the center of the optimal set, i.e. to  $(x^*, y^*) = (1/2, 1/2)$  (to see this in **MOSEK** deactivate *Presolve*).

In practice, when the algorithm gets close to the optimal solution, it is possible to construct in polynomial time an initial basis for the simplex algorithm from the current interior point solution. This basis is used to warm-start the simplex algorithm that will provide the optimal basic solution.

In most cases the constructed basis is optimal, or very few iterations are required by the simplex algorithm to make it optimal and hence the final *clean* phase be short. However, in some cases for nasty problems e.g. ill-conditioned problems the additional simplex clean up phase may take of lot a time.

By default **MOSEK** performs a basis identification. However, if a basic solution is not needed, the basis identification procedure can be turned off. The parameters

- `MSK_IPAR_INTPNT_BASIS`,
- `MSK_IPAR_BI_IGNORE_MAX_ITER`, and
- `MSK_IPAR_BI_IGNORE_NUM_ERROR`

control when basis identification is performed.

The type of simplex algorithm to be used can be tuned by the `MSK_IPAR_BI_CLEAN_OPTIMIZER` parameter i.e. primal or dual simplex, and the maximum number of iterations can be set by the `MSK_IPAR_BI_MAX_ITERATIONS`.

Finally, it should be mentioned that there is no guarantee on which basic solution will be returned.

## The Interior-point Log

Below is a typical log output from the interior-point optimizer presented:

Optimizer	- threads	:	1						
Optimizer	- solved problem	:	the dual						
Optimizer	- Constraints	:	2						
Optimizer	- Cones	:	0						
Optimizer	- Scalar variables	:	6	conic	:	0			
Optimizer	- Semi-definite variables:	:	0	scalarized	:	0			
Factor	- setup time	:	0.00	dense det. time	:	0.00			
Factor	- ML order time	:	0.00	GP order time	:	0.00			
Factor	- nonzeros before factor	:	3	after factor	:	3			
Factor	- dense dim.	:	0	flops	:	7.00e+001			
ITE	PFEAS	DFEAS	GFEAS	PRSTATUS	POBJ	DOBJ	MU	TIME	
0	1.0e+000	8.6e+000	6.1e+000	1.00e+000	0.000000000e+000	-2.208000000e+003	1.0e+000	0.00	
1	1.1e+000	2.5e+000	1.6e-001	0.00e+000	-7.901380925e+003	-7.394611417e+003	2.5e+000	0.00	
2	1.4e-001	3.4e-001	2.1e-002	8.36e-001	-8.113031650e+003	-8.055866001e+003	3.3e-001	0.00	
3	2.4e-002	5.8e-002	3.6e-003	1.27e+000	-7.777530698e+003	-7.766471080e+003	5.7e-002	0.01	
4	1.3e-004	3.2e-004	2.0e-005	1.08e+000	-7.668323435e+003	-7.668207177e+003	3.2e-004	0.01	
5	1.3e-008	3.2e-008	2.0e-009	1.00e+000	-7.668000027e+003	-7.668000015e+003	3.2e-008	0.01	
6	1.3e-012	3.2e-012	2.0e-013	1.00e+000	-7.667999994e+003	-7.667999994e+003	3.2e-012	0.01	

The first line displays the number of threads used by the optimizer and second line tells that the optimizer chose to solve the dual problem rather than the primal problem. The next line displays the problem dimensions as seen by the optimizer, and the `Factor...` lines show various statistics. This is followed by the iteration log.

Using the same notation as in Section 6.2.2 the columns of the iteration log have the following meaning:

- ITE: Iteration index.
- PFEAS:  $\|Ax^k - b\tau^k\|_\infty$ . The numbers in this column should converge monotonically towards zero but may stall at low level due to rounding errors.
- DFEAS:  $\|A^T y^k + s^k - c\tau^k\|_\infty$ . The numbers in this column should converge monotonically toward zero but may stall at low level due to rounding errors.

- **GFEAS**:  $|-c^T x^k + b^T y^k - \kappa^k|$ . The numbers in this column should converge monotonically toward zero but may stall at low level due to rounding errors.
- **PRSTATUS**: This number converges to 1 if the problem has an optimal solution whereas it converges to  $-1$  if that is not the case.
- **POBJ**:  $c^T x^k / \tau^k$ . An estimate for the primal objective value.
- **DOBJ**:  $b^T y^k / \tau^k$ . An estimate for the dual objective value.
- **MU**:  $\frac{(x^k)^T s^k + \tau^k \kappa^k}{n+1}$ . The numbers in this column should always converge monotonically to zero.
- **TIME**: Time spend since the optimization started.

### 6.2.3 The simplex Based Optimizer

An alternative to the interior-point optimizer is the simplex optimizer.

The simplex optimizer uses a different method that allows exploiting an initial guess for the optimal solution to reduce the solution time. Depending on the problem it may be faster or slower to use an initial guess; see section 6.2.4 for a discussion.

**MOSEK** provides both a primal and a dual variant of the simplex optimizer — we will return to this later.

#### Simplex Termination Criterion

The simplex optimizer terminates when it finds an optimal basic solution or an infeasibility certificate. A basic solution is optimal when it is primal and dual feasible; see Section 5.1 and 5.1.1 for a definition of the primal and dual problem. Due to the fact that computations are performed in finite precision **MOSEK** allows violation of primal and dual feasibility within certain tolerances. The user can control the allowed primal and dual tolerances with the parameters `MSK_DPAR_BASIS_TOL_X` and `MSK_DPAR_BASIS_TOL_S`.

#### Starting From an Existing Solution

When using the simplex optimizer it may be possible to reuse an existing solution and thereby reduce the solution time significantly. When a simplex optimizer starts from an existing solution it is said to perform a *warm-start*. If the user is solving a sequence of optimization problems by solving the problem, making modifications, and solving again, **MOSEK** will warm-start automatically.

Setting the parameter `MSK_IPAR_OPTIMIZER` to `MSK_OPTIMIZER_FREE_SIMPLEX` instructs **MOSEK** to select automatically between the primal and the dual simplex optimizers. Hence, **MOSEK** tries to choose the best optimizer for the given problem and the available solution.

By default **MOSEK** uses presolve when performing a warm-start. If the optimizer only needs very few iterations to find the optimal solution it may be better to turn off the presolve.

#### Numerical Difficulties in the Simplex Optimizers

Though **MOSEK** is designed to minimize numerical instability, completely avoiding it is impossible when working in finite precision. **MOSEK** counts a “numerical unexpected behavior” event inside the optimizer as a *set-back*. The user can define how many set-backs the optimizer accepts; if that number is exceeded, the optimization will be aborted. Set-backs are implemented to avoid long sequences where the optimizer tries to recover from an unstable situation.

Set-backs are, for example, repeated singularities when factorizing the basis matrix, repeated loss of feasibility, degeneracy problems (no progress in objective) and other events indicating numerical difficulties. If the simplex optimizer encounters a lot of set-backs the problem is usually badly scaled; in such

a situation try to reformulate into a better scaled problem. Then, if a lot of set-backs still occur, trying one or more of the following suggestions may be worthwhile:

- Raise tolerances for allowed primal or dual feasibility: Hence, increase the value of
  - `MSK_DPAR_BASIS_TOL_X`, and
  - `MSK_DPAR_BASIS_TOL_S`.
- Raise or lower pivot tolerance: Change the `MSK_DPAR_SIMPLEX_ABS_TOL_PIV` parameter.
- Switch optimizer: Try another optimizer.
- Switch off crash: Set both `MSK_IPAR_SIM_PRIMAL_CRASH` and `MSK_IPAR_SIM_DUAL_CRASH` to 0.
- Experiment with other pricing strategies: Try different values for the parameters
  - `MSK_IPAR_SIM_PRIMAL_SELECTION` and
  - `MSK_IPAR_SIM_DUAL_SELECTION`.
- If you are using warm-starts, in rare cases switching off this feature may improve stability. This is controlled by the `MSK_IPAR_SIM_HOTSTART` parameter.
- Increase maximum set backs allowed controlled by `MSK_IPAR_SIM_MAX_NUM_SETBACKS`.
- If the problem repeatedly becomes infeasible try switching off the special degeneracy handling. See the parameter `MSK_IPAR_SIM_DEGEN` for details.

#### 6.2.4 The Interior-point or the Simplex Optimizer?

Given a linear optimization problem, which optimizer is the best: The primal simplex, the dual simplex or the interior-point optimizer?

It is impossible to provide a general answer to this question. However, the interior-point optimizer behaves more predictably: it tends to use between 20 and 100 iterations, almost independently of problem size, but cannot perform warm-start, while simplex can take advantage of an initial solution, but is less predictable for cold-start. The interior-point optimizer is used by default.

#### 6.2.5 The Primal or the Dual Simplex Variant?

**MOSEK** provides both a primal and a dual simplex optimizer. Predicting which simplex optimizer is faster is impossible, however, in recent years the dual optimizer has seen several algorithmic and computational improvements, which, in our experience, makes it faster on average than the primal simplex optimizer. Still, it depends much on the problem structure and size.

Setting the `MSK_IPAR_OPTIMIZER` parameter to `MSK_OPTIMIZER_FREE_SIMPLEX` instructs **MOSEK** to choose which simplex optimizer to use automatically.

To summarize, if you want to know which optimizer is faster for a given problem type, you should try all the optimizers.

### 6.3 Conic Optimization

#### 6.3.1 The Interior-point Optimizer

For conic optimization problems only an interior-point type optimizer is available. The interior-point optimizer is an implementation of the so-called homogeneous and self-dual algorithm. For a detailed description of the algorithm, please see [\[ART03\]](#).

## Interior-point Termination Criteria

The parameters controlling when the conic interior-point optimizer terminates are shown in [Table 6.2](#).

Table 6.2: Parameters employed in termination criterion.

Parameter name	Purpose
<i>MSK_DPAR_INTPNT_CO_TOL_PFEAS</i>	Controls primal feasibility
<i>MSK_DPAR_INTPNT_CO_TOL_DFEAS</i>	Controls dual feasibility
<i>MSK_DPAR_INTPNT_CO_TOL_REL_GAP</i>	Controls relative gap
<i>MSK_DPAR_INTPNT_TOL_INFEAS</i>	Controls when the problem is declared infeasible
<i>MSK_DPAR_INTPNT_CO_TOL_MU_RED</i>	Controls when the complementarity is reduced enough

## 6.4 Nonlinear Convex Optimization

### 6.4.1 The Interior-point Optimizer

For quadratic, quadratically constrained, and general convex optimization problems an interior-point type optimizer is available. The interior-point optimizer is an implementation of the homogeneous and self-dual algorithm. For a detailed description of the algorithm, please see [\[AY98\]](#), [\[AY99\]](#).

#### The Convexity Requirement

Continuous nonlinear problems are required to be convex. For quadratic problems **MOSEK** test this requirement before optimizing. Specifying a non-convex problem results in an error message.

The following parameters are available to control the convexity check:

- *MSK\_IPAR\_CHECK\_CONVEXITY*: Turn convexity check on/off.
- *MSK\_DPAR\_CHECK\_CONVEXITY\_REL\_TOL*: Tolerance for convexity check.
- *MSK\_IPAR\_LOG\_CHECK\_CONVEXITY*: Turn on more log information for debugging.

#### The Differentiability Requirement

The nonlinear optimizer in **MOSEK** requires both first order and second order derivatives. This of course implies care should be taken when solving problems involving non-differentiable functions.

For instance, the function

$$f(x) = x^2$$

is differentiable everywhere whereas the function

$$f(x) = \sqrt{x}$$

is only differentiable for  $x > 0$ . In order to make sure that **MOSEK** evaluates the functions at points where they are differentiable, the function domains must be defined by setting appropriate variable bounds.

In general, if a variable is not ranged **MOSEK** will only evaluate that variable at points strictly within the bounds. Hence, imposing the bound

$$x \geq 0$$

in the case of  $\sqrt{x}$  is sufficient to guarantee that the function will only be evaluated in points where it is differentiable.

However, if a function is differentiable on a closed range, specifying the variable bounds is not sufficient. Consider the function

$$f(x) = \frac{1}{x} + \frac{1}{1-x}. \quad (6.6)$$

In this case the bounds

$$0 \leq x \leq 1$$

will not guarantee that **MOSEK** only evaluates the function for  $x$  between 0 and 1. To force **MOSEK** to strictly satisfy both bounds on ranged variables set the parameter `MSK_IPAR_INTPNT_STARTING_POINT` to `MSK_STARTING_POINT_SATISFY_BOUNDS`.

For efficiency reasons it may be better to reformulate the problem than to force **MOSEK** to observe ranged bounds strictly. For instance, (6.6) can be reformulated as follows

$$\begin{aligned} f(x) &= \frac{1}{x} + \frac{1}{y} \\ 0 &= 1 - x - y \\ 0 &\leq x \\ 0 &\leq y. \end{aligned}$$

### Interior-point Termination Criteria

The parameters controlling when the general convex interior-point optimizer terminates are shown in Table 6.3.

Table 6.3: Parameters employed in termination criteria.

Parameter name	Purpose
<code>MSK_DPAR_INTPNT_NL_TOL_PFEAS</code>	Controls primal feasibility
<code>MSK_DPAR_INTPNT_NL_TOL_DFEAS</code>	Controls dual feasibility
<code>MSK_DPAR_INTPNT_NL_TOL_REL_GAP</code>	Controls relative gap
<code>MSK_DPAR_INTPNT_TOL_INFEAS</code>	Controls when the problem is declared infeasible
<code>MSK_DPAR_INTPNT_NL_TOL_MU_RED</code>	Controls when the complementarity is reduced enough

## 6.5 Using Multiple Threads in an Optimizer

If multiple cores are available then it is possible for **MOSEK** to take advantage of them to speed up the computation. However, please note the speedup achieved is going to be dependent on the problem characteristics e.g. the size of problem. Typically for smallish problems no speedup is obtained by exploiting multiple cores. In fact forcing **MOSEK** to use one core can increase speed because parallel overhead is avoided.

### 6.5.1 Thread Safety

The **MOSEK** API is thread-safe provided that a task is only modified or accessed from one thread at any given time. Also accessing two or more separate tasks from threads at the same time is safe. Sharing an environment between threads is safe.

### 6.5.2 Determinism

The optimizers are run-to-run deterministic which means if a problem is solved twice on the same computer using the same parameter setting and exactly the same input then exactly the same results is obtained. One qualification is that no time limits must be imposed because the time taken to perform an operation on a computer is dependent on many factors such as the current workload.

### 6.5.3 The Parallelized Interior-point Optimizer

By default the interior-point optimizer exploits multiple cores using multithreading. Hence, big tasks such as large dense matrix multiplication may be divided into several independent smaller tasks that can be computed independently. However, there is a computational overhead associated with exploiting multiple threads e.g. cost of the additional coordination etc. Therefore, it may be advantageous to turn off the multithreading for smallish problem using the parameter `MSK_IPAR_INTPNT_MULTI_THREAD`.

Moreover, when the interior-point optimizer is allowed to exploit multiple threads, then the parameter `MSK_IPAR_NUM_THREADS` controls the maximum number of threads (and therefore the number of cores) that **MOSEK** will employ.

## THE OPTIMIZER FOR MIXED-INTEGER PROBLEMS

A problem is a mixed-integer optimization problem when one or more of the variables are constrained to be integer valued. **MOSEK** can solve mixed-integer

- linear,
- quadratic and quadratically constrained, and
- conic quadratic

problems.

Readers unfamiliar with integer optimization are recommended to consult some relevant literature, e.g. the book [Wol98] by Wolsey.

### 7.1 Some Concepts and Facts Related to Mixed-integer Optimization

It is important to understand that in a worst-case scenario, the time required to solve integer optimization problems grows exponentially with the size of the problem. For instance, assume that a problem contains  $n$  binary variables, then the time required to solve the problem in the worst case may be proportional to  $2^n$ . The value of  $2^n$  is huge even for moderate values of  $n$ .

In practice this implies that the focus should be on computing a near optimal solution quickly rather than on locating an optimal solution. Even if the problem is only solved approximately, it is important to know how far the approximate solution is from an optimal one. In order to say something about the quality of an approximate solution the concept of *relaxation* is important.

The mixed-integer optimization problem

$$\begin{aligned} z^* = \quad & \text{minimize} && c^T x \\ & \text{subject to} && Ax = b, \\ & && x \geq 0 \\ & && x_j \in \mathbb{Z}, \quad \forall j \in \mathcal{J}, \end{aligned} \tag{7.1}$$

has the continuous relaxation

$$\begin{aligned} \underline{z} = \quad & \text{minimize} && c^T x \\ & \text{subject to} && Ax = b, \\ & && x \geq 0 \end{aligned} \tag{7.2}$$

The continuous relaxation is identical to the mixed-integer problem with the restriction that some variables must be integers removed.

There are two important observations about the continuous relaxation. First, the continuous relaxation is usually much faster to optimize than the mixed-integer problem. Secondly if  $\hat{x}$  is any feasible solution to (7.1) and

$$\bar{z} := c^T \hat{x}$$

then

$$\underline{z} \leq z^* \leq \bar{z}.$$

This is an important observation since if it is only possible to find a near optimal solution within a reasonable time frame then the quality of the solution can nevertheless be evaluated. The value  $\underline{z}$  is a lower bound on the optimal objective value. This implies that the obtained solution is no further away from the optimum than  $\bar{z} - \underline{z}$  in terms of the objective value.

Whenever a mixed-integer problem is solved **MOSEK** reports this lower bound so that the quality of the reported solution can be evaluated.

## 7.2 The Mixed-integer Optimizer

The mixed-integer optimizer can handle problems with linear, quadratic objective and constraints and conic constraints. However, a problem can not contain both quadratic objective or constraints and conic constraints.

The mixed-integer optimizer is specialized for solving linear and conic optimization problems. It can also solve pure quadratic and quadratically constrained problems; these problems are automatically converted to conic problems before being solved.

The mixed-integer optimizer is run-to-run deterministic. This means that if a problem is solved twice on the same computer with identical options then the obtained solution will be bit-for-bit identical for the two runs. However, if a time limit is set then this may not be case since the time taken to solve a problem is not deterministic. The mixed-integer optimizer is parallelized i.e. it can exploit multiple cores during the optimization.

The solution process can be split into these phases:

1. **Presolve:** In this phase the optimizer tries to reduce the size of the problem and improve the formulation using preprocessing techniques. The presolve stage can be turned off using the `MSK_IPAR_PRESOLVE_USE` parameter
2. **Cut generation:** Valid inequalities (cuts) are added to improve the lower bound
3. **Heuristic:** Using heuristics the optimizer tries to guess a good feasible solution. Heuristics can be controlled by the parameter `MSK_IPAR_MIO_HEURISTIC_LEVEL`
4. **Search:** The optimal solution is located by branching on integer variables

## 7.3 Termination Criterion

In general, it is time consuming to find an exact feasible and optimal solution to an integer optimization problem, though in many practical cases it may be possible to find a sufficiently good solution. Therefore, the mixed-integer optimizer employs a relaxed feasibility and optimality criterion to determine when a satisfactory solution is located.

A candidate solution that is feasible for the continuous relaxation is said to be an integer feasible solution if the criterion

$$\min(x_j - \lfloor x_j \rfloor, \lceil x_j \rceil - x_j) \leq \delta_1 \quad \forall j \in \mathcal{J}$$

is satisfied, meaning that  $x_j$  is at most  $\delta_1$  from the nearest integer.

Whenever the integer optimizer locates an integer feasible solution it will check if the criterion

$$\bar{z} - \underline{z} \leq \max(\delta_2, \delta_3 \max(10^{-10}, |\bar{z}|))$$



is satisfied. If this is the case, the integer optimizer terminates and reports the integer feasible solution as an optimal solution. Please note that  $\underline{z}$  is a valid lower bound determined by the integer optimizer during the solution process, i.e.

$$\underline{z} \leq z^*.$$

The lower bound  $\underline{z}$  normally increases during the solution process.

### 7.3.1 Relaxed Termination

If an optimal solution cannot be located within a reasonable time, it may be advantageous to employ a relaxed termination criterion after some time. Whenever the integer optimizer locates an integer feasible solution and has spent at least the number of seconds defined by the *MSK\_DPAR\_MIO\_DISABLE\_TERM\_TIME* parameter on solving the problem, it will check whether the criterion

$$\bar{z} - \underline{z} \leq \max(\delta_4, \delta_5 \max(10^{-10}, |\bar{z}|))$$

is satisfied. If it is satisfied, the optimizer will report that the candidate solution is **near optimal** and then terminate. Please note that since this criterion depends on timing, the optimizer will not be run to run deterministic.

## 7.4 Parameters Affecting the Termination of the Integer Optimizer.

All  $\delta$  tolerances can be adjusted using suitable parameters — see Table 7.1.

Table 7.1: Tolerances for the mixed-integer optimizer.

Tolerance	Parameter name
$\delta_1$	<i>MSK_DPAR_MIO_TOL_ABS_RELAX_INT</i>
$\delta_2$	<i>MSK_DPAR_MIO_TOL_ABS_GAP</i>
$\delta_3$	<i>MSK_DPAR_MIO_TOL_REL_GAP</i>
$\delta_4$	<i>MSK_DPAR_MIO_NEAR_TOL_ABS_GAP</i>
$\delta_5$	<i>MSK_DPAR_MIO_NEAR_TOL_REL_GAP</i>

In Table 7.2 some other parameters affecting the integer optimizer termination criterion are shown. Please note that if the effect of a parameter is delayed, the associated termination criterion is applied only after some time, specified by the *MSK\_DPAR\_MIO\_DISABLE\_TERM\_TIME* parameter.

Table 7.2: Other parameters affecting the integer optimizer termination criterion.

Parameter name	De- layed	Explanation
<i>MSK_IPAR_MIO_MAX_NUM_BRANCHES</i>	Yes	Maximum number of branches allowed.
<i>MSK_IPAR_MIO_MAX_NUM_RELAXS</i>	Yes	Maximum number of relaxations allowed.
<i>MSK_IPAR_MIO_MAX_NUM_SOLUTIONS</i>	Yes	Maximum number of feasible integer solutions allowed.

## 7.5 How to Speed Up the Solution Process

As mentioned previously, in many cases it is not possible to find an optimal solution to an integer optimization problem in a reasonable amount of time. Some suggestions to reduce the solution time are:

- Relax the termination criterion: In case the run time is not acceptable, the first thing to do is to relax the termination criterion — see Section 7.3 for details.
- Specify a good initial solution: In many cases a good feasible solution is either known or easily computed using problem specific knowledge. If a good feasible solution is known, it is usually worthwhile to use this as a starting point for the integer optimizer.
- Improve the formulation: A mixed-integer optimization problem may be impossible to solve in one form and quite easy in another form. However, it is beyond the scope of this manual to discuss good formulations for mixed-integer problems. For discussions on this topic see for example [\[Wol98\]](#).

## 7.6 Understanding Solution Quality

To determine the quality of the solution one should check the following:

- The solution status key returned by **MOSEK**
- The *optimality gap*: A measure of how much the located solution can deviate from the optimal solution to the problem
- Feasibility. How much the solution violates the constraints of the problem

The *optimality gap* is a measure for how close the solution is to the optimal solution. The optimality gap is given by

$$\epsilon = |(\text{objective value of feasible solution}) - (\text{objective bound})|.$$

The objective value of the solution is guaranteed to be within  $\epsilon$  of the optimal solution.

The optimality gap can be retrieved through the solution item `MSK_DINF_MIO_OBJ_ABS_GAP`. Often it is more meaningful to look at the optimality gap normalized with the magnitude of the solution. The relative optimality gap is available in `MSK_DINF_MIO_OBJ_REL_GAP`.

## PROBLEM ANALYZER

The problem analyzer prints a detailed survey of the

- linear constraints and objective
- quadratic constraints
- conic constraints
- variables

of the model.

In the initial stages of model formulation the problem analyzer may be used as a quick way of verifying that the model has been built or imported correctly. In later stages it can help revealing special structures within the model that may be used to tune the optimizer's performance or to identify the causes of numerical difficulties.

The problem analyzer is run from the command line using the *-anapro* argument and produces something similar to the following (this is the problem analyzer's survey of the *aflow30a* problem from the MIPLIB 2003 collection.)

Analyzing the problem

Constraints		Bounds		Variables	
upper bd:	421	ranged	: all	cont:	421
fixed :	58			bin :	421

-----

Objective, min cx

range: min  c :	0.00000	min  c >0:	11.0000	max  c :	500.000
distrib:	c	vars			
	0	421			
	[11, 100)	150			
	[100, 500]	271			

-----

Constraint matrix A has

479 rows (constraints)  
842 columns (variables)  
2091 (0.518449%) nonzero entries (coefficients)

Row nonzeros, A\_i

range: min A_i:	2 (0.23753%)	max A_i:	34 (4.038%)
distrib:	A_i	rows	rows% acc%
	2	421	87.89 87.89
	[8, 15]	20	4.18 92.07
	[16, 31]	30	6.26 98.33
	[32, 34]	8	1.67 100.00

```

Column nonzeros, A|j
  range: min A|j: 2 (0.417537%)    max A|j: 3 (0.626305%)
distrib:      A|j      cols      cols%      acc%
              2        435        51.66        51.66
              3        407        48.34        100.00

A nonzeros, A(ij)
  range: min |A(ij)|: 1.00000    max |A(ij)|: 100.000
distrib:      A(ij)      coeffs
              [1, 10)      1670
              [10, 100]    421

```

```

-----
Constraint bounds, lb <= Ax <= ub
distrib:      |b|      lbs      lbs      ub
              0        421
              [1, 10]    58      58

```

```

Variable bounds, lb <= x <= ub
distrib:      |b|      lbs      lbs      ub
              0        842
              [1, 10)    421
              [10, 100]  421

```

The survey is divided into six different sections, each described below. To keep the presentation short with focus on key elements the analyzer generally attempts to display information on issues relevant for the current model only: E.g., if the model does not have any conic constraints (this is the case in the example above) or any integer variables, those parts of the analysis will not appear.

## 8.1 General Characteristics

The first part of the survey consists of a brief summary of the model's linear and quadratic constraints (indexed by  $i$ ) and variables (indexed by  $j$ ). The summary is divided into three subsections:

### Constraints

- **upper bd** The number of upper bounded constraints,  $\sum_{j=0}^{n-1} a_{ij}x_j \leq u_i^c$
- **lower bd** The number of lower bounded constraints,  $l_i^c \leq \sum_{j=0}^{n-1} a_{ij}x_j$
- **ranged** The number of ranged constraints,  $l_i^c \leq \sum_{j=0}^{n-1} a_{ij}x_j \leq u_i^c$
- **fixed** The number of fixed constraints,  $l_i^c = \sum_{j=0}^{n-1} a_{ij}x_j = u_i^c$
- **free** The number of free constraints

### Bounds

- **upper bd** The number of upper bounded variables,  $x_j \leq u_j^x$
- **lower bd** The number of lower bounded variables,  $l_k^x \leq x_j$
- **ranged** The number of ranged variables,  $l_k^x \leq x_j \leq u_j^x$
- **fixed** The number of fixed variables,  $l_k^x = x_j = u_j^x$

- **free** The number of free variables

#### Variables

- **cont** The number of continuous variables,  $x_j \in \mathbb{R}$
- **bin** The number of binary variables,  $x_j \in \{0, 1\}$
- **int** The number of general integer variables,  $x_j \in \mathbb{Z}$

Only constraints, bounds and domains actually in the model will be reported on; if all entities in a section turn out to be of the same kind, the number will be replaced by **all** for brevity.

## 8.2 Objective

The second part of the survey focuses on (the linear part of) the objective, summarizing the optimization sense and the coefficients' absolute value range and distribution. The number of 0 (zero) coefficients is singled out (if any such variables are in the problem).

The range is displayed using three terms:

- **min |c|** The minimum absolute value among all coefficients
- **min |c|>0** The minimum absolute value among the nonzero coefficients
- **max |c|** The maximum absolute value among the coefficients

If some of these extrema turn out to be equal, the display is shortened accordingly:

- If **min |c|** is greater than zero, the **min |c|>0** term is obsolete and will not be displayed
- If only one or two different coefficients occur this will be displayed using **all** and an explicit listing of the coefficients

The absolute value distribution is displayed as a table summarizing the numbers by orders of magnitude (with a ratio of 10). Again, the number of variables with a coefficient of 0 (if any) is singled out. Each line of the table is headed by an interval (half-open intervals including their lower bounds), and is followed by the number of variables with their objective coefficient in this interval. Intervals with no elements are skipped.

## 8.3 Linear Constraints

The third part of the survey displays information on the nonzero coefficients of the linear constraint matrix.

Following a brief summary of the matrix dimensions and the number of nonzero coefficients in total, three sections provide further details on how the nonzero coefficients are distributed by row-wise count (**A|j**), by column-wise count (**A|i**), and by absolute value (**|A(ij)|**). Each section is headed by a brief display of the distribution's range (**min** and **max**), and for the row/column-wise counts the corresponding densities are displayed too (in parentheses).

The distribution tables single out three particularly interesting counts: zero, one, and two nonzeros per row/column; the remaining row/column nonzeros are displayed by orders of magnitude (ratio 2). For each interval the relative and accumulated relative counts are also displayed.

Note that constraints may have both linear and quadratic terms, but the empty rows and columns reported in this part of the survey relate to the linear terms only. If empty rows and/or columns are found in the linear constraint matrix, the problem is analyzed further in order to determine if the corresponding constraints have any quadratic terms or the corresponding variables are used in conic or quadratic constraints.

The distribution of the absolute values,  $|A(ij)|$ , is displayed just as for the objective coefficients described above.

## 8.4 Constraint and Variable Bounds

The fourth part of the survey displays distributions for the absolute values of the finite lower and upper bounds for both constraints and variables. The number of bounds at 0 is singled out and, otherwise, displayed by orders of magnitude (with a ratio of 10).

## 8.5 Quadratic Constraints

The fifth part of the survey displays distributions for the nonzero elements in the gradient of the quadratic constraints, i.e. the nonzero row counts for the column vectors  $Qx$ . The table is similar to the tables for the linear constraints' nonzero row and column counts described in the survey's third part.

---

**Note:** Quadratic constraints may also have a linear part, but that will be included in the linear constraints survey; this means that if a problem has one or more pure quadratic constraints, part three of the survey will report an equal number of linear constraint rows with 0 (zero) nonzeros. Likewise, variables that appear in quadratic terms only will be reported as empty columns (0 nonzeros) in the linear constraint report.

---

## 8.6 Conic Constraints

The last part of the survey summarizes the model's conic constraints. For each of the two types of cones, quadratic and rotated quadratic, the total number of cones are reported, and the distribution of the cones' dimensions are displayed using intervals. Cone dimensions of 2, 3, and 4 are singled out.

## ANALYZING INFEASIBLE PROBLEMS

When developing and implementing a new optimization model, the first attempts will often be either infeasible, due to specification of inconsistent constraints, or unbounded, if important constraints have been left out.

In this section we will

- go over an example demonstrating how to locate infeasible constraints using the **MOSEK** infeasibility report tool,
- discuss in more general terms which properties may cause infeasibilities, and
- present the more formal theory of infeasible and unbounded problems.

### 9.1 Example: Primal Infeasibility

A problem is said to be *primal infeasible* if no solution exists that satisfies all the constraints of the problem.

As an example of a primal infeasible problem consider the problem of minimizing the cost of transportation between a number of production plants and stores: Each plant produces a fixed number of goods, and each store has a fixed demand that must be met. Supply, demand and cost of transportation per unit are given in Fig. 9.1.

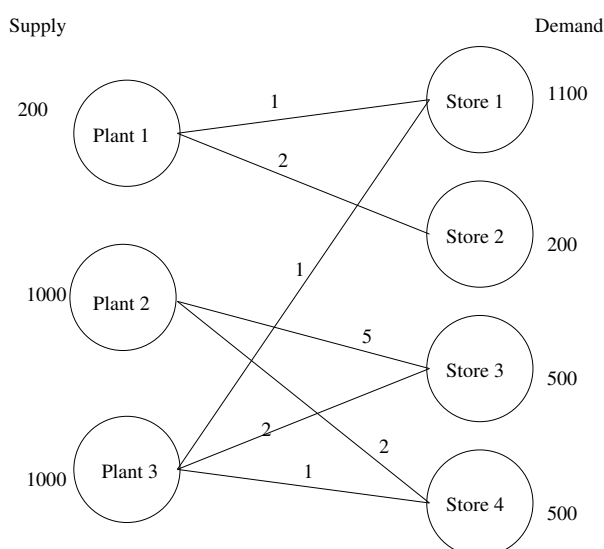


Fig. 9.1: Supply, demand and cost of transportation.

The problem represented in Fig. 9.1 is infeasible, since the total demand

$$2300 = 1100 + 200 + 500 + 500$$

exceeds the total supply

$$2200 = 200 + 1000 + 1000$$

If we denote the number of transported goods from plant  $i$  to store  $j$  by  $x_{ij}$ , the problem can be formulated as the LP:

$$\begin{array}{llllllllllll}
 \text{minimize} & x_{11} & + & 2x_{12} & + & 5x_{23} & + & 2x_{24} & + & x_{31} & + & 2x_{33} & + & x_{34} \\
 \text{subject to} & x_{11} & + & x_{12} & & & & & & & & & & \leq 200, \\
 & & & & & x_{23} & + & x_{24} & & & & & & \leq 1000, \\
 & & & & & & & & x_{31} & + & x_{33} & + & x_{34} & \leq 1000, \\
 & x_{11} & & & & & & & + & x_{31} & & & & = 1100, \quad (9.1) \\
 & & x_{12} & & & & & & & & & & & = 200, \\
 & & & x_{23} & + & & & & & & x_{33} & & & = 500, \\
 & & & & & x_{24} & + & & & & & x_{34} & = 500, \\
 & x_{ij} & \geq 0.
 \end{array}$$

Solving problem (9.1) using **MOSEK** will result in a solution, a solution status and a problem status. Among the log output from the execution of **MOSEK** on the above problem are the lines:

```

Basic solution
Problem status : PRIMAL_INFEASIBLE
Solution status : PRIMAL_INFEASIBLE_CER

```

The first line indicates that the problem status is primal infeasible. The second line says that a *certificate of the infeasibility* was found. The certificate is returned in place of the solution to the problem.

## 9.2 Locating the cause of Primal Infeasibility

Usually a primal infeasible problem status is caused by a mistake in formulating the problem and therefore the question arises: *What is the cause of the infeasible status?* When trying to answer this question, it is often advantageous to follow these steps:

- Remove the objective function. This does not change the infeasibility status but simplifies the problem, eliminating any possibility of issues related to the objective function.
- Consider whether your problem has some necessary conditions for feasibility and examine if these are satisfied, e.g. total supply should be greater than or equal to total demand.
- Verify that coefficients and bounds are reasonably sized in your problem.

If the problem is still primal infeasible, some of the constraints must be relaxed or removed completely. The **MOSEK** infeasibility report (Section 9.4) may assist you in finding the constraints causing the infeasibility.

Possible ways of relaxing your problem include:

- Increasing (decreasing) upper (lower) bounds on variables and constraints.
- Removing suspected constraints from the problem.

Returning to the transportation example, we discover that removing the fifth constraint

$$x_{12} = 200$$

makes the problem feasible.

## 9.3 Locating the Cause of Dual Infeasibility

A problem may also be *dual infeasible*. In this case the primal problem is often unbounded, meaning that feasible solutions exist such that the objective tends towards infinity. An example of a dual infeasible



and primal unbounded problem is:

$$\begin{array}{ll}\text{minimize} & x_1 \\ \text{subject to} & x_1 \leq 5.\end{array}$$

To resolve a dual infeasibility the primal problem must be made more restricted by

- Adding upper or lower bounds on variables or constraints.
- Removing variables.
- Changing the objective.

### 9.3.1 A cautionary note

The problem

$$\begin{array}{ll}\text{minimize} & 0 \\ \text{subject to} & 0 \leq x_1, \\ & x_j \leq x_{j+1}, \quad j = 1, \dots, n-1, \\ & x_n \leq -1\end{array}$$

is clearly infeasible. Moreover, if any one of the constraints is dropped, then the problem becomes feasible.

This illustrates the worst case scenario where all, or at least a significant portion of the constraints are involved in causing infeasibility. Hence, it may not always be easy or possible to pinpoint a few constraints responsible for infeasibility.

## 9.4 The Infeasibility Report

**MOSEK** includes functionality for diagnosing the cause of a primal or a dual infeasibility. It can be turned on by setting the `MSK_IPAR_INFEAS_REPORT_AUTO` to `MSK_ON`. This causes **MOSEK** to print a report on variables and constraints involved in the infeasibility.

The `MSK_IPAR_INFEAS_REPORT_LEVEL` parameter controls the amount of information presented in the infeasibility report. The default value is 1.

### 9.4.1 Example: Primal Infeasibility

We will keep working with the problem (9.1) written in LP format:

Listing 9.1: The code for problem (9.1).

```
\
\ An example of an infeasible linear problem.
\
minimize
  obj: + 1 x11 + 2 x12
        + 5 x23 + 2 x24
        + 1 x31 + 2 x33 + 1 x34
st
  s0: + x11 + x12          <= 200
  s1: + x23 + x24          <= 1000
  s2: + x31 + x33 + x34    <= 1000
  d1: + x11 + x31          = 1100
  d2: + x12                = 200
  d3: + x23 + x33          = 500
  d4: + x24 + x34          = 500
bounds
end
```

Using the command line (please remember it accepts options following the C API format)

```
mosek -d MSK_IPAR_INFEAS_REPORT_AUTO MSK_ON infeas.lp
```

MOSEK produces the following infeasibility report:

MOSEK PRIMAL INFEASIBILITY REPORT.

Problem status: The problem is primal infeasible

The following constraints are involved in the primal infeasibility.

Index	Name	Lower bound	Upper bound	Dual lower	Dual upper
0	s0	NONE	2.000000e+002	0.000000e+000	1.000000e+000
2	s2	NONE	1.000000e+003	0.000000e+000	1.000000e+000
3	d1	1.100000e+003	1.100000e+003	1.000000e+000	0.000000e+000
4	d2	2.000000e+002	2.000000e+002	1.000000e+000	0.000000e+000

The following bound constraints are involved in the infeasibility.

Index	Name	Lower bound	Upper bound	Dual lower	Dual upper
8	x33	0.000000e+000	NONE	1.000000e+000	0.000000e+000
10	x34	0.000000e+000	NONE	1.000000e+000	0.000000e+000

The infeasibility report is divided into two sections corresponding to constraints and variables. It is a selection of those lines from the problem solution (in this case the file `infeas.sol`), which are important in understanding primal infeasibility. In this case the constraints `s0`, `s2`, `d1`, `d2` and variables `x33`, `x34` are of importance.

The columns `Dual lower` and `Dual upper` contain the values of dual variables  $s_l^c$ ,  $s_u^c$ ,  $s_l^x$  and  $s_u^x$  in the primal infeasibility certificate (see Section 5.1.2.1). Only the non-zero ones, which contribute to the optimization objective and thus are important for infeasibility, are shown.

It is also possible to obtain the infeasible subproblem. The command line

```
mosek -d MSK_IPAR_INFEAS_REPORT_AUTO MSK_ON infeas.lp -info rinfeas.lp
```

produces the files `rinfeas.bas.inf.lp`. In this case the content of the file `rinfeas.bas.inf.lp` is

```
minimize
obj:  + 0 x11 + 0 x12 + 0 x13 + 0 x21 + 0 x22 + 0 x23
      + 0 x31 + 0 x32 + 0 x33 + 0 x24 + 0 x34
subject to
s0:  + x11 + x12 <= 2e+02
s2:  + x31 + x33 + x34 <= 1e+03
d1:  + x11 + x31 = 1.1e+03
d2:  + x12 = 2e+02
bounds
x11 free
x12 free
x13 free
x21 free
x22 free
x23 free
x31 free
x32 free
0 <= x33 <= +infinity
x24 free
0 <= x34 <= +infinity
end
```

which is an optimization problem. This problem is identical to (9.1), except that the objective and some of the constraints and bounds have been removed. Executing the command

```
mosek -d MSK_IPAR_INFEAS_REPORT_AUTO MSK_ON rinfeas.bas.inf.lp
```

demonstrates that the reduced problem is **primal infeasible**. Since the reduced problem is usually smaller than original problem, it should be easier to locate the cause of infeasibility in this rather than in the original (9.1).

### 9.4.2 Example: Dual Infeasibility

The following problem is dual to (9.1) and therefore it is dual infeasible.

Listing 9.2: The dual of problem (9.1).

```
maximize + 200 y1 + 1000 y2 + 1000 y3 + 1100 y4 + 200 y5 + 500 y6 + 500 y7
subject to
  x11: y1+y4 < 1
  x12: y1+y5 < 2
  x23: y2+y6 < 5
  x24: y2+y7 < 2
  x31: y3+y4 < 1
  x33: y3+y6 < 2
  x34: y3+y7 < 1
bounds
  -inf <= y1 < 0
  -inf <= y2 < 0
  -inf <= y3 < 0
  y4 free
  y5 free
  y6 free
  y7 free
end
```

This can be verified by proving that

$$(y_1, \dots, y_7) = (-1, 0, -1, 1, 1, 0, 0)$$

is a certificate of dual infeasibility (see Section 5.1.2.2) as we can see from this report:

```
MOSEK DUAL INFEASIBILITY REPORT.

Problem status: The problem is dual infeasible

The following constraints are involved in the infeasibility.
```

Index	Name	Activity	Objective	Lower bound	Upper bound
5	x33	-1.000000e+00		NONE	2.000000e+00
6	x34	-1.000000e+00		NONE	1.000000e+00

```

The following variables are involved in the infeasibility.
```

Index	Name	Activity	Objective	Lower bound	Upper bound
0	y1	-1.000000e+00	2.000000e+02	NONE	0.000000e+00
2	y3	-1.000000e+00	1.000000e+03	NONE	0.000000e+00
3	y4	1.000000e+00	1.100000e+03	NONE	NONE
4	y5	1.000000e+00	2.000000e+02	NONE	NONE

```

Interior-point solution summary
  Problem status : DUAL_INFEASIBLE
  Solution status : DUAL_INFEASIBLE_CER
  Primal.  obj: 1.0000000000e+02   nrm: 1e+00   Viol.  con: 0e+00   var: 0e+00
```

Let  $y^*$  denote the reported primal solution. **MOSEK** states

- that the problem is *dual infeasible*,
- that the reported solution is a certificate of dual infeasibility, and
- that the infeasibility measure for  $y^*$  is approximately zero.

Since the original objective was maximization, we have that  $c^T y^* > 0$ . See Section 5.1.2 for how to interpret the parameter values in the infeasibility report for a linear program. We see that the variables  $y1$ ,  $y3$ ,  $y4$ ,  $y5$  and the constraints  $x33$  and  $x34$  contribute to infeasibility with non-zero values in the Activity column.

One possible strategy to *fix* the infeasibility is to modify the problem so that the certificate of infeasibility becomes invalid. In this case we could do one the following things:

- Add a lower bound on  $y3$ . This will directly invalidate the certificate of dual infeasibility.
- Increase the object coefficient of  $y3$ . Changing the coefficients sufficiently will invalidate the inequality  $c^T y^* > 0$  and thus the certificate.
- Add lower bounds on  $x11$  or  $x31$ . This will directly invalidate the certificate of infeasibility.

Please note that modifying the problem to invalidate the reported certificate does *not* imply that the problem becomes dual feasible — the reason for infeasibility may simply *move*, resulting a problem that is still infeasible, but for a different reason.

More often, the reported certificate can be used to give a hint about errors or inconsistencies in the model that produced the problem.

## 9.5 Theory Concerning Infeasible Problems

This section discusses the theory of infeasibility certificates and how **MOSEK** uses a certificate to produce an infeasibility report. In general, **MOSEK** solves the problem

$$\begin{array}{llll} \text{minimize} & & c^T x + c^f & \\ \text{subject to} & l^c \leq & Ax & \leq u^c, \\ & l^x \leq & x & \leq u^x \end{array} \quad (9.2)$$

where the corresponding dual problem is

$$\begin{array}{ll} \text{maximize} & (l^c)^T s_l^c - (u^c)^T s_u^c \\ & + (l^x)^T s_l^x - (u^x)^T s_u^x + c^f \\ \text{subject to} & A^T y + s_l^x - s_u^x = c, \\ & -y + s_l^c - s_u^c = 0, \\ & s_l^c, s_u^c, s_l^x, s_u^x \leq 0. \end{array} \quad (9.3)$$

We use the convention that for any bound that is not finite, the corresponding dual variable is fixed at zero (and thus will have no influence on the dual problem). For example

$$l_j^x = -\infty \quad \Rightarrow \quad (s_l^x)_j = 0$$

## 9.6 The Certificate of Primal Infeasibility

A certificate of primal infeasibility is *any* solution to the homogenized dual problem

$$\begin{array}{ll} \text{maximize} & (l^c)^T s_l^c - (u^c)^T s_u^c \\ & + (l^x)^T s_l^x - (u^x)^T s_u^x \\ \text{subject to} & A^T y + s_l^x - s_u^x = 0, \\ & -y + s_l^c - s_u^c = 0, \\ & s_l^c, s_u^c, s_l^x, s_u^x \leq 0. \end{array}$$

with a positive objective value. That is,  $(s_l^{c*}, s_u^{c*}, s_l^{x*}, s_u^{x*})$  is a certificate of primal infeasibility if

$$(l^c)^T s_l^{c*} - (u^c)^T s_u^{c*} + (l^x)^T s_l^{x*} - (u^x)^T s_u^{x*} > 0$$

and

$$\begin{aligned} A^T y + s_l^{x*} - s_u^{x*} &= 0, \\ -y + s_l^{c*} - s_u^{c*} &= 0, \\ s_l^{c*}, s_u^{c*}, s_l^{x*}, s_u^{x*} &\leq 0. \end{aligned}$$

The well-known *Farkas Lemma* tells us that (9.2) is infeasible if and only if a certificate of primal infeasibility exists.

Let  $(s_l^{c*}, s_u^{c*}, s_l^{x*}, s_u^{x*})$  be a certificate of primal infeasibility then

$$(s_l^{c*})_i > 0 ((s_u^{c*})_i > 0)$$

implies that the lower (upper) bound on the  $i$  th constraint is important for the infeasibility. Furthermore,

$$(s_l^{x*})_j > 0 ((s_u^{x*})_j > 0)$$

implies that the lower (upper) bound on the  $j$  th variable is important for the infeasibility.

## 9.7 The certificate of dual infeasibility

A certificate of dual infeasibility is *any* solution to the problem

$$\begin{aligned} &\text{minimize} && c^T x \\ &\text{subject to} && \bar{l}^c \leq Ax \leq \bar{u}^c, \\ &&& \bar{l}^x \leq x \leq \bar{u}^x \end{aligned}$$

with negative objective value, where we use the definitions

$$\bar{l}_i^c := \begin{cases} 0, & l_i^c > -\infty, \\ -\infty, & \text{otherwise,} \end{cases}, \quad \bar{u}_i^c := \begin{cases} 0, & u_i^c < \infty, \\ \infty, & \text{otherwise,} \end{cases}$$

and

$$\bar{l}_i^x := \begin{cases} 0, & l_i^x > -\infty, \\ -\infty, & \text{otherwise,} \end{cases} \quad \text{and} \quad \bar{u}_i^x := \begin{cases} 0, & u_i^x < \infty, \\ \infty, & \text{otherwise.} \end{cases}$$

Stated differently, a certificate of dual infeasibility is any  $x^*$  such that

$$\begin{aligned} c^T x^* &< 0, \\ \bar{l}^c &\leq Ax^* \leq \bar{u}^c, \\ \bar{l}^x &\leq x^* \leq \bar{u}^x \end{aligned} \tag{9.4}$$

The well-known Farkas Lemma tells us that (9.3) is infeasible if and only if a certificate of dual infeasibility exists.

Note that if  $x^*$  is a certificate of dual infeasibility then for any  $j$  such that

$$x_j^* \leq 0,$$

variable  $j$  is involved in the dual infeasibility.

Given the assumption that all weights are 1 then the command

```
mosek -primalrepair -d MSK_IPAR_LOG_FEAS_REPAIR 3 feasrepair.lp
```

will form the repaired problem and solve it. The parameter `MSK_IPAR_LOG_FEAS_REPAIR` controls the amount of log output from the repair. A value of 2 causes the optimal repair to be printed out.

The output from running the above command is:

```

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Open file 'feasrepair.lp'

Read summary
Type           : LO (linear optimization problem)
Objective sense : min
Constraints     : 4
Scalar variables : 2
Matrix variables : 0
Time           : 0.0

Computer
Platform       : Windows/64-X86
Cores          : 4

Problem
Name           :
Objective sense : min
Type           : LO (linear optimization problem)
Constraints     : 4
Cones          : 0
Scalar variables : 2
Matrix variables : 0
Integer variables : 0

Primal feasibility repair started.
Optimizer started.
Interior-point optimizer started.
Presolve started.
Linear dependency checker started.
Linear dependency checker terminated.
Eliminator started.
Total number of eliminations : 2
Eliminator terminated.
Eliminator - tries          : 1          time          : 0.00
Eliminator - elim's        : 2
Lin. dep. - tries          : 1          time          : 0.00
Lin. dep. - number         : 0
Presolve terminated. Time: 0.00
Optimizer - threads         : 1
Optimizer - solved problem  : the primal
Optimizer - Constraints     : 2
Optimizer - Cones          : 0
Optimizer - Scalar variables : 6          conic          : 0
Optimizer - Semi-definite variables: 0      scalarized      : 0
Factor - setup time         : 0.00        dense det. time : 0.00
Factor - ML order time      : 0.00        GP order time   : 0.00
Factor - nonzeros before factor : 3        after factor    : 3
Factor - dense dim.        : 0          flops           : 5.40e+001
ITE PFEAS   DFEAS   GFEAS   PRSTATUS   POBJ          DOBJ          MU          TIME
0   2.7e+001 1.0e+000 4.8e+000 1.00e+000 4.195228609e+000 0.000000000e+000 1.0e+000 0.00
1   2.4e+001 8.6e-001 1.5e+000 0.00e+000 1.227497414e+001 1.504971820e+001 2.6e+000 0.00
2   2.6e+000 9.7e-002 1.7e-001 -6.19e-001 4.363064729e+001 4.648523094e+001 3.0e-001 0.00
3   4.7e-001 1.7e-002 3.1e-002 1.24e+000 4.256803136e+001 4.298540657e+001 5.2e-002 0.00
4   8.7e-004 3.2e-005 5.7e-005 1.08e+000 4.249989892e+001 4.250078747e+001 9.7e-005 0.00
5   8.7e-008 3.2e-009 5.7e-009 1.00e+000 4.249999999e+001 4.250000008e+001 9.7e-009 0.00
6   8.7e-012 3.2e-013 5.7e-013 1.00e+000 4.250000000e+001 4.250000000e+001 9.7e-013 0.00
Basis identification started.
Primal basis identification phase started.
ITER      TIME
0          0.00
Primal basis identification phase terminated. Time: 0.00

```

```

Dual basis identification phase started.
ITER      TIME
0         0.00
Dual basis identification phase terminated. Time: 0.00
Basis identification terminated. Time: 0.00
Interior-point optimizer terminated. Time: 0.00.

Optimizer terminated. Time: 0.03
Basic solution summary
Problem status : PRIMAL_AND_DUAL_FEASIBLE
Solution status : OPTIMAL
Primal.  obj: 4.2500000000e+001  Viol.  con: 1e-013  var: 0e+000
Dual.    obj: 4.2500000000e+001  Viol.  con: 0e+000  var: 5e-013
Optimal objective value of the penalty problem: 4.2500000000e+001

Repairing bounds.
Increasing the upper bound -2.25e+001 on constraint 'c4' (3) with 1.35e+002.
Decreasing the lower bound 6.50e+002 on variable 'x2' (4) with 2.00e+001.
Primal feasibility repair terminated.
Optimizer started.
Interior-point optimizer started.
Presolve started.
Presolve terminated. Time: 0.00
Interior-point optimizer terminated. Time: 0.00.

Optimizer terminated. Time: 0.00

Interior-point solution summary
Problem status : PRIMAL_AND_DUAL_FEASIBLE
Solution status : OPTIMAL
Primal.  obj: -5.6700000000e+003  Viol.  con: 0e+000  var: 0e+000
Dual.    obj: -5.6700000000e+003  Viol.  con: 0e+000  var: 0e+000

Basic solution summary
Problem status : PRIMAL_AND_DUAL_FEASIBLE
Solution status : OPTIMAL
Primal.  obj: -5.6700000000e+003  Viol.  con: 0e+000  var: 0e+000
Dual.    obj: -5.6700000000e+003  Viol.  con: 0e+000  var: 0e+000

Optimizer summary
Optimizer          -                time: 0.00
Interior-point    - iterations : 0      time: 0.00
Basis identification -                time: 0.00
Primal           - iterations : 0      time: 0.00
Dual             - iterations : 0      time: 0.00
Clean primal     - iterations : 0      time: 0.00
Clean dual       - iterations : 0      time: 0.00
Clean primal-dual - iterations : 0      time: 0.00
Simplex          -                time: 0.00
Primal simplex   - iterations : 0      time: 0.00
Dual simplex     - iterations : 0      time: 0.00
Primal-dual simplex - iterations : 0      time: 0.00
Mixed integer    - relaxations: 0      time: 0.00

```

reports the optimal repair. In this case it is to increase the upper bound on constraint c4 by 1.35e2 and decrease the lower bound on variable x2 by 20.





## SENSITIVITY ANALYSIS

Given an optimization problem it is often useful to obtain information about how the optimal objective value changes when the problem parameters are perturbed. E.g, assume that a bound represents the capacity of a machine. Now, it may be possible to expand the capacity for a certain cost and hence it is worthwhile knowing what the value of additional capacity is. This is precisely the type of questions the sensitivity analysis deals with.

Analyzing how the optimal objective value changes when the problem data is changed is called *sensitivity analysis*.

### References

The book [Chv83] discusses the classical sensitivity analysis in Chapter 10 whereas the book [RTV97] presents a modern introduction to sensitivity analysis. Finally, it is recommended to read the short paper [Wal00] to avoid some of the pitfalls associated with sensitivity analysis.

**Warning:** Currently, sensitivity analysis is only available for continuous linear optimization problems. Moreover, **MOSEK** can only deal with perturbations of bounds and objective function coefficients.

## 10.1 Sensitivity Analysis for Linear Problems

### 10.1.1 The Optimal Objective Value Function

Assume that we are given the problem

$$\begin{aligned} z(l^c, u^c, l^x, u^x, c) = & \text{minimize} && c^T x \\ & \text{subject to} && l^c \leq Ax \leq u^c, \\ & && l^x \leq x \leq u^x, \end{aligned} \quad (10.1)$$

and we want to know how the optimal objective value changes as  $l_i^c$  is perturbed. To answer this question we define the perturbed problem for  $l_i^c$  as follows

$$\begin{aligned} f_{l_i^c}(\beta) = & \text{minimize} && c^T x \\ & \text{subject to} && l^c + \beta e_i \leq Ax \leq u^c, \\ & && l^x \leq x \leq u^x, \end{aligned}$$

where  $e_i$  is the  $i$ -th column of the identity matrix. The function

$$f_{l_i^c}(\beta) \quad (10.2)$$

shows the optimal objective value as a function of  $\beta$ . Please note that a change in  $\beta$  corresponds to a perturbation in  $l_i^c$  and hence (10.2) shows the optimal objective value as a function of varying  $l_i^c$  with the other bounds fixed.

It is possible to prove that the function (10.2) is a piecewise linear and convex function, i.e. its graph may look like in Fig. 10.1 and Fig. 10.2.

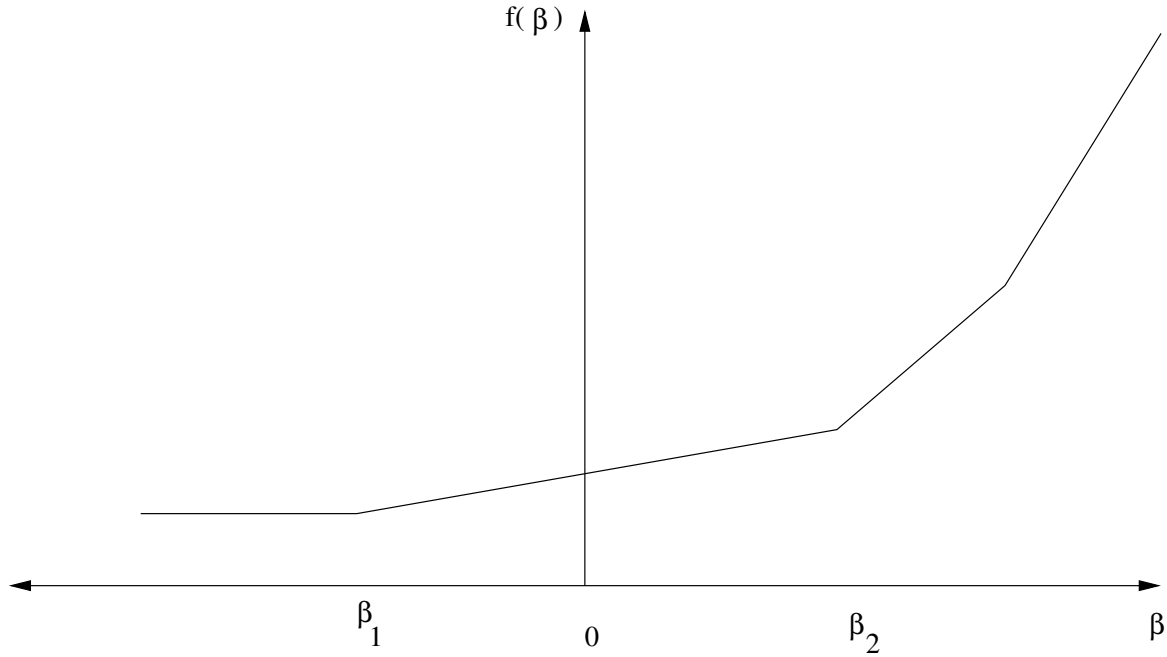


Fig. 10.1:  $\beta = 0$  is in the interior of linearity interval.

Clearly, if the function  $f_{l_i^c}(\beta)$  does not change much when  $\beta$  is changed, then we can conclude that the optimal objective value is insensitive to changes in  $l_i^c$ . Therefore, we are interested in the rate of change in  $f_{l_i^c}(\beta)$  for small changes in  $\beta$  — specifically the gradient

$$f'_{l_i^c}(0),$$

which is called the *shadow price* related to  $l_i^c$ . The shadow price specifies how the objective value changes for small changes of  $\beta$  around zero. Moreover, we are interested in the *linearity interval*

$$\beta \in [\beta_1, \beta_2]$$

for which

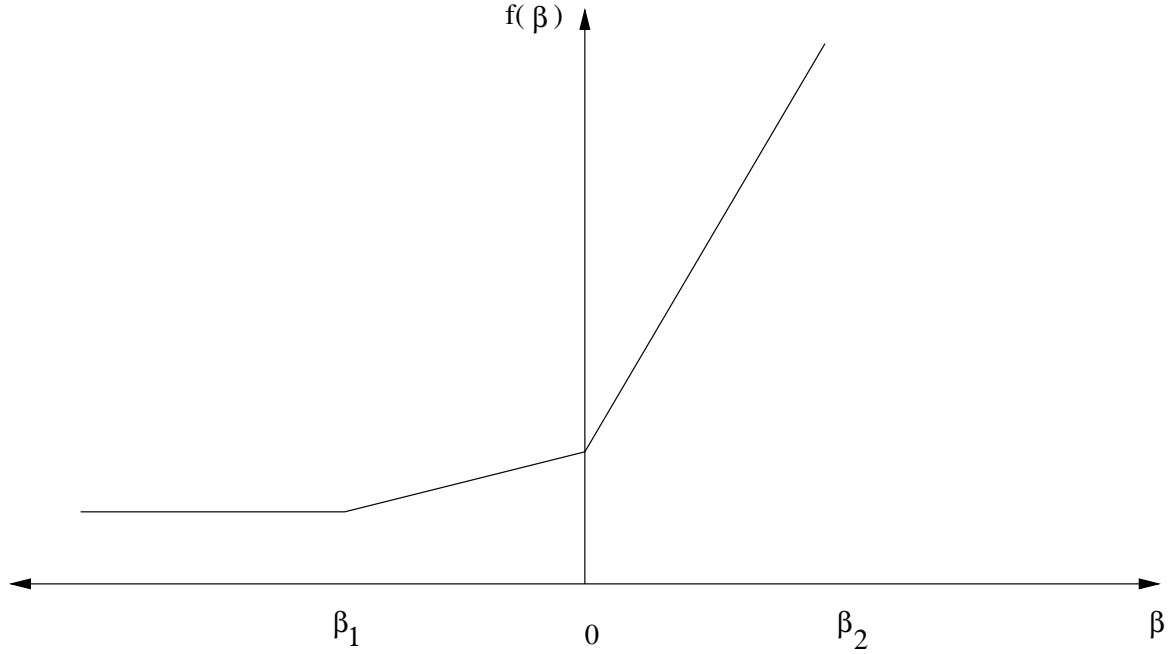
$$f'_{l_i^c}(\beta) = f'_{l_i^c}(0).$$

Since  $f_{l_i^c}$  is not a smooth function  $f'_{l_i^c}$  may not be defined at 0, as illustrated in Fig. 10.2. In this case we can define a left and a right shadow price and a left and a right linearity interval.

The function  $f_{l_i^c}$  considered only changes in  $l_i^c$ . We can define similar functions for the remaining parameters of the  $z$  defined in (10.1) as well:

$$\begin{aligned} f_{l_i^c}(\beta) &= z(l^c + \beta e_i, u^c, l^x, u^x, c), & i = 1, \dots, m, \\ f_{u_i^c}(\beta) &= z(l^c, u^c + \beta e_i, l^x, u^x, c), & i = 1, \dots, m, \\ f_{l_j^x}(\beta) &= z(l^c, u^c, l^x + \beta e_j, u^x, c), & j = 1, \dots, n, \\ f_{u_j^x}(\beta) &= z(l^c, u^c, l^x, u^x + \beta e_j, c), & j = 1, \dots, n, \\ f_{c_j}(\beta) &= z(l^c, u^c, l^x, u^x, c + \beta e_j), & j = 1, \dots, n. \end{aligned}$$

Given these definitions it should be clear how linearity intervals and shadow prices are defined for the parameters  $u_i^c$  etc.

Fig. 10.2:  $\beta = 0$  is a breakpoint.

### Equality Constraints

In **MOSEK** a constraint can be specified as either an equality constraint or a ranged constraint. If some constraint  $e_i^c$  is an equality constraint, we define the optimal value function for this constraint as

$$f_{e_i^c}(\beta) = z(l^c + \beta e_i, u^c + \beta e_i, l^x, u^x, c)$$

Thus for an equality constraint the upper and the lower bounds (which are equal) are perturbed simultaneously. Therefore, **MOSEK** will handle sensitivity analysis differently for a ranged constraint with  $l_i^c = u_i^c$  and for an equality constraint.

#### 10.1.2 The Basis Type Sensitivity Analysis

The classical sensitivity analysis discussed in most textbooks about linear optimization, e.g. [Chv83], is based on an optimal basic solution or, equivalently, on an optimal basis. This method may produce misleading results [RTV97] but is **computationally cheap**. Therefore, and for historical reasons, this method is available in **MOSEK**.

We will now briefly discuss the basis type sensitivity analysis. Given an optimal basic solution which provides a partition of variables into basic and non-basic variables, the basis type sensitivity analysis computes the linearity interval  $[\beta_1, \beta_2]$  so that the basis remains optimal for the perturbed problem. A shadow price associated with the linearity interval is also computed. However, it is well-known that an optimal basic solution may not be unique and therefore the result depends on the optimal basic solution employed in the sensitivity analysis. This implies that the computed interval is only a subset of the largest interval for which the shadow price is constant. Furthermore, the optimal objective value function might have a breakpoint for  $\beta = 0$ . In this case the basis type sensitivity method will only provide a subset of either the left or the right linearity interval.

In summary, the basis type sensitivity analysis is computationally cheap but does not provide complete information. Hence, the results of the basis type sensitivity analysis should be used with care.

### 10.1.3 The Optimal Partition Type Sensitivity Analysis

Another method for computing the complete linearity interval is called the *optimal partition type sensitivity analysis*. The main drawback of the optimal partition type sensitivity analysis is that it is computationally expensive compared to the basis type analysis. This type of sensitivity analysis is currently provided as an experimental feature in **MOSEK**.

Given the optimal primal and dual solutions to (10.1), i.e.  $x^*$  and  $((s_l^c)^*, (s_u^c)^*, (s_l^x)^*, (s_u^x)^*)$  the optimal objective value is given by

$$z^* := c^T x^*.$$

The left and right shadow prices  $\sigma_1$  and  $\sigma_2$  for  $l_i^c$  are given by this pair of optimization problems:

$$\begin{aligned} \sigma_1 = \text{minimize} \quad & e_i^T s_l^c \\ \text{subject to} \quad & A^T(s_l^c - s_u^c) + s_l^x - s_u^x = c, \\ & (l^c)^T(s_l^c) - (u^c)^T(s_u^c) + (l^x)^T(s_l^x) - (u^x)^T(s_u^x) = z^*, \\ & s_l^c, s_u^c, s_l^x, s_u^x \geq 0 \end{aligned}$$

and

$$\begin{aligned} \sigma_2 = \text{maximize} \quad & e_i^T s_l^c \\ \text{subject to} \quad & A^T(s_l^c - s_u^c) + s_l^x - s_u^x = c, \\ & (l^c)^T(s_l^c) - (u^c)^T(s_u^c) + (l^x)^T(s_l^x) - (u^x)^T(s_u^x) = z^*, \\ & s_l^c, s_u^c, s_l^x, s_u^x \geq 0. \end{aligned}$$

These two optimization problems make it easy to interpret the shadow price. Indeed, if  $((s_l^c)^*, (s_u^c)^*, (s_l^x)^*, (s_u^x)^*)$  is an arbitrary optimal solution then

$$(s_l^c)^* \in [\sigma_1, \sigma_2].$$

Next, the linearity interval  $[\beta_1, \beta_2]$  for  $l_i^c$  is computed by solving the two optimization problems

$$\begin{aligned} \beta_1 = \text{minimize} \quad & \beta \\ \text{subject to} \quad & l^c + \beta e_i \leq Ax \leq u^c, \\ & c^T x - \sigma_1 \beta = z^*, \\ & l^x \leq x \leq u^x, \end{aligned}$$

and

$$\begin{aligned} \beta_2 = \text{maximize} \quad & \beta \\ \text{subject to} \quad & l^c + \beta e_i \leq Ax \leq u^c, \\ & c^T x - \sigma_2 \beta = z^*, \\ & l^x \leq x \leq u^x. \end{aligned}$$

The linearity intervals and shadow prices for  $u_i^c$ ,  $l_j^x$ , and  $u_j^x$  are computed similarly to  $l_i^c$ .

The left and right shadow prices for  $c_j$  denoted  $\sigma_1$  and  $\sigma_2$  respectively are computed as follows:

$$\begin{aligned} \sigma_1 = \text{minimize} \quad & e_j^T x \\ \text{subject to} \quad & l^c + \beta e_i \leq Ax \leq u^c, \\ & c^T x = z^*, \\ & l^x \leq x \leq u^x, \end{aligned}$$

and

$$\begin{aligned} \sigma_2 = \text{maximize} \quad & e_j^T x \\ \text{subject to} \quad & l^c + \beta e_i \leq Ax \leq u^c, \\ & c^T x = z^*, \\ & l^x \leq x \leq u^x. \end{aligned}$$

Once again the above two optimization problems make it easy to interpret the shadow prices. Indeed, if  $x^*$  is an arbitrary primal optimal solution, then

$$x_j^* \in [\sigma_1, \sigma_2].$$

The linearity interval  $[\beta_1, \beta_2]$  for a  $c_j$  is computed as follows:

$$\begin{aligned} \beta_1 = & \text{minimize} && \beta \\ & \text{subject to} && A^T(s_l^c - s_u^c) + s_l^x - s_u^x = c + \beta e_j, \\ & && (l^c)^T(s_l^c) - (u^c)^T(s_u^c) + (l^x)^T(s_l^x) - (u^x)^T(s_u^x) - \sigma_1 \beta \leq z^*, \\ & && s_l^c, s_u^c, s_l^x, s_u^x \geq 0 \end{aligned}$$

and

$$\begin{aligned} \beta_2 = & \text{maximize} && \beta \\ & \text{subject to} && A^T(s_l^c - s_u^c) + s_l^x - s_u^x = c + \beta e_j, \\ & && (l^c)^T(s_l^c) - (u^c)^T(s_u^c) + (l^x)^T(s_l^x) - (u^x)^T(s_u^x) - \sigma_2 \beta \leq z^*, \\ & && s_l^c, s_u^c, s_l^x, s_u^x \geq 0. \end{aligned}$$

#### 10.1.4 Example: Sensitivity Analysis

As an example we will use the following transportation problem. Consider the problem of minimizing the transportation cost between a number of production plants and stores. Each plant supplies a number of goods and each store has a given demand that must be met. Supply, demand and cost of transportation per unit are shown in Fig. 10.3.

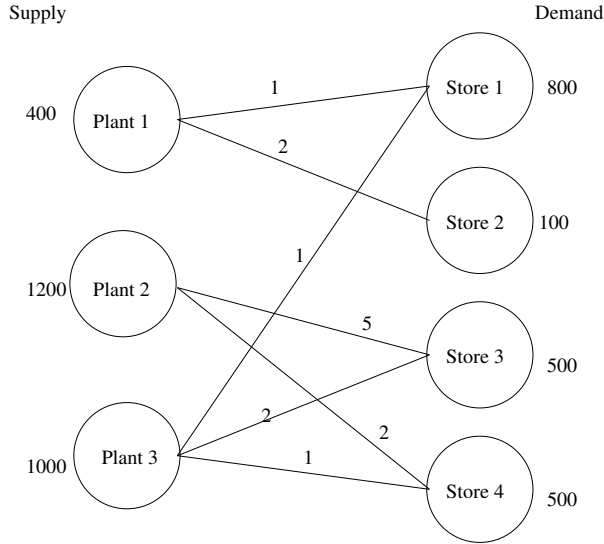


Fig. 10.3: Supply, demand and cost of transportation.

If we denote the number of transported goods from location  $i$  to location  $j$  by  $x_{ij}$ , problem can be formulated as the linear optimization problem of minimizing

$$1x_{11} + 2x_{12} + 5x_{23} + 2x_{24} + 1x_{31} + 2x_{33} + 1x_{34}$$

subject to

$$\begin{aligned} x_{11} + x_{12} & \leq 400, \\ x_{23} + x_{24} & \leq 1200, \\ x_{31} + x_{33} + x_{34} & \leq 1000, \\ x_{11} + x_{31} & = 800, \\ x_{12} + x_{32} & = 100, \\ x_{23} + x_{33} & = 500, \\ x_{24} + x_{34} & = 500, \\ x_{11}, x_{12}, x_{23}, x_{24}, x_{31}, x_{33}, x_{34} & \geq 0. \end{aligned} \tag{10.3}$$

The sensitivity parameters are shown in Table 10.1 and Table 10.2 for the basis type analysis and in Table 10.3 and Table 10.4 for the optimal partition type analysis.

Table 10.1: Ranges and shadow prices related to bounds on constraints and variables: results for the basis type sensitivity analysis.

Con.	$\beta_1$	$\beta_2$	$\sigma_1$	$\sigma_2$
1	-300.00	0.00	3.00	3.00
2	-700.00	$+\infty$	0.00	0.00
3	-500.00	0.00	3.00	3.00
4	-0.00	500.00	4.00	4.00
5	-0.00	300.00	5.00	5.00
6	-0.00	700.00	5.00	5.00
7	-500.00	700.00	2.00	2.00
Var.	$\beta_1$	$\beta_2$	$\sigma_1$	$\sigma_2$
$x_{11}$	$-\infty$	300.00	0.00	0.00
$x_{12}$	$-\infty$	100.00	0.00	0.00
$x_{23}$	$-\infty$	0.00	0.00	0.00
$x_{24}$	$-\infty$	500.00	0.00	0.00
$x_{31}$	$-\infty$	500.00	0.00	0.00
$x_{33}$	$-\infty$	500.00	0.00	0.00
$x_{34}$	-0.000000	500.00	2.00	2.00

Table 10.2: Ranges and shadow prices related to bounds on constraints and variables: results for the optimal partition type sensitivity analysis.

Con.	$\beta_1$	$\beta_2$	$\sigma_1$	$\sigma_2$
1	-300.00	500.00	3.00	1.00
2	-700.00	$+\infty$	-0.00	-0.00
3	-500.00	500.00	3.00	1.00
4	-500.00	500.00	2.00	4.00
5	-100.00	300.00	3.00	5.00
6	-500.00	700.00	3.00	5.00
7	-500.00	700.00	2.00	2.00
Var.	$\beta_1$	$\beta_2$	$\sigma_1$	$\sigma_2$
$x_{11}$	$-\infty$	300.00	0.00	0.00
$x_{12}$	$-\infty$	100.00	0.00	0.00
$x_{23}$	$-\infty$	500.00	0.00	2.00
$x_{24}$	$-\infty$	500.00	0.00	0.00
$x_{31}$	$-\infty$	500.00	0.00	0.00
$x_{33}$	$-\infty$	500.00	0.00	0.00
$x_{34}$	$-\infty$	500.00	0.00	2.00

Table 10.3: Ranges and shadow prices related to the objective coefficients: results for the basis type sensitivity analysis.

Var.	$\beta_1$	$\beta_2$	$\sigma_1$	$\sigma_2$
$c_1$	$-\infty$	3.00	300.00	300.00
$c_2$	$-\infty$	$\infty$	100.00	100.00
$c_3$	-2.00	$\infty$	0.00	0.00
$c_4$	$-\infty$	2.00	500.00	500.00
$c_5$	-3.00	$\infty$	500.00	500.00
$c_6$	$-\infty$	2.00	500.00	500.00
$c_7$	-2.00	$\infty$	0.00	0.00

Table 10.4: Ranges and shadow prices related to the objective coefficients: results for the optimal partition type sensitivity analysis.

Var.	$\beta_1$	$\beta_2$	$\sigma_1$	$\sigma_2$
$c_1$	$-\infty$	3.00	300.00	300.00
$c_2$	$-\infty$	$\infty$	100.00	100.00
$c_3$	-2.00	$\infty$	0.00	0.00
$c_4$	$-\infty$	2.00	500.00	500.00
$c_5$	-3.00	$\infty$	500.00	500.00
$c_6$	$-\infty$	2.00	500.00	500.00
$c_7$	-2.00	$\infty$	0.00	0.00

Examining the results from the optimal partition type sensitivity analysis we see that for constraint number 1 we have  $\sigma_1 = 3$ ,  $\sigma_2 = 1$  and  $\beta_1 = -300$ ,  $\beta_2 = 500$ . Therefore, we have a left linearity interval of  $[-300, 0]$  and a right interval of  $[0, 500]$ . The corresponding left and right shadow prices are 3 and 1 respectively. This implies that if the upper bound on constraint 1 increases by

$$\beta \in [0, \beta_1] = [0, 500]$$

then the optimal objective value will decrease by the value

$$\sigma_2 \beta = 1\beta.$$

Correspondingly, if the upper bound on constraint 1 is decreased by

$$\beta \in [0, 300]$$

then the optimal objective value will increase by the value

$$\sigma_1 \beta = 3\beta.$$

## 10.2 Sensitivity Analysis with MOSEK

A sensitivity analysis can be performed with the **MOSEK** command line tool specifying the option `-sen`, e.g.

```
mosek myproblem.mps -sen sensitivity.ssp
```

where `sensitivity.ssp` is a file in the format described in the next section. The `ssp` file describes which parts of the problem the sensitivity analysis should be performed on, see Section 10.2.1.

By default results are written to a file named `myproblem.sen`. If necessary, this filename can be changed by setting the `MSK_SPAR_SENSITIVITY_RES_FILE_NAME` parameter. By default a basis type sensitivity analysis is performed. However, the type of sensitivity analysis (basis or optimal partition) can be changed by setting the parameter `MSK_IPAR_SENSITIVITY_TYPE` appropriately. Following values are accepted for this parameter:

- `MSK_SENSITIVITY_TYPE_BASIS`
- `MSK_SENSITIVITY_TYPE_OPTIMAL_PARTITION`

### 10.2.1 Sensitivity Analysis Specification File

MOSEK employs an MPS-like file format to specify on which model parameters the sensitivity analysis should be performed. As the optimal partition type sensitivity analysis can be computationally expensive it is important to limit the sensitivity analysis.

The format of the sensitivity specification file is shown in Listing 10.1, where capitalized names are keywords, and names in brackets are names of the constraints and variables to be included in the analysis.

Listing 10.1: Sensitivity analysis file specification.

```
BOUNDS CONSTRAINTS
U|L|LU [cname1]
U|L|LU [cname2] - [cname3]
BOUNDS VARIABLES
U|L|LU [vname1]
U|L|LU [vname2] - [vname3]
OBJECTIVE VARIABLES
[vname1]
[vname2] - [vname3]
```

The sensitivity specification file has three sections, i.e.

- **BOUNDS CONSTRAINTS:** Specifies on which bounds on constraints the sensitivity analysis should be performed.
- **BOUNDS VARIABLES:** Specifies on which bounds on variables the sensitivity analysis should be performed.
- **OBJECTIVE VARIABLES:** Specifies on which objective coefficients the sensitivity analysis should be performed.

A line in the body of a section must begin with a whitespace. In the **BOUNDS** sections one of the keys L, U, and LU must appear next. These keys specify whether the sensitivity analysis is performed on the lower bound, on the upper bound, or on both the lower and the upper bound respectively. Next, a single constraint (variable) or range of constraints (variables) is specified.

Recall from Section 10.1.1.1 that equality constraints are handled in a special way. Sensitivity analysis of an equality constraint can be specified with either L, U, or LU, all indicating the same, namely that upper and lower bounds (which are equal) are perturbed simultaneously.

As an example consider

```
BOUNDS CONSTRAINTS
L "cons1"
U "cons2"
LU "cons3" - "cons6"
```



which requests that sensitivity analysis is performed on the lower bound of the constraint named `cons1`, on the upper bound of the constraint named `cons2`, and on both lower and upper bound on the constraints named `cons3` to `cons6`.

It is allowed to use indexes instead of names, for instance

```
BOUNDS CONSTRAINTS
L "cons1"
U 2
LU 3 - 6
```

The character `*` indicates that the line contains a comment and is ignored.

## 10.2.2 Example: Sensitivity Analysis from Command Line

As an example consider problem (10.3): the sensitivity file shown below (included in the distribution among the examples).

Listing 10.2: Sensitivity file for problem (10.3).

```
* Comment 1

BOUNDS CONSTRAINTS
U "c1"          * Analyze upper bound for constraints named c1
U 2             * Analyze upper bound for constraints with index 2
U 3-5          * Analyze upper bound for constraint with index in interval [3:5]

VARIABLES CONSTRAINTS
L 2-4           * This section specifies which bounds on variables should be analyzed.
L "x11"

OBJECTIVE CONSTRAINTS
"x11"          * This section specifies which objective coefficients should be analysed.
2
```

The command

```
mosek transport.lp -sen sensitivity.ssp -d MSK_IPAR_SENSITIVITY_TYPE sensitivitytype.basis
```

produces the output file as follow

```
BOUNDS CONSTRAINTS
INDEX  NAME          BOUND  LEFTRANGE  RIGHTRANGE  LEFTPRICE  RIGHTPRICE
0      c1            UP      -6.574875e-18  5.000000e+02  1.000000e+00  1.
2      c3            UP      -6.574875e-18  5.000000e+02  1.000000e+00  1.
3      c4            FIX      -5.000000e+02  6.574875e-18  2.000000e+00  2.
4      c5            FIX      -1.000000e+02  6.574875e-18  3.000000e+00  3.
5      c6            FIX      -5.000000e+02  6.574875e-18  3.000000e+00  3.

BOUNDS VARIABLES
INDEX  NAME          BOUND  LEFTRANGE  RIGHTRANGE  LEFTPRICE  RIGHTPRICE
2      x23          L0      -6.574875e-18  5.000000e+02  2.000000e+00  2.
3      x24          L0      -inf        5.000000e+02  0.000000e+00  0.
4      x31          L0      -inf        5.000000e+02  0.000000e+00  0.
```

0	x11	L0	-inf	3.000000e+02	0.000000e+00	0.
↪000000e+00						
OBJECTIVE VARIABLES						
INDEX	NAME	LEFTRANGE	RIGHTRANGE	LEFTPRICE	└	
↪RIGHTPRICE						
0	x11	-inf	1.000000e+00	3.000000e+02	3.	
↪000000e+02						
2	x23	-2.000000e+00	+inf	0.000000e+00	0.	
↪000000e+00						

### 10.2.3 Controlling Log Output

Setting the parameter *MSK\_IPAR\_LOG\_SENSITIVITY* to 1 or 0 (default) controls whether or not the results from sensitivity calculations are printed to the message stream.

The parameter *MSK\_IPAR\_LOG\_SENSITIVITY\_OPT* controls the amount of debug information on internal calculations from the sensitivity analysis.

## API REFERENCE

### 11.1 Parameters

*All parameters (alphabetical order)*

- *double parameters*
- *integer parameters*
- *string parameters*

#### Parameters grouped by topic

Note: some parameters may appear in more than one group.

- *Infeasibility report*
- *Logging*
- *Data input/output*
- *Presolve*
- *Interior-point method*
- *Overall solver*
- *Termination criterion*
- *Conic interior-point method*
- *Nonlinear convex method*
- *Optimization system*
- *Basis identification*
- *Analysis*
- *Data check*
- *Primal simplex optimizer*
- *Progress call-back*
- *License manager*
- *Debugging*
- *Dual simplex optimizer*
- *Mixed-integer optimization*
- *Simplex optimizer*
- *Output information*

- *Solution input/output*

### 11.1.1 Parameters List (alphabetically)

#### Double Parameters

##### MSK\_DPAR\_ANA\_SOL\_INFEAS\_TOL

If a constraint violates its bound with an amount larger than this value, the constraint name, index and violation will be printed by the solution analyzer.

Accepted Values: [0.0 ;+inf ]

Default Value: 1e-6

Groups: *Analysis*

##### MSK\_DPAR\_BASIS\_REL\_TOL\_S

Maximum relative dual bound violation allowed in an optimal basic solution.

Accepted Values: [0.0 ;+inf ]

Default Value: 1.0e-12

Groups: *Simplex optimizer, Termination criterion*

##### MSK\_DPAR\_BASIS\_TOL\_S

Maximum absolute dual bound violation in an optimal basic solution.

Accepted Values: [1.0e-9 ;+inf ]

Default Value: 1.0e-6

Groups: *Simplex optimizer, Termination criterion*

##### MSK\_DPAR\_BASIS\_TOL\_X

Maximum absolute primal bound violation allowed in an optimal basic solution.

Accepted Values: [1.0e-9 ;+inf ]

Default Value: 1.0e-6

Groups: *Simplex optimizer, Termination criterion*

##### MSK\_DPAR\_CHECK\_CONVEXITY\_REL\_TOL

This parameter controls when the full convexity check declares a problem to be non-convex. Increasing this tolerance relaxes the criteria for declaring the problem non-convex.

A problem is declared non-convex if negative (positive) pivot elements are detected in the Cholesky factor of a matrix which is required to be PSD (NSD). This parameter controls how much this non-negativity requirement may be violated.

If  $d_i$  is the pivot element for column  $i$ , then the matrix  $Q$  is considered to not be PSD if:

$$d_i \leq -|Q_{ii}| \text{check\_convexity\_rel\_tol}$$

Accepted Values: [0 ;+inf ]

Default Value: 1e-10

Groups: *Interior-point method*

##### MSK\_DPAR\_DATA\_SYM\_MAT\_TOL

Absolute zero tolerance for elements in in suymmetric matrixes. If any value in a symmetric matrix is smaller than this parameter in absolute terms **MOSEK** will treat the values as zero and generate a warning.

Accepted Values: [1.0e-16 ;1.0e-6 ]

Default Value: 1.0e-12

Groups: *Data check*

#### MSK\_DPAR\_DATA\_SYM\_MAT\_TOL\_HUGE

An element in a symmetric matrix which is larger than this value in absolute size causes an error.

Accepted Values: [0.0 ;+inf ]

Default Value: 1.0e20

Groups: *Data check*

#### MSK\_DPAR\_DATA\_SYM\_MAT\_TOL\_LARGE

An element in a symmetric matrix which is larger than this value in absolute size causes a warning message to be printed.

Accepted Values: [0.0 ;+inf ]

Default Value: 1.0e10

Groups: *Data check*

#### MSK\_DPAR\_DATA\_TOL\_AIJ

Absolute zero tolerance for elements in  $A$ . If any value  $A_{ij}$  is smaller than this parameter in absolute terms **MOSEK** will treat the values as zero and generate a warning.

Accepted Values: [1.0e-16 ;1.0e-6 ]

Default Value: 1.0e-12

Groups: *Data check*

#### MSK\_DPAR\_DATA\_TOL\_AIJ\_HUGE

An element in  $A$  which is larger than this value in absolute size causes an error.

Accepted Values: [0.0 ;+inf ]

Default Value: 1.0e20

Groups: *Data check*

#### MSK\_DPAR\_DATA\_TOL\_AIJ\_LARGE

An element in  $A$  which is larger than this value in absolute size causes a warning message to be printed.

Accepted Values: [0.0 ;+inf ]

Default Value: 1.0e10

Groups: *Data check*

#### MSK\_DPAR\_DATA\_TOL\_BOUND\_INF

Any bound which in absolute value is greater than this parameter is considered infinite.

Accepted Values: [0.0 ;+inf ]

Default Value: 1.0e16

Groups: *Data check*

#### MSK\_DPAR\_DATA\_TOL\_BOUND\_WRN

If a bound value is larger than this value in absolute size, then a warning message is issued.

Accepted Values: [0.0 ;+inf ]

Default Value: 1.0e8

Groups: *Data check*

#### MSK\_DPAR\_DATA\_TOL\_CJ\_LARGE

An element in  $c$  which is larger than this value in absolute terms causes a warning message to be printed.

Accepted Values: [0.0 ;+inf ]

Default Value: 1.0e8

Groups: *Data check*

#### MSK\_DPAR\_DATA\_TOL\_C\_HUGE

An element in  $c$  which is larger than the value of this parameter in absolute terms is considered to be huge and generates an error.

Accepted Values:  $[0.0 ; +\infty]$

Default Value: 1.0e16

Groups: *Data check*

#### MSK\_DPAR\_DATA\_TOL\_QIJ

Absolute zero tolerance for elements in  $Q$  matrices.

Accepted Values:  $[0.0 ; +\infty]$

Default Value: 1.0e-16

Groups: *Data check*

#### MSK\_DPAR\_DATA\_TOL\_X

Zero tolerance for constraints and variables i.e. if the distance between the lower and upper bound is less than this value, then the lower and upper bound is considered identical.

Accepted Values:  $[0.0 ; +\infty]$

Default Value: 1.0e-8

Groups: *Data check*

#### MSK\_DPAR\_INTPNT\_CO\_TOL\_DFEAS

Dual feasibility tolerance used by the conic interior-point optimizer.

Accepted Values:  $[0.0 ; 1.0]$

Default Value: 1.0e-8

Groups: *Interior-point method, Termination criterion, Conic interior-point method*

#### MSK\_DPAR\_INTPNT\_CO\_TOL\_INFEAS

Controls when the conic interior-point optimizer declares the model primal or dual infeasible. A small number means the optimizer gets more conservative about declaring the model infeasible.

Accepted Values:  $[0.0 ; 1.0]$

Default Value: 1.0e-10

Groups: *Interior-point method, Termination criterion, Conic interior-point method*

#### MSK\_DPAR\_INTPNT\_CO\_TOL\_MU\_RED

Relative complementarity gap feasibility tolerance used by the conic interior-point optimizer.

Accepted Values:  $[0.0 ; 1.0]$

Default Value: 1.0e-8

Groups: *Interior-point method, Termination criterion, Conic interior-point method*

#### MSK\_DPAR\_INTPNT\_CO\_TOL\_NEAR\_REL

If **MOSEK** cannot compute a solution that has the prescribed accuracy, then it will multiply the termination tolerances with value of this parameter. If the solution then satisfies the termination criteria, then the solution is denoted near optimal, near feasible and so forth.

Accepted Values:  $[1.0 ; +\infty]$

Default Value: 1000

Groups: *Interior-point method, Termination criterion, Conic interior-point method*

**MSK\_DPAR\_INTPNT\_CO\_TOL\_PFEAS**

Primal feasibility tolerance used by the conic interior-point optimizer.

Accepted Values: [0.0 ;1.0 ]

Default Value: 1.0e-8

Groups: *Interior-point method, Termination criterion, Conic interior-point method*

**MSK\_DPAR\_INTPNT\_CO\_TOL\_REL\_GAP**

Relative gap termination tolerance used by the conic interior-point optimizer.

Accepted Values: [0.0 ;1.0 ]

Default Value: 1.0e-7

Groups: *Interior-point method, Termination criterion, Conic interior-point method*

**MSK\_DPAR\_INTPNT\_NL\_MERIT\_BAL**

Controls if the complementarity and infeasibility is converging to zero at about equal rates.

Accepted Values: [0.0 ;0.99 ]

Default Value: 1.0e-4

Groups: *Interior-point method, Nonlinear convex method*

**MSK\_DPAR\_INTPNT\_NL\_TOL\_DFEAS**

Dual feasibility tolerance used when a nonlinear model is solved.

Accepted Values: [0.0 ;1.0 ]

Default Value: 1.0e-8

Groups: *Interior-point method, Termination criterion, Nonlinear convex method*

**MSK\_DPAR\_INTPNT\_NL\_TOL\_MU\_RED**

Relative complementarity gap tolerance.

Accepted Values: [0.0 ;1.0 ]

Default Value: 1.0e-12

Groups: *Interior-point method, Termination criterion, Nonlinear convex method*

**MSK\_DPAR\_INTPNT\_NL\_TOL\_NEAR\_REL**

If the **MOSEK** nonlinear interior-point optimizer cannot compute a solution that has the prescribed accuracy, then it will multiply the termination tolerances with value of this parameter. If the solution then satisfies the termination criteria, then the solution is denoted near optimal, near feasible and so forth.

Accepted Values: [1.0 ;+inf ]

Default Value: 1000.0

Groups: *Interior-point method, Termination criterion, Nonlinear convex method*

**MSK\_DPAR\_INTPNT\_NL\_TOL\_PFEAS**

Primal feasibility tolerance used when a nonlinear model is solved.

Accepted Values: [0.0 ;1.0 ]

Default Value: 1.0e-8

Groups: *Interior-point method, Termination criterion, Nonlinear convex method*

**MSK\_DPAR\_INTPNT\_NL\_TOL\_REL\_GAP**

Relative gap termination tolerance for nonlinear problems.

Accepted Values: [1.0e-14 ;+inf ]

Default Value: 1.0e-6

Groups: *Termination criterion, Interior-point method, Nonlinear convex method*

**MSK\_DPAR\_INTPNT\_NL\_TOL\_REL\_STEP**

Relative step size to the boundary for general nonlinear optimization problems.

Accepted Values: [1.0e-4 ;0.9999999 ]

Default Value: 0.995

Groups: *Interior-point method, Nonlinear convex method*

**MSK\_DPAR\_INTPNT\_QO\_TOL\_DFEAS**

Dual feasibility tolerance used when the interior-point optimizer is applied to a quadratic optimization problem..

Accepted Values: [0.0 ;1.0 ]

Default Value: 1.0e-8

Groups: *Interior-point method, Termination criterion*

**MSK\_DPAR\_INTPNT\_QO\_TOL\_INFEAS**

Controls when the conic interior-point optimizer declares the model primal or dual infeasible. A small number means the optimizer gets more conservative about declaring the model infeasible.

Accepted Values: [0.0 ;1.0 ]

Default Value: 1.0e-10

Groups: *Interior-point method, Termination criterion*

**MSK\_DPAR\_INTPNT\_QO\_TOL\_MU\_RED**

Relative complementarity gap feasibility tolerance used when interior-point optimizer is applied to a quadratic optimization problem.

Accepted Values: [0.0 ;1.0 ]

Default Value: 1.0e-8

Groups: *Interior-point method, Termination criterion*

**MSK\_DPAR\_INTPNT\_QO\_TOL\_NEAR\_REL**

If **MOSEK** cannot compute a solution that has the prescribed accuracy, then it will multiply the termination tolerances with value of this parameter. If the solution then satisfies the termination criteria, then the solution is denoted near optimal, near feasible and so forth.

Accepted Values: [1.0 ;+inf ]

Default Value: 1000

Groups: *Interior-point method, Termination criterion*

**MSK\_DPAR\_INTPNT\_QO\_TOL\_PFEAS**

Primal feasibility tolerance used when the interior-point optimizer is applied to a quadratic optimization problem.

Accepted Values: [0.0 ;1.0 ]

Default Value: 1.0e-8

Groups: *Interior-point method, Termination criterion*

**MSK\_DPAR\_INTPNT\_QO\_TOL\_REL\_GAP**

Relative gap termination tolerance used when the interior-point optimizer is applied to a quadratic optimization problem.

Accepted Values: [0.0 ;1.0 ]

Default Value: 1.0e-8

Groups: *Interior-point method, Termination criterion*



**MSK\_DPAR\_INTPNT\_TOL\_DFEAS**

Dual feasibility tolerance used for linear and quadratic optimization problems.

Accepted Values: [0.0 ;1.0 ]

Default Value: 1.0e-8

Groups: *Interior-point method, Termination criterion*

**MSK\_DPAR\_INTPNT\_TOL\_DSAFE**

Controls the initial dual starting point used by the interior-point optimizer. If the interior-point optimizer converges slowly and/or the constraint or variable bounds are very large, then it might be worthwhile to increase this value.

Accepted Values: [1.0e-4 ;+inf ]

Default Value: 1.0

Groups: *Interior-point method*

**MSK\_DPAR\_INTPNT\_TOL\_INFEAS**

Controls when the optimizer declares the model primal or dual infeasible. A small number means the optimizer gets more conservative about declaring the model infeasible. A value of 0.0 means the optimizer must have an exact certificate of infeasibility and this is very unlikely to happen.

Accepted Values: [0.0 ;1.0 ]

Default Value: 1.0e-10

Groups: *Interior-point method, Termination criterion, Nonlinear convex method*

**MSK\_DPAR\_INTPNT\_TOL\_MU\_RED**

Relative complementarity gap tolerance.

Accepted Values: [0.0 ;1.0 ]

Default Value: 1.0e-16

Groups: *Interior-point method, Termination criterion*

**MSK\_DPAR\_INTPNT\_TOL\_PATH**

Controls how close the interior-point optimizer follows the central path. A large value of this parameter means the central is followed very closely. On numerical unstable problems it may be worthwhile to increase this parameter.

Accepted Values: [0.0 ;0.9999 ]

Default Value: 1.0e-8

Groups: *Interior-point method*

**MSK\_DPAR\_INTPNT\_TOL\_PFEAS**

Primal feasibility tolerance used for linear and quadratic optimization problems.

Accepted Values: [0.0 ;1.0 ]

Default Value: 1.0e-8

Groups: *Interior-point method, Termination criterion*

**MSK\_DPAR\_INTPNT\_TOL\_PSAFE**

Controls the initial primal starting point used by the interior-point optimizer. If the interior-point optimizer converges slowly and/or the constraint or variable bounds are very large, then it may be worthwhile to increase this value.

Accepted Values: [1.0e-4 ;+inf ]

Default Value: 1.0

Groups: *Interior-point method*

**MSK\_DPAR\_INTPNT\_TOL\_REL\_GAP**

Relative gap termination tolerance.

Accepted Values: [1.0e-14 ;+inf ]

Default Value: 1.0e-8

Groups: *Termination criterion, Interior-point method*

**MSK\_DPAR\_INTPNT\_TOL\_REL\_STEP**

Relative step size to the boundary for linear and quadratic optimization problems.

Accepted Values: [1.0e-4 ;0.999999 ]

Default Value: 0.9999

Groups: *Interior-point method*

**MSK\_DPAR\_INTPNT\_TOL\_STEP\_SIZE**

If the step size falls below the value of this parameter, then the interior-point optimizer assumes that it is stalled. In other words the interior-point optimizer does not make any progress and therefore it is better stop.

Accepted Values: [0.0 ;1.0 ]

Default Value: 1.0e-6

Groups: *Interior-point method*

**MSK\_DPAR\_LOWER\_OBJ\_CUT**

If either a primal or dual feasible solution is found proving that the optimal objective value is outside, the interval [ *MSK\_DPAR\_LOWER\_OBJ\_CUT*, *MSK\_DPAR\_UPPER\_OBJ\_CUT* ], then **MOSEK** is terminated.

Accepted Values: [-inf ;+inf ]

Default Value: -1.0e30

Groups: *Termination criterion*

**MSK\_DPAR\_LOWER\_OBJ\_CUT\_FINITE\_TRH**

If the lower objective cut is less than the value of this parameter value, then the lower objective cut i.e. *MSK\_DPAR\_LOWER\_OBJ\_CUT* is treated as  $-\infty$ .

Accepted Values: [-inf ;+inf ]

Default Value: -0.5e30

Groups: *Termination criterion*

**MSK\_DPAR\_MIO\_DISABLE\_TERM\_TIME**

This parameter specifies the number of seconds  $n$  during which the termination criteria governed by

- *MSK\_IPAR\_MIO\_MAX\_NUM\_RELAXS*
- *MSK\_IPAR\_MIO\_MAX\_NUM\_BRANCHES*
- *MSK\_DPAR\_MIO\_NEAR\_TOL\_ABS\_GAP*
- *MSK\_DPAR\_MIO\_NEAR\_TOL\_REL\_GAP*

is disabled since the beginning of the optimization.

A negative value is identical to infinity i.e. the termination criteria are never checked.

Accepted Values: [-inf ;+inf ]

Default Value: -1.0

Groups: *Mixed-integer optimization, Termination criterion*

**MSK\_DPAR\_MIO\_MAX\_TIME**

This parameter limits the maximum time spent by the mixed-integer optimizer. A negative number means infinity.

Accepted Values:  $[-\text{inf}; +\text{inf}]$

Default Value: -1.0

Groups: *Mixed-integer optimization, Termination criterion*

**MSK\_DPAR\_MIO\_NEAR\_TOL\_ABS\_GAP**

Relaxed absolute optimality tolerance employed by the mixed-integer optimizer. This termination criteria is delayed. See [MSK\\_DPAR\\_MIO\\_DISABLE\\_TERM\\_TIME](#) for details.

Accepted Values:  $[0.0; +\text{inf}]$

Default Value: 0.0

Groups: *Mixed-integer optimization*

**MSK\_DPAR\_MIO\_NEAR\_TOL\_REL\_GAP**

The mixed-integer optimizer is terminated when this tolerance is satisfied. This termination criteria is delayed. See [MSK\\_DPAR\\_MIO\\_DISABLE\\_TERM\\_TIME](#) for details.

Accepted Values:  $[0.0; +\text{inf}]$

Default Value: 1.0e-3

Groups: *Mixed-integer optimization, Termination criterion*

**MSK\_DPAR\_MIO\_REL\_GAP\_CONST**

This value is used to compute the relative gap for the solution to an integer optimization problem.

Accepted Values:  $[1.0\text{e-}15; +\text{inf}]$

Default Value: 1.0e-10

Groups: *Mixed-integer optimization, Termination criterion*

**MSK\_DPAR\_MIO\_TOL\_ABS\_GAP**

Absolute optimality tolerance employed by the mixed-integer optimizer.

Accepted Values:  $[0.0; +\text{inf}]$

Default Value: 0.0

Groups: *Mixed-integer optimization*

**MSK\_DPAR\_MIO\_TOL\_ABS\_RELAX\_INT**

Absolute relaxation tolerance of the integer constraints. I.e.  $\min(|x| - \lfloor x \rfloor, \lceil x \rceil - |x|)$  is less than the tolerance then the integer restrictions assumed to be satisfied.

Accepted Values:  $[1\text{e-}9; +\text{inf}]$

Default Value: 1.0e-5

Groups: *Mixed-integer optimization*

**MSK\_DPAR\_MIO\_TOL\_FEAS**

Feasibility tolerance for mixed integer solver.

Accepted Values:  $[1\text{e-}9; 1\text{e-}3]$

Default Value: 1.0e-6

Groups: *Mixed-integer optimization*

**MSK\_DPAR\_MIO\_TOL\_REL\_DUAL\_BOUND\_IMPROVEMENT**

If the relative improvement of the dual bound is smaller than this value, the solver will terminate the root cut generation. A value of 0.0 means that the value is selected automatically.

Accepted Values:  $[0.0; 1.0]$

Default Value: 0.0

Groups: *Mixed-integer optimization*

#### MSK\_DPAR\_MIO\_TOL\_REL\_GAP

Relative optimality tolerance employed by the mixed-integer optimizer.

Accepted Values: [0.0 ;+inf ]

Default Value: 1.0e-4

Groups: *Mixed-integer optimization, Termination criterion*

#### MSK\_DPAR\_OPTIMIZER\_MAX\_TIME

Maximum amount of time the optimizer is allowed to spent on the optimization. A negative number means infinity.

Accepted Values: [-inf ;+inf ]

Default Value: -1.0

Groups: *Termination criterion*

#### MSK\_DPAR\_PREOLVE\_TOL\_ABS\_LINDEP

Absolute tolerance employed by the linear dependency checker.

Accepted Values: [0.0 ;+inf ]

Default Value: 1.0e-6

Groups: *Presolve*

#### MSK\_DPAR\_PREOLVE\_TOL\_AIJ

Absolute zero tolerance employed for  $a_{ij}$  in the presolve.

Accepted Values: [1.0e-15 ;+inf ]

Default Value: 1.0e-12

Groups: *Presolve*

#### MSK\_DPAR\_PREOLVE\_TOL\_REL\_LINDEP

Relative tolerance employed by the linear dependency checker.

Accepted Values: [0.0 ;+inf ]

Default Value: 1.0e-10

Groups: *Presolve*

#### MSK\_DPAR\_PREOLVE\_TOL\_S

Absolute zero tolerance employed for  $s_i$  in the presolve.

Accepted Values: [0.0 ;+inf ]

Default Value: 1.0e-8

Groups: *Presolve*

#### MSK\_DPAR\_PREOLVE\_TOL\_X

Absolute zero tolerance employed for  $x_j$  in the presolve.

Accepted Values: [0.0 ;+inf ]

Default Value: 1.0e-8

Groups: *Presolve*

#### MSK\_DPAR\_QCQO\_REFORMULATE\_REL\_DROP\_TOL

This parameter determines when columns are dropped in incomplete Cholesky factorization during reformulation of quadratic problems.

Accepted Values: [0 ;+inf ]

Default Value: 1e-15

Groups: *Interior-point method*

#### MSK\_DPAR\_SEMIDEFINITE\_TOL\_APPROX

Tolerance to define a matrix to be positive semidefinite.

Accepted Values: [1.0e-15 ;+inf ]

Default Value: 1.0e-10

Groups: *Data check*

#### MSK\_DPAR\_SIMPLEX\_ABS\_TOL\_PIV

Absolute pivot tolerance employed by the simplex optimizers.

Accepted Values: [1.0e-12 ;+inf ]

Default Value: 1.0e-7

Groups: *Simplex optimizer*

#### MSK\_DPAR\_SIM\_LU\_TOL\_REL\_PIV

Relative pivot tolerance employed when computing the LU factorization of the basis in the simplex optimizers and in the basis identification procedure.

A value closer to 1.0 generally improves numerical stability but typically also implies an increase in the computational work.

Accepted Values: [1.0e-6 ;0.999999 ]

Default Value: 0.01

Groups: *Basis identification, Simplex optimizer*

#### MSK\_DPAR\_UPPER\_OBJ\_CUT

If either a primal or dual feasible solution is found proving that the optimal objective value is outside, the interval [ *MSK\_DPAR\_LOWER\_OBJ\_CUT*, *MSK\_DPAR\_UPPER\_OBJ\_CUT* ], then **MOSEK** is terminated.

Accepted Values: [-inf ;+inf ]

Default Value: 1.0e30

Groups: *Termination criterion*

#### MSK\_DPAR\_UPPER\_OBJ\_CUT\_FINITE\_TRH

If the upper objective cut is greater than the value of this parameter, then the upper objective cut *MSK\_DPAR\_UPPER\_OBJ\_CUT* is treated as  $\infty$ .

Accepted Values: [-inf ;+inf ]

Default Value: 0.5e30

Groups: *Termination criterion*

### Integer Parameters

#### MSK\_IPAR\_ANA\_SOL\_BASIS

Controls whether the basis matrix is analyzed in solution analyzer.

Accepted Values: *MSKonoffkeye*

Default Value: *MSK\_ON*

Groups: *Analysis*

#### MSK\_IPAR\_ANA\_SOL\_PRINT\_VIOLATED

Controls whether a list of violated constraints is printed.

All constraints violated by more than the value set by the parameter *MSK\_DPAR\_ANA\_SOL\_INFEAS\_TOL* will be printed.

Accepted Values: *MSK\_onoffkeye*

Default Value: *MSK\_OFF*

Groups: *Analysis*

#### MSK\_IPAR\_AUTO\_SORT\_A\_BEFORE\_OPT

Controls whether the elements in each column of *A* are sorted before an optimization is performed. This is not required but makes the optimization more deterministic.

Accepted Values: *MSK\_onoffkeye*

Default Value: *MSK\_OFF*

Groups: *Debugging*

#### MSK\_IPAR\_AUTO\_UPDATE\_SOL\_INFO

Controls whether the solution information items are automatically updated after an optimization is performed.

Accepted Values: *MSK\_onoffkeye*

Default Value: *MSK\_OFF*

Groups: *Optimization system*

#### MSK\_IPAR\_BASIS\_SOLVE\_USE\_PLUS\_ONE

If a slack variable is in the basis, then the corresponding column in the basis is a unit vector with -1 in the right position. However, if this parameter is set to *MSK\_ON*, -1 is replaced by 1.

Accepted Values: *MSK\_onoffkeye*

Default Value: *MSK\_OFF*

Groups: *Simplex optimizer*

#### MSK\_IPAR\_BI\_CLEAN\_OPTIMIZER

Controls which simplex optimizer is used in the clean-up phase.

Accepted Values: *MSK\_optimizertypee*

Default Value: *MSK\_OPTIMIZER\_FREE*

Groups: *Basis identification, Overall solver*

#### MSK\_IPAR\_BI\_IGNORE\_MAX\_ITER

If the parameter *MSK\_IPAR\_INTPNT\_BASIS* has the value *MSK\_BI\_NO\_ERROR* and the interior-point optimizer has terminated due to maximum number of iterations, then basis identification is performed if this parameter has the value *MSK\_ON*.

Accepted Values: *MSK\_onoffkeye*

Default Value: *MSK\_OFF*

Groups: *Interior-point method, Basis identification*

#### MSK\_IPAR\_BI\_IGNORE\_NUM\_ERROR

If the parameter *MSK\_IPAR\_INTPNT\_BASIS* has the value *MSK\_BI\_NO\_ERROR* and the interior-point optimizer has terminated due to a numerical problem, then basis identification is performed if this parameter has the value *MSK\_ON*.

Accepted Values: *MSK\_onoffkeye*

Default Value: *MSK\_OFF*

Groups: *Interior-point method, Basis identification*

**MSK\_IPAR\_BI\_MAX\_ITERATIONS**

Controls the maximum number of simplex iterations allowed to optimize a basis after the basis identification.

Accepted Values: [0 ;+inf ]

Default Value: 1000000

Groups: *Basis identification, Termination criterion*

**MSK\_IPAR\_CACHE\_LICENSE**

Specifies if the license is kept checked out for the lifetime of the mosek environment (*MSK\_ON*) or returned to the server immediately after the optimization (*MSK\_OFF*).

By default the license is checked out for the lifetime of the **MOSEK** environment by the first call to the optimizer.

Check-in and check-out of licenses have an overhead. Frequent communication with the license server should be avoided.

Accepted Values: *MSKonoffkeye*

Default Value: *MSK\_ON*

Groups: *License manager*

**MSK\_IPAR\_CHECK\_CONVEXITY**

Specify the level of convexity check on quadratic problems

Accepted Values: *MSKcheckconvexitytypee*

Default Value: *MSK\_CHECK\_CONVEXITY\_FULL*

Groups: *Data check, Nonlinear convex method*

**MSK\_IPAR\_COMPRESS\_STATFILE**

Control compression of stat files.

Accepted Values: *MSKonoffkeye*

Default Value: *MSK\_ON*

**MSK\_IPAR\_INFEAS\_GENERIC\_NAMES**

Controls whether generic names are used when an infeasible subproblem is created.

Accepted Values: *MSKonoffkeye*

Default Value: *MSK\_OFF*

Groups: *Infeasibility report*

**MSK\_IPAR\_INFEAS\_PREFER\_PRIMAL**

If both certificates of primal and dual infeasibility are supplied then only the primal is used when this option is turned on.

Accepted Values: *MSKonoffkeye*

Default Value: *MSK\_ON*

Groups: *Overall solver*

**MSK\_IPAR\_INFEAS\_REPORT\_AUTO**

Controls whether an infeasibility report is automatically produced after the optimization if the problem is primal or dual infeasible.

Accepted Values: *MSKonoffkeye*

Default Value: *MSK\_OFF*

Groups: *Data input/output, Solution input/output*

**MSK\_IPAR\_INFEAS\_REPORT\_LEVEL**

Controls the amount of information presented in an infeasibility report. Higher values imply more information.

Accepted Values: [0 ;+inf ]

Default Value: 1

Groups: *Infeasibility report, Output information*

**MSK\_IPAR\_INTPNT\_BASIS**

Controls whether the interior-point optimizer also computes an optimal basis.

Accepted Values: *MSKbasindtypee*

Default Value: *MSK\_BI\_ALWAYS*

Groups: *Interior-point method, Basis identification*

**MSK\_IPAR\_INTPNT\_DIFF\_STEP**

Controls whether different step sizes are allowed in the primal and dual space.

Accepted Values: *MSKonoffkeye*

Default Value: *MSK\_ON*

Groups: *Interior-point method*

**MSK\_IPAR\_INTPNT\_HOTSTART**

Currently not in use.

Accepted Values: *MSKintpnthotstarte*

Default Value: *MSK\_INTPNT\_HOTSTART\_NONE*

Groups: *Interior-point method*

**MSK\_IPAR\_INTPNT\_MAX\_ITERATIONS**

Controls the maximum number of iterations allowed in the interior-point optimizer.

Accepted Values: [0 ;+inf ]

Default Value: 400

Groups: *Interior-point method, Termination criterion*

**MSK\_IPAR\_INTPNT\_MAX\_NUM\_COR**

Controls the maximum number of correctors allowed by the multiple corrector procedure. A negative value means that **MOSEK** is making the choice.

Accepted Values: [-1 ;+inf ]

Default Value: -1

Groups: *Interior-point method*

**MSK\_IPAR\_INTPNT\_MAX\_NUM\_REFINEMENT\_STEPS**

Maximum number of steps to be used by the iterative refinement of the search direction. A negative value implies that the optimizer chooses the maximum number of iterative refinement steps.

Accepted Values: [-inf ;+inf ]

Default Value: -1

Groups: *Interior-point method*

**MSK\_IPAR\_INTPNT\_MULTI\_THREAD**

Controls whether the interior-point optimizers are allowed to employ multiple threads if more threads is available.

Accepted Values: *MSKonoffkeye*

Default Value: *MSK\_ON*



Groups: *Optimization system*

#### MSK\_IPAR\_INTPNT\_OFF\_COL\_TRH

Controls how many offending columns are detected in the Jacobian of the constraint matrix.

0	no detection
1	aggressive detection
> 1	higher values mean less aggressive detection

Accepted Values:  $[0 ; +\infty]$

Default Value: 40

Groups: *Interior-point method*

#### MSK\_IPAR\_INTPNT\_ORDER\_METHOD

Controls the ordering strategy used by the interior-point optimizer when factorizing the Newton equation system.

Accepted Values: *MSKorderingtypee*

Default Value: *MSK\_ORDER\_METHOD\_FREE*

Groups: *Interior-point method*

#### MSK\_IPAR\_INTPNT\_REGULARIZATION\_USE

Controls whether regularization is allowed.

Accepted Values: *MSKonoffkeye*

Default Value: *MSK\_ON*

Groups: *Interior-point method*

#### MSK\_IPAR\_INTPNT\_SCALING

Controls how the problem is scaled before the interior-point optimizer is used.

Accepted Values: *MSKscalingtypee*

Default Value: *MSK\_SCALING\_FREE*

Groups: *Interior-point method*

#### MSK\_IPAR\_INTPNT\_SOLVE\_FORM

Controls whether the primal or the dual problem is solved.

Accepted Values: *MSKsolveforme*

Default Value: *MSK\_SOLVE\_FREE*

Groups: *Interior-point method*

#### MSK\_IPAR\_INTPNT\_STARTING\_POINT

Starting point used by the interior-point optimizer.

Accepted Values: *MSKstartpointtypee*

Default Value: *MSK\_STARTING\_POINT\_FREE*

Groups: *Interior-point method*

#### MSK\_IPAR\_LICENSE\_DEBUG

This option is used to turn on debugging of the license manager.

Accepted Values: *MSKonoffkeye*

Default Value: *MSK\_OFF*

Groups: *License manager*

**MSK\_IPAR\_LICENSE\_PAUSE\_TIME**

If *MSK\_IPAR\_LICENSE\_WAIT* = *MSK\_ON* and no license is available, then **MOSEK** sleeps a number of milliseconds between each check of whether a license has become free.

Accepted Values: [0 ;1000000 ]

Default Value: 100

Groups: *License manager*

**MSK\_IPAR\_LICENSE\_SUPPRESS\_EXPIRE\_WRNS**

Controls whether license features expire warnings are suppressed.

Accepted Values: *MSK\_onoffkeye*

Default Value: *MSK\_OFF*

Groups: *License manager, Output information*

**MSK\_IPAR\_LICENSE\_TRH\_EXPIRY\_WRN**

If a license feature expires in a numbers days less than the value of this parameter then a warning will be issued.

Accepted Values: [0 ;+inf ]

Default Value: 7

**MSK\_IPAR\_LICENSE\_WAIT**

If all licenses are in use **MOSEK** returns with an error code. However, by turning on this parameter **MOSEK** will wait for an available license.

Accepted Values: *MSK\_onoffkeye*

Default Value: *MSK\_OFF*

Groups: *Overall solver, Optimization system, License manager*

**MSK\_IPAR\_LOG**

Controls the amount of log information. The value 0 implies that all log information is suppressed. A higher level implies that more information is logged.

Please note that if a task is employed to solve a sequence of optimization problems the value of this parameter is reduced by the value of *MSK\_IPAR\_LOG\_CUT\_SECOND\_OPT* for the second and any subsequent optimizations.

Accepted Values: [0 ;+inf ]

Default Value: 10

Groups: *Output information, Logging*

**MSK\_IPAR\_LOG\_ANA\_PRO**

Controls amount of output from the problem analyzer.

Accepted Values: [0 ;+inf ]

Default Value: 1

Groups: *Analysis, Logging*

**MSK\_IPAR\_LOG\_BI**

Controls the amount of output printed by the basis identification procedure. A higher level implies that more information is logged.

Accepted Values: [0 ;+inf ]

Default Value: 4

Groups: *Basis identification, Output information, Logging*

**MSK\_IPAR\_LOG\_BI\_FREQ**

Controls how frequent the optimizer outputs information about the basis identification and how frequent the user-defined call-back function is called.

Accepted Values: [0 ;+inf ]

Default Value: 2500

Groups: *Basis identification, Output information, Logging*

**MSK\_IPAR\_LOG\_CHECK\_CONVEXITY**

Controls logging in convexity check on quadratic problems. Set to a positive value to turn logging on. If a quadratic coefficient matrix is found to violate the requirement of PSD (NSD) then a list of negative (positive) pivot elements is printed. The absolute value of the pivot elements is also shown.

Accepted Values: [0 ;+inf ]

Default Value: 0

Groups: *Data check, Nonlinear convex method*

**MSK\_IPAR\_LOG\_CUT\_SECOND\_OPT**

If a task is employed to solve a sequence of optimization problems, then the value of the log levels is reduced by the value of this parameter. E.g *MSK\_IPAR\_LOG* and *MSK\_IPAR\_LOG\_SIM* are reduced by the value of this parameter for the second and any subsequent optimizations.

Accepted Values: [0 ;+inf ]

Default Value: 1

Groups: *Output information, Logging*

**MSK\_IPAR\_LOG\_EXPAND**

Controls the amount of logging when a data item such as the maximum number constraints is expanded.

Accepted Values: [0 ;+inf ]

Default Value: 0

Groups: *Output information, Logging*

**MSK\_IPAR\_LOG\_FACTOR**

If turned on, then the factor log lines are added to the log.

Accepted Values: [0 ;+inf ]

Default Value: 1

Groups: *Output information, Logging*

**MSK\_IPAR\_LOG\_FEAS\_REPAIR**

Controls the amount of output printed when performing feasibility repair. A value higher than one means extensive logging.

Accepted Values: [0 ;+inf ]

Default Value: 1

Groups: *Output information, Logging*

**MSK\_IPAR\_LOG\_FILE**

If turned on, then some log info is printed when a file is written or read.

Accepted Values: [0 ;+inf ]

Default Value: 1

Groups: *Data input/output, Output information, Logging*

**MSK\_IPAR\_LOG\_HEAD**

If turned on, then a header line is added to the log.

Accepted Values: [0 ;+inf ]

Default Value: 1

Groups: *Output information, Logging*

**MSK\_IPAR\_LOG\_INFEAS\_ANA**

Controls amount of output printed by the infeasibility analyzer procedures. A higher level implies that more information is logged.

Accepted Values: [0 ;+inf ]

Default Value: 1

Groups: *Infeasibility report, Output information, Logging*

**MSK\_IPAR\_LOG\_INTPNT**

Controls amount of output printed by the interior-point optimizer. A higher level implies that more information is logged.

Accepted Values: [0 ;+inf ]

Default Value: 4

Groups: *Interior-point method, Output information, Logging*

**MSK\_IPAR\_LOG\_MIO**

Controls the log level for the mixed-integer optimizer. A higher level implies that more information is logged.

Accepted Values: [0 ;+inf ]

Default Value: 4

Groups: *Mixed-integer optimization, Output information, Logging*

**MSK\_IPAR\_LOG\_MIO\_FREQ**

Controls how frequent the mixed-integer optimizer prints the log line. It will print line every time *MSK\_IPAR\_LOG\_MIO\_FREQ* relaxations have been solved.

Accepted Values: [-inf ;+inf ]

Default Value: 10

Groups: *Mixed-integer optimization, Output information, Logging*

**MSK\_IPAR\_LOG\_OPTIMIZER**

Controls the amount of general optimizer information that is logged.

Accepted Values: [0 ;+inf ]

Default Value: 1

Groups: *Output information, Logging*

**MSK\_IPAR\_LOG\_ORDER**

If turned on, then factor lines are added to the log.

Accepted Values: [0 ;+inf ]

Default Value: 1

Groups: *Output information, Logging*

**MSK\_IPAR\_LOG\_PRESOLVE**

Controls amount of output printed by the presolve procedure. A higher level implies that more information is logged.

Accepted Values: [0 ;+inf ]

Default Value: 1

Groups: *Interior-point method, Logging*

#### MSK\_IPAR\_LOG\_RESPONSE

Controls amount of output printed when response codes are reported. A higher level implies that more information is logged.

Accepted Values: [0 ;+inf ]

Default Value: 0

Groups: *Output information, Logging*

#### MSK\_IPAR\_LOG\_SENSITIVITY

Controls the amount of logging during the sensitivity analysis.

0.Means no logging information is produced.

1.Timing information is printed.

2.Sensitivity results are printed.

Accepted Values: [0 ;+inf ]

Default Value: 1

Groups: *Output information, Logging*

#### MSK\_IPAR\_LOG\_SENSITIVITY\_OPT

Controls the amount of logging from the optimizers employed during the sensitivity analysis. 0 means no logging information is produced.

Accepted Values: [0 ;+inf ]

Default Value: 0

Groups: *Output information, Logging*

#### MSK\_IPAR\_LOG\_SIM

Controls amount of output printed by the simplex optimizer. A higher level implies that more information is logged.

Accepted Values: [0 ;+inf ]

Default Value: 4

Groups: *Simplex optimizer, Output information, Logging*

#### MSK\_IPAR\_LOG\_SIM\_FREQ

Controls how frequent the simplex optimizer outputs information about the optimization and how frequent the user-defined call-back function is called.

Accepted Values: [0 ;+inf ]

Default Value: 1000

Groups: *Simplex optimizer, Output information, Logging*

#### MSK\_IPAR\_LOG\_SIM\_MINOR

Currently not in use.

Accepted Values: [0 ;+inf ]

Default Value: 1

Groups: *Simplex optimizer, Output information*

#### MSK\_IPAR\_LOG\_STORAGE

When turned on, **MOSEK** prints messages regarding the storage usage and allocation.

Accepted Values: [0 ;+inf ]

Default Value: 0

Groups: *Output information, Optimization system, Logging*

#### MSK\_IPAR\_MAX\_NUM\_WARNINGS

Each warning is shown a limit number times controlled by this parameter. A negative value is identical to infinite number of times.

Accepted Values: `[-inf ; +inf ]`

Default Value: `10`

Groups: *Output information*

#### MSK\_IPAR\_MIO\_BRANCH\_DIR

Controls whether the mixed-integer optimizer is branching up or down by default.

Accepted Values: *MSKbranchdire*

Default Value: *MSK\_BRANCH\_DIR\_FREE*

Groups: *Mixed-integer optimization*

#### MSK\_IPAR\_MIO\_CONSTRUCT\_SOL

If set to *MSK\_ON* and all integer variables have been given a value for which a feasible mixed integer solution exists, then **MOSEK** generates an initial solution to the mixed integer problem by fixing all integer values and solving the remaining problem.

Accepted Values: *MSKonoffkeye*

Default Value: *MSK\_OFF*

Groups: *Mixed-integer optimization*

#### MSK\_IPAR\_MIO\_CUT\_CLIQUE

Controls whether clique cuts should be generated.

Accepted Values: *MSKonoffkeye*

Default Value: *MSK\_ON*

Groups: *Mixed-integer optimization*

#### MSK\_IPAR\_MIO\_CUT\_CMIR

Controls whether mixed integer rounding cuts should be generated.

Accepted Values: *MSKonoffkeye*

Default Value: *MSK\_ON*

Groups: *Mixed-integer optimization*

#### MSK\_IPAR\_MIO\_CUT\_GMI

Controls whether GMI cuts should be generated.

Accepted Values: *MSKonoffkeye*

Default Value: *MSK\_ON*

Groups: *Mixed-integer optimization*

#### MSK\_IPAR\_MIO\_CUT\_IMPLIED\_BOUND

Controls whether implied bound cuts should be generated.

Accepted Values: *MSKonoffkeye*

Default Value: *MSK\_OFF*

Groups: *Mixed-integer optimization*

#### MSK\_IPAR\_MIO\_CUT\_KNAPSACK\_COVER

Controls whether knapsack cover cuts should be generated.

Accepted Values: *MSKonoffkeye*

Default Value: *MSK\_OFF*

Groups: *Mixed-integer optimization*

#### MSK\_IPAR\_MIO\_CUT\_SELECTION\_LEVEL

Controls how aggressively generated cuts are selected to be included in the relaxation.

-1. The optimizer chooses the level of cut selection

0. Generated cuts less likely to be added to the relaxation

1. Cuts are more aggressively selected to be included in the relaxation

Accepted Values: `[-1 ; +1 ]`

Default Value: `-1`

Groups: *Mixed-integer optimization*

#### MSK\_IPAR\_MIO\_HEURISTIC\_LEVEL

Controls the heuristic employed by the mixed-integer optimizer to locate an initial good integer feasible solution. A value of zero means the heuristic is not used at all. A larger value than 0 means that a gradually more sophisticated heuristic is used which is computationally more expensive. A negative value implies that the optimizer chooses the heuristic. Normally a value around 3 to 5 should be optimal.

Accepted Values: `[-inf ; +inf ]`

Default Value: `-1`

Groups: *Mixed-integer optimization*

#### MSK\_IPAR\_MIO\_MAX\_NUM\_BRANCHES

Maximum number of branches allowed during the branch and bound search. A negative value means infinite.

Accepted Values: `[-inf ; +inf ]`

Default Value: `-1`

Groups: *Mixed-integer optimization, Termination criterion*

#### MSK\_IPAR\_MIO\_MAX\_NUM\_RELAXS

Maximum number of relaxations allowed during the branch and bound search. A negative value means infinite.

Accepted Values: `[-inf ; +inf ]`

Default Value: `-1`

Groups: *Mixed-integer optimization*

#### MSK\_IPAR\_MIO\_MAX\_NUM\_SOLUTIONS

The mixed-integer optimizer can be terminated after a certain number of different feasible solutions has been located. If this parameter has the value  $n > 0$ , then the mixed-integer optimizer will be terminated when  $n$  feasible solutions have been located.

Accepted Values: `[-inf ; +inf ]`

Default Value: `-1`

Groups: *Mixed-integer optimization, Termination criterion*

#### MSK\_IPAR\_MIO\_MODE

Controls whether the optimizer includes the integer restrictions when solving a (mixed) integer optimization problem.

Accepted Values: *MSKmiomodee*

Default Value: *MSK\_MIO\_MODE\_SATISFIED*

Groups: *Overall solver*

**MSK\_IPAR\_MIO\_MT\_USER\_CB**

It true user callbacks are called from each thread used by this optimizer. If false the user callback is only called from a single thread.

Accepted Values: *MSKonoffkeye*

Default Value: *MSK\_OFF*

Groups: *Optimization system*

**MSK\_IPAR\_MIO\_NODE\_OPTIMIZER**

Controls which optimizer is employed at the non-root nodes in the mixed-integer optimizer.

Accepted Values: *MSKoptimizertypee*

Default Value: *MSK\_OPTIMIZER\_FREE*

Groups: *Mixed-integer optimization*

**MSK\_IPAR\_MIO\_NODE\_SELECTION**

Controls the node selection strategy employed by the mixed-integer optimizer.

Accepted Values: *MSKmionodeseltypee*

Default Value: *MSK\_MIO\_NODE\_SELECTION\_FREE*

Groups: *Mixed-integer optimization*

**MSK\_IPAR\_MIO\_PERSPECTIVE\_REFORMULATE**

Enables or disables perspective reformulation in presolve.

Accepted Values: *MSKonoffkeye*

Default Value: *MSK\_ON*

Groups: *Mixed-integer optimization*

**MSK\_IPAR\_MIO\_PROBING\_LEVEL**

Controls the amount of probing employed by the mixed-integer optimizer in presolve.

-1. The optimizer chooses the level of probing employed

0. Probing is disabled

1. A low amount of probing is employed

2. A medium amount of probing is employed

3. A high amount of probing is employed

Accepted Values: *[-inf ;+inf ]*

Default Value: *-1*

Groups: *Mixed-integer optimization*

**MSK\_IPAR\_MIO\_RINS\_MAX\_NODES**

Controls the maximum number of nodes allowed in each call to the RINS heuristic. The default value of -1 means that the value is determined automatically. A value of zero turns off the heuristic.

Accepted Values: *[-1 ;+inf ]*

Default Value: *-1*

Groups: *Mixed-integer optimization*

**MSK\_IPAR\_MIO\_ROOT\_OPTIMIZER**

Controls which optimizer is employed at the root node in the mixed-integer optimizer.

Accepted Values: *MSKoptimizertypee*

Default Value: *MSK\_OPTIMIZER\_FREE*

Groups: *Mixed-integer optimization*



**MSK\_IPAR\_MIO\_ROOT\_REPEAT\_PRESOLVE\_LEVEL**

Controls whether presolve can be repeated at root node.

- -1 The optimizer chooses whether presolve is repeated
- 0 Never repeat presolve
- 1 Always repeat presolve

Accepted Values: [-1 ; 1 ]

Default Value: -1

Groups: *Mixed-integer optimization*

**MSK\_IPAR\_MIO\_VB\_DETECTION\_LEVEL**

Controls how much effort is put into detecting variable bounds.

- 1. The optimizer chooses
  - 0. No variable bounds are detected
  - 1. Only detect variable bounds that are directly represented in the problem
  - 2. Detect variable bounds in probing

Accepted Values: [-1 ; +2 ]

Default Value: -1

Groups: *Mixed-integer optimization*

**MSK\_IPAR\_MT\_SPINCOUNT**

Set the number of iterations to spin before sleeping.

Accepted Values: [0 ; 1000000000 ]

Default Value: 0

Groups: *Optimization system*

**MSK\_IPAR\_NUM\_THREADS**

Controls the number of threads employed by the optimizer. If set to 0 the number of threads used will be equal to the number of cores detected on the machine.

Accepted Values: [0 ; +inf ]

Default Value: 0

Groups: *Optimization system*

**MSK\_IPAR\_OPF\_MAX\_TERMS\_PER\_LINE**

The maximum number of terms (linear and quadratic) per line when an OPF file is written.

Accepted Values: [0 ; +inf ]

Default Value: 5

Groups: *Data input/output*

**MSK\_IPAR\_OPF\_WRITE\_HEADER**

Write a text header with date and **MOSEK** version in an OPF file.

Accepted Values: *MSKonoffkeye*

Default Value: *MSK\_ON*

Groups: *Data input/output*

**MSK\_IPAR\_OPF\_WRITE\_HINTS**

Write a hint section with problem dimensions in the beginning of an OPF file.

Accepted Values: *MSKonoffkeye*

Default Value: *MSK\_ON*

Groups: *Data input/output*

#### MSK\_IPAR\_OPF\_WRITE\_PARAMETERS

Write a parameter section in an OPF file.

Accepted Values: *MSKonoffkeye*

Default Value: *MSK\_OFF*

Groups: *Data input/output*

#### MSK\_IPAR\_OPF\_WRITE\_PROBLEM

Write objective, constraints, bounds etc. to an OPF file.

Accepted Values: *MSKonoffkeye*

Default Value: *MSK\_ON*

Groups: *Data input/output*

#### MSK\_IPAR\_OPF\_WRITE\_SOLUTIONS

Enable inclusion of solutions in the OPF files.

Accepted Values: *MSKonoffkeye*

Default Value: *MSK\_OFF*

Groups: *Data input/output*

#### MSK\_IPAR\_OPF\_WRITE\_SOL\_BAS

If *MSK\_IPAR\_OPF\_WRITE\_SOLUTIONS* is *MSK\_ON* and a basic solution is defined, include the basic solution in OPF files.

Accepted Values: *MSKonoffkeye*

Default Value: *MSK\_ON*

Groups: *Data input/output*

#### MSK\_IPAR\_OPF\_WRITE\_SOL\_ITG

If *MSK\_IPAR\_OPF\_WRITE\_SOLUTIONS* is *MSK\_ON* and an integer solution is defined, write the integer solution in OPF files.

Accepted Values: *MSKonoffkeye*

Default Value: *MSK\_ON*

Groups: *Data input/output*

#### MSK\_IPAR\_OPF\_WRITE\_SOL\_ITR

If *MSK\_IPAR\_OPF\_WRITE\_SOLUTIONS* is *MSK\_ON* and an interior solution is defined, write the interior solution in OPF files.

Accepted Values: *MSKonoffkeye*

Default Value: *MSK\_ON*

Groups: *Data input/output*

#### MSK\_IPAR\_OPTIMIZER

The parameter controls which optimizer is used to optimize the task.

Accepted Values: *MSKoptimizertypee*

Default Value: *MSK\_OPTIMIZER\_FREE*

Groups: *Overall solver*

#### MSK\_IPAR\_PARAM\_READ\_CASE\_NAME

If turned on, then names in the parameter file are case sensitive.

Accepted Values: *MSKonoffkeye*

Default Value: *MSK\_ON*

Groups: *Data input/output*

#### MSK\_IPAR\_PARAM\_READ\_IGN\_ERROR

If turned on, then errors in parameter settings is ignored.

Accepted Values: *MSK\_onoffkeye*

Default Value: *MSK\_OFF*

Groups: *Data input/output*

#### MSK\_IPAR\_PRESOLVE\_ELIMINATOR\_MAX\_FILL

Controls the maximum amount of fill-in that can be created by one pivot in the elimination phase of the presolve. A negative value means the parameter value is selected automatically.

Accepted Values:  $[-inf ; +inf]$

Default Value: -1

Groups: *Presolve*

#### MSK\_IPAR\_PRESOLVE\_ELIMINATOR\_MAX\_NUM\_TRIES

Control the maximum number of times the eliminator is tried.

Accepted Values:  $[-inf ; +inf]$

Default Value: -1

Groups: *Presolve*

#### MSK\_IPAR\_PRESOLVE\_LEVEL

Currently not used.

Accepted Values:  $[-inf ; +inf]$

Default Value: -1

Groups: *Overall solver, Presolve*

#### MSK\_IPAR\_PRESOLVE\_LINDEP\_ABS\_WORK\_TRH

The linear dependency check is potentially computationally expensive.

Accepted Values:  $[-inf ; +inf]$

Default Value: 100

Groups: *Presolve*

#### MSK\_IPAR\_PRESOLVE\_LINDEP\_REL\_WORK\_TRH

The linear dependency check is potentially computationally expensive.

Accepted Values:  $[-inf ; +inf]$

Default Value: 100

Groups: *Presolve*

#### MSK\_IPAR\_PRESOLVE\_LINDEP\_USE

Controls whether the linear constraints are checked for linear dependencies.

Accepted Values: *MSK\_onoffkeye*

Default Value: *MSK\_ON*

Groups: *Presolve*

#### MSK\_IPAR\_PRESOLVE\_MAX\_NUM\_REDUCTIONS

Controls the maximum number of reductions performed by the presolve. The value of the parameter is normally only changed in connection with debugging. A negative value implies that an infinite number of reductions are allowed.

Accepted Values:  $[-inf ; +inf]$

Default Value: -1

**MSK\_IPAR\_PRESOLVE\_USE**

Controls whether the presolve is applied to a problem before it is optimized.

Accepted Values: *MSKpresolvemodee*

Default Value: *MSK\_PRESOLVE\_MODE\_FREE*

Groups: *Overall solver, Presolve*

**MSK\_IPAR\_PRIMAL\_REPAIR\_OPTIMIZER**

Controls which optimizer that is used to find the optimal repair.

Accepted Values: *MSKoptimizertypee*

Default Value: *MSK\_OPTIMIZER\_FREE*

Groups: *Overall solver*

**MSK\_IPAR\_READ\_DATA\_COMPRESSED**

If this option is turned on, it is assumed that the data file is compressed.

Accepted Values: *MSKcompresstypee*

Default Value: *MSK\_COMPRESS\_FREE*

Groups: *Data input/output*

**MSK\_IPAR\_READ\_DATA\_FORMAT**

Format of the data file to be read.

Accepted Values: *MSKdataformate*

Default Value: *MSK\_DATA\_FORMAT\_EXTENSION*

Groups: *Data input/output*

**MSK\_IPAR\_READ\_DEBUG**

Turns on additional debugging information when reading files.

Accepted Values: *MSKonoffkeye*

Default Value: *MSK\_OFF*

Groups: *Data input/output*

**MSK\_IPAR\_READ\_KEEP\_FREE\_CON**

Controls whether the free constraints are included in the problem.

Accepted Values: *MSKonoffkeye*

Default Value: *MSK\_OFF*

Groups: *Data input/output*

**MSK\_IPAR\_READ\_LP\_DROP\_NEW\_VARS\_IN\_BOU**

If this option is turned on, **MOSEK** will drop variables that are defined for the first time in the bounds section.

Accepted Values: *MSKonoffkeye*

Default Value: *MSK\_OFF*

Groups: *Data input/output*

**MSK\_IPAR\_READ\_LP\_QUOTED\_NAMES**

If a name is in quotes when reading an LP file, the quotes will be removed.

Accepted Values: *MSKonoffkeye*

Default Value: *MSK\_ON*

Groups: *Data input/output*

**MSK\_IPAR\_READ\_MPS\_FORMAT**

Controls how strictly the MPS file reader interprets the MPS format.

Accepted Values: *MSKmpsformat*

Default Value: *MSK\_MPS\_FORMAT\_FREE*

Groups: *Data input/output*

**MSK\_IPAR\_READ\_MPS\_WIDTH**

Controls the maximal number of characters allowed in one line of the MPS file.

Accepted Values: *[80 ;+inf ]*

Default Value: *1024*

Groups: *Data input/output*

**MSK\_IPAR\_READ\_TASK\_IGNORE\_PARAM**

Controls whether **MOSEK** should ignore the parameter setting defined in the task file and use the default parameter setting instead.

Accepted Values: *MSKonoffkeye*

Default Value: *MSK\_OFF*

Groups: *Data input/output*

**MSK\_IPAR\_SENSITIVITY\_ALL**

Not applicable.

Accepted Values: *MSKonoffkeye*

Default Value: *MSK\_OFF*

Groups: *Overall solver*

**MSK\_IPAR\_SENSITIVITY\_OPTIMIZER**

Controls which optimizer is used for optimal partition sensitivity analysis.

Accepted Values: *MSKoptimizertypee*

Default Value: *MSK\_OPTIMIZER\_FREE\_SIMPLEX*

Groups: *Overall solver, Simplex optimizer*

**MSK\_IPAR\_SENSITIVITY\_TYPE**

Controls which type of sensitivity analysis is to be performed.

Accepted Values: *MSKsensitivitytypee*

Default Value: *MSK\_SENSITIVITY\_TYPE\_BASIS*

Groups: *Overall solver*

**MSK\_IPAR\_SIM\_BASIS\_FACTOR\_USE**

Controls whether a (LU) factorization of the basis is used in a hot-start. Forcing a refactorization sometimes improves the stability of the simplex optimizers, but in most cases there is a performance penalty.

Accepted Values: *MSKonoffkeye*

Default Value: *MSK\_ON*

Groups: *Simplex optimizer*

**MSK\_IPAR\_SIM\_DEGEN**

Controls how aggressively degeneration is handled.

Accepted Values: *MSKsimdegene*

Default Value: *MSK\_SIM\_DEGEN\_FREE*

Groups: *Simplex optimizer*

**MSK\_IPAR\_SIM\_DUAL\_CRASH**

Controls whether crashing is performed in the dual simplex optimizer.

If this parameter is set to  $x$ , then a crash will be performed if a basis consists of more than  $(100 - x) \bmod f_v$  entries, where  $f_v$  is the number of fixed variables.

Accepted Values: `[0 ; +inf ]`

Default Value: `90`

Groups: *Dual simplex optimizer*

**MSK\_IPAR\_SIM\_DUAL\_PHASEONE\_METHOD**

An experimental feature.

Accepted Values: `[0 ; 10 ]`

Default Value: `0`

Groups: *Simplex optimizer*

**MSK\_IPAR\_SIM\_DUAL\_RESTRICT\_SELECTION**

The dual simplex optimizer can use a so-called restricted selection/pricing strategy to choose the outgoing variable. Hence, if restricted selection is applied, then the dual simplex optimizer first choose a subset of all the potential outgoing variables. Next, for some time it will choose the outgoing variable only among the subset. From time to time the subset is redefined.

A larger value of this parameter implies that the optimizer will be more aggressive in its restriction strategy, i.e. a value of 0 implies that the restriction strategy is not applied at all.

Accepted Values: `[0 ; 100 ]`

Default Value: `50`

Groups: *Dual simplex optimizer*

**MSK\_IPAR\_SIM\_DUAL\_SELECTION**

Controls the choice of the incoming variable, known as the selection strategy, in the dual simplex optimizer.

Accepted Values: *MSKsimseltypee*

Default Value: *MSK\_SIM\_SELECTION\_FREE*

Groups: *Dual simplex optimizer*

**MSK\_IPAR\_SIM\_EXPLOIT\_DUPVEC**

Controls if the simplex optimizers are allowed to exploit duplicated columns.

Accepted Values: *MSKsimdupvece*

Default Value: *MSK\_SIM\_EXPLOIT\_DUPVEC\_OFF*

Groups: *Simplex optimizer*

**MSK\_IPAR\_SIM\_HOTSTART**

Controls the type of hot-start that the simplex optimizer perform.

Accepted Values: *MSKsimhotstarte*

Default Value: *MSK\_SIM\_HOTSTART\_FREE*

Groups: *Simplex optimizer*

**MSK\_IPAR\_SIM\_HOTSTART\_LU**

Determines if the simplex optimizer should exploit the initial factorization.

Accepted Values: *MSKonoffkeye*

Default Value: *MSK\_ON*

**MSK\_IPAR\_SIM\_INTEGER**

An experimental feature.

Accepted Values: [0 ;10 ]

Default Value: 0

Groups: *Simplex optimizer*

**MSK\_IPAR\_SIM\_MAX\_ITERATIONS**

Maximum number of iterations that can be used by a simplex optimizer.

Accepted Values: [0 ;+inf ]

Default Value: 10000000

Groups: *Simplex optimizer, Termination criterion*

**MSK\_IPAR\_SIM\_MAX\_NUM\_SETBACKS**

Controls how many set-backs are allowed within a simplex optimizer. A set-back is an event where the optimizer moves in the wrong direction. This is impossible in theory but may happen due to numerical problems.

Accepted Values: [0 ;+inf ]

Default Value: 250

Groups: *Simplex optimizer*

**MSK\_IPAR\_SIM\_NON\_SINGULAR**

Controls if the simplex optimizer ensures a non-singular basis, if possible.

Accepted Values: *MSKonoffkeye*

Default Value: *MSK\_ON*

Groups: *Simplex optimizer*

**MSK\_IPAR\_SIM\_PRIMAL\_CRASH**

Controls whether crashing is performed in the primal simplex optimizer.

In general, if a basis consists of more than (100-this parameter value)% fixed variables, then a crash will be performed.

Accepted Values: [0 ;+inf ]

Default Value: 90

Groups: *Primal simplex optimizer*

**MSK\_IPAR\_SIM\_PRIMAL\_PHASEONE\_METHOD**

An experimental feature.

Accepted Values: [0 ;10 ]

Default Value: 0

Groups: *Simplex optimizer*

**MSK\_IPAR\_SIM\_PRIMAL\_RESTRICT\_SELECTION**

The primal simplex optimizer can use a so-called restricted selection/pricing strategy to choose the outgoing variable. Hence, if restricted selection is applied, then the primal simplex optimizer first choose a subset of all the potential incoming variables. Next, for some time it will choose the incoming variable only among the subset. From time to time the subset is redefined.

A larger value of this parameter implies that the optimizer will be more aggressive in its restriction strategy, i.e. a value of 0 implies that the restriction strategy is not applied at all.

Accepted Values: [0 ;100 ]

Default Value: 50

Groups: *Primal simplex optimizer*

**MSK\_IPAR\_SIM\_PRIMAL\_SELECTION**

Controls the choice of the incoming variable, known as the selection strategy, in the primal simplex optimizer.

Accepted Values: *MSKsimseltypee*

Default Value: *MSK\_SIM\_SELECTION\_FREE*

Groups: *Primal simplex optimizer*

**MSK\_IPAR\_SIM\_REFACTOR\_FREQ**

Controls how frequent the basis is refactorized. The value 0 means that the optimizer determines the best point of refactorization.

It is strongly recommended NOT to change this parameter.

Accepted Values: *[0 ;+inf ]*

Default Value: *0*

Groups: *Simplex optimizer*

**MSK\_IPAR\_SIM\_REFORMULATION**

Controls if the simplex optimizers are allowed to reformulate the problem.

Accepted Values: *MSKsimreforme*

Default Value: *MSK\_SIM\_REFORMULATION\_OFF*

Groups: *Simplex optimizer*

**MSK\_IPAR\_SIM\_SAVE\_LU**

Controls if the LU factorization stored should be replaced with the LU factorization corresponding to the initial basis.

Accepted Values: *MSKonoffkeye*

Default Value: *MSK\_OFF*

Groups: *Simplex optimizer*

**MSK\_IPAR\_SIM\_SCALING**

Controls how much effort is used in scaling the problem before a simplex optimizer is used.

Accepted Values: *MSKscalingtypee*

Default Value: *MSK\_SCALING\_FREE*

Groups: *Simplex optimizer*

**MSK\_IPAR\_SIM\_SCALING\_METHOD**

Controls how the problem is scaled before a simplex optimizer is used.

Accepted Values: *MSKscalingmethode*

Default Value: *MSK\_SCALING\_METHOD\_POW2*

Groups: *Simplex optimizer*

**MSK\_IPAR\_SIM\_SOLVE\_FORM**

Controls whether the primal or the dual problem is solved by the primal-/dual-simplex optimizer.

Accepted Values: *MSKsolveforme*

Default Value: *MSK\_SOLVE\_FREE*

Groups: *Simplex optimizer*

**MSK\_IPAR\_SIM\_STABILITY\_PRIORITY**

Controls how high priority the numerical stability should be given.

Accepted Values: *[0 ;100 ]*

Default Value: *50*



Groups: *Simplex optimizer*

#### MSK\_IPAR\_SIM\_SWITCH\_OPTIMIZER

The simplex optimizer sometimes chooses to solve the dual problem instead of the primal problem. This implies that if you have chosen to use the dual simplex optimizer and the problem is dualized, then it actually makes sense to use the primal simplex optimizer instead. If this parameter is on and the problem is dualized and furthermore the simplex optimizer is chosen to be the primal (dual) one, then it is switched to the dual (primal).

Accepted Values: *MSKonoffkeye*

Default Value: *MSK\_OFF*

Groups: *Simplex optimizer*

#### MSK\_IPAR\_SOLUTION\_CALLBACK

Indicates whether solution call-backs will be performed during the optimization.

Accepted Values: *MSKonoffkeye*

Default Value: *MSK\_OFF*

Groups: *Progress call-back, Overall solver*

#### MSK\_IPAR\_SOL\_FILTER\_KEEP\_BASIC

If turned on, then basic and super basic constraints and variables are written to the solution file independent of the filter setting.

Accepted Values: *MSKonoffkeye*

Default Value: *MSK\_OFF*

Groups: *Solution input/output*

#### MSK\_IPAR\_SOL\_FILTER\_KEEP\_RANGED

If turned on, then ranged constraints and variables are written to the solution file independent of the filter setting.

Accepted Values: *MSKonoffkeye*

Default Value: *MSK\_OFF*

Groups: *Solution input/output*

#### MSK\_IPAR\_SOL\_READ\_NAME\_WIDTH

When a solution is read by **MOSEK** and some constraint, variable or cone names contain blanks, then a maximum name width must be specified. A negative value implies that no name contain blanks.

Accepted Values: *[-inf ;+inf ]*

Default Value: *-1*

Groups: *Data input/output, Solution input/output*

#### MSK\_IPAR\_SOL\_READ\_WIDTH

Controls the maximal acceptable width of line in the solutions when read by **MOSEK**.

Accepted Values: *[0 ;+inf ]*

Default Value: *1024*

Groups: *Data input/output, Solution input/output*

#### MSK\_IPAR\_TIMING\_LEVEL

Controls the amount of timing performed inside **MOSEK**.

Accepted Values: *[0 ;+inf ]*

Default Value: *1*

Groups: *Optimization system*

**MSK\_IPAR\_WRITE\_BAS\_CONSTRAINTS**

Controls whether the constraint section is written to the basic solution file.

Accepted Values: *MSKonoffkeye*

Default Value: *MSK\_ON*

Groups: *Data input/output, Solution input/output*

**MSK\_IPAR\_WRITE\_BAS\_HEAD**

Controls whether the header section is written to the basic solution file.

Accepted Values: *MSKonoffkeye*

Default Value: *MSK\_ON*

Groups: *Data input/output, Solution input/output*

**MSK\_IPAR\_WRITE\_BAS\_VARIABLES**

Controls whether the variables section is written to the basic solution file.

Accepted Values: *MSKonoffkeye*

Default Value: *MSK\_ON*

Groups: *Data input/output, Solution input/output*

**MSK\_IPAR\_WRITE\_DATA\_COMPRESSED**

Controls whether the data file is compressed while it is written. 0 means no compression while higher values mean more compression.

Accepted Values: *[0 ;+inf ]*

Default Value: *0*

Groups: *Data input/output*

**MSK\_IPAR\_WRITE\_DATA\_FORMAT**

Controls the file format when writing task data to a file.

Accepted Values: *MSKdataformate*

Default Value: *MSK\_DATA\_FORMAT\_EXTENSION*

Groups: *Data input/output*

**MSK\_IPAR\_WRITE\_DATA\_PARAM**

If this option is turned on the parameter settings are written to the data file as parameters.

Accepted Values: *MSKonoffkeye*

Default Value: *MSK\_OFF*

Groups: *Data input/output*

**MSK\_IPAR\_WRITE\_FREE\_CON**

Controls whether the free constraints are written to the data file.

Accepted Values: *MSKonoffkeye*

Default Value: *MSK\_ON*

Groups: *Data input/output*

**MSK\_IPAR\_WRITE\_GENERIC\_NAMES**

Controls whether the generic names or user-defined names are used in the data file.

Accepted Values: *MSKonoffkeye*

Default Value: *MSK\_OFF*

Groups: *Data input/output*

**MSK\_IPAR\_WRITE\_GENERIC\_NAMES\_IO**

Index origin used in generic names.

Accepted Values: [0 ;+inf ]

Default Value: 1

Groups: *Data input/output*

**MSK\_IPAR\_WRITE\_IGNORE\_INCOMPATIBLE\_ITEMS**

Controls if the writer ignores incompatible problem items when writing files.

Accepted Values: *MSKonoffkeye*

Default Value: *MSK\_OFF*

Groups: *Data input/output*

**MSK\_IPAR\_WRITE\_INT\_CONSTRAINTS**

Controls whether the constraint section is written to the integer solution file.

Accepted Values: *MSKonoffkeye*

Default Value: *MSK\_ON*

Groups: *Data input/output, Solution input/output*

**MSK\_IPAR\_WRITE\_INT\_HEAD**

Controls whether the header section is written to the integer solution file.

Accepted Values: *MSKonoffkeye*

Default Value: *MSK\_ON*

Groups: *Data input/output, Solution input/output*

**MSK\_IPAR\_WRITE\_INT\_VARIABLES**

Controls whether the variables section is written to the integer solution file.

Accepted Values: *MSKonoffkeye*

Default Value: *MSK\_ON*

Groups: *Data input/output, Solution input/output*

**MSK\_IPAR\_WRITE\_LP\_FULL\_OBJ**

Write all variables, including the ones with 0-coefficients, in the objective.

Accepted Values: *MSKonoffkeye*

Default Value: *MSK\_ON*

Groups: *Data input/output*

**MSK\_IPAR\_WRITE\_LP\_LINE\_WIDTH**

Maximum width of line in an LP file written by **MOSEK**.

Accepted Values: [40 ;+inf ]

Default Value: 80

Groups: *Data input/output*

**MSK\_IPAR\_WRITE\_LP\_QUOTED\_NAMES**

If this option is turned on, then **MOSEK** will quote invalid LP names when writing an LP file.

Accepted Values: *MSKonoffkeye*

Default Value: *MSK\_ON*

Groups: *Data input/output*

**MSK\_IPAR\_WRITE\_LP\_STRICT\_FORMAT**

Controls whether LP output files satisfy the LP format strictly.

Accepted Values: *MSKonoffkeye*

Default Value: *MSK\_OFF*

Groups: *Data input/output*

**MSK\_IPAR\_WRITE\_LP\_TERMS\_PER\_LINE**

Maximum number of terms on a single line in an LP file written by **MOSEK**. 0 means unlimited.

Accepted Values: *[0 ;+inf ]*

Default Value: *10*

Groups: *Data input/output*

**MSK\_IPAR\_WRITE\_MPS\_FORMAT**

Controls in which format the MPS is written.

Accepted Values: *MSKmpsformate*

Default Value: *MSK\_MPS\_FORMAT\_FREE*

Groups: *Data input/output*

**MSK\_IPAR\_WRITE\_MPS\_INT**

Controls if marker records are written to the MPS file to indicate whether variables are integer restricted.

Accepted Values: *MSKonoffkeye*

Default Value: *MSK\_ON*

Groups: *Data input/output*

**MSK\_IPAR\_WRITE\_PRECISION**

Controls the precision with which **double** numbers are printed in the MPS data file. In general it is not worthwhile to use a value higher than 15.

Accepted Values: *[0 ;+inf ]*

Default Value: *15*

Groups: *Data input/output*

**MSK\_IPAR\_WRITE\_SOL\_BARVARIABLES**

Controls whether the symmetric matrix variables section is written to the solution file.

Accepted Values: *MSKonoffkeye*

Default Value: *MSK\_ON*

Groups: *Data input/output, Solution input/output*

**MSK\_IPAR\_WRITE\_SOL\_CONSTRAINTS**

Controls whether the constraint section is written to the solution file.

Accepted Values: *MSKonoffkeye*

Default Value: *MSK\_ON*

Groups: *Data input/output, Solution input/output*

**MSK\_IPAR\_WRITE\_SOL\_HEAD**

Controls whether the header section is written to the solution file.

Accepted Values: *MSKonoffkeye*

Default Value: *MSK\_ON*

Groups: *Data input/output, Solution input/output*

**MSK\_IPAR\_WRITE\_SOL\_IGNORE\_INVALID\_NAMES**

Even if the names are invalid MPS names, then they are employed when writing the solution file.

Accepted Values: *MSKonoffkeye*

Default Value: *MSK\_OFF*

Groups: *Data input/output, Solution input/output*

**MSK\_IPAR\_WRITE\_SOL\_VARIABLES**

Controls whether the variables section is written to the solution file.

Accepted Values: *MSKonoffkeye*

Default Value: *MSK\_ON*

Groups: *Data input/output, Solution input/output*

**MSK\_IPAR\_WRITE\_TASK\_INC\_SOL**

Controls whether the solutions are stored in the task file too.

Accepted Values: *MSKonoffkeye*

Default Value: *MSK\_ON*

Groups: *Data input/output*

**MSK\_IPAR\_WRITE\_XML\_MODE**

Controls if linear coefficients should be written by row or column when writing in the XML file format.

Accepted Values: *MSKxmlwriteroutputtypee*

Default Value: *MSK\_WRITE\_XML\_MODE\_ROW*

Groups: *Data input/output*

**String Parameters****MSK\_SPAR\_BAS\_SOL\_FILE\_NAME**

Name of the bas solution file.

Accepted Values: Any valid file name.

Groups: *Data input/output, Solution input/output*

**MSK\_SPAR\_DATA\_FILE\_NAME**

Data are read and written to this file.

Accepted Values: Any valid file name.

Groups: *Data input/output*

**MSK\_SPAR\_DEBUG\_FILE\_NAME**

**MOSEK** debug file.

Accepted Values: Any valid file name.

Groups: *Data input/output*

**MSK\_SPAR\_INT\_SOL\_FILE\_NAME**

Name of the int solution file.

Accepted Values: Any valid file name.

Groups: *Data input/output, Solution input/output*

**MSK\_SPAR\_ITR\_SOL\_FILE\_NAME**

Name of the itr solution file.

Accepted Values: Any valid file name.

Groups: *Data input/output, Solution input/output*

**MSK\_SPAR\_MIO\_DEBUG\_STRING**

For internal use only.

Accepted Values: Any valid string.

Groups: *Data input/output*

**MSK\_SPAR\_PARAM\_COMMENT\_SIGN**

Only the first character in this string is used. It is considered as a start of comment sign in the **MOSEK** parameter file. Spaces are ignored in the string.

Accepted Values: Any valid string.

Default Value: %%

Groups: *Data input/output*

**MSK\_SPAR\_PARAM\_READ\_FILE\_NAME**

Modifications to the parameter database is read from this file.

Accepted Values: Any valid file name.

Groups: *Data input/output*

**MSK\_SPAR\_PARAM\_WRITE\_FILE\_NAME**

The parameter database is written to this file.

Accepted Values: Any valid file name.

Groups: *Data input/output*

**MSK\_SPAR\_READ\_MPS\_BOU\_NAME**

Name of the BOUNDS vector used. An empty name means that the first BOUNDS vector is used.

Accepted Values: Any valid MPS name.

Groups: *Data input/output*

**MSK\_SPAR\_READ\_MPS\_OBJ\_NAME**

Name of the free constraint used as objective function. An empty name means that the first constraint is used as objective function.

Accepted Values: Any valid MPS name.

Groups: *Data input/output*

**MSK\_SPAR\_READ\_MPS\_RAN\_NAME**

Name of the RANGE vector used. An empty name means that the first RANGE vector is used.

Accepted Values: Any valid MPS name.

Groups: *Data input/output*

**MSK\_SPAR\_READ\_MPS\_RHS\_NAME**

Name of the RHS used. An empty name means that the first RHS vector is used.

Accepted Values: Any valid MPS name.

Groups: *Data input/output*

**MSK\_SPAR\_REMOTE\_ACCESS\_TOKEN**

An access token used to submit tasks to a remote **MOSEK** server. An access token is a random 32-byte string encoded in base64, i.e. it is a 44 character ASCII string.

Accepted Values: Any valid string.

**MSK\_SPAR\_SENSITIVITY\_FILE\_NAME**

Not applicable.

Accepted Values: Any valid string.

Groups: *Data input/output*

MSK\_SPAR\_SENSITIVITY\_RES\_FILE\_NAME

Not applicable.

Accepted Values: Any valid string.

Groups: *Data input/output*

MSK\_SPAR\_SOL\_FILTER\_XC\_LOW

A filter used to determine which constraints should be listed in the solution file. A value of 0.5 means that all constraints having  $xc[i] > 0.5$  should be listed, whereas +0.5 means that all constraints having  $xc[i] \geq blc[i] + 0.5$  should be listed. An empty filter means that no filter is applied.

Accepted Values: Any valid filter.

Groups: *Data input/output, Solution input/output*

MSK\_SPAR\_SOL\_FILTER\_XC\_UPR

A filter used to determine which constraints should be listed in the solution file. A value of 0.5 means that all constraints having  $xc[i] < 0.5$  should be listed, whereas -0.5 means all constraints having  $xc[i] \leq buc[i] - 0.5$  should be listed. An empty filter means that no filter is applied.

Accepted Values: Any valid filter.

Groups: *Data input/output, Solution input/output*

MSK\_SPAR\_SOL\_FILTER\_XX\_LOW

A filter used to determine which variables should be listed in the solution file. A value of "0.5" means that all constraints having  $xx[j] \geq 0.5$  should be listed, whereas "+0.5" means that all constraints having  $xx[j] \geq blx[j] + 0.5$  should be listed. An empty filter means no filter is applied.

Accepted Values: Any valid filter.

Groups: *Data input/output, Solution input/output*

MSK\_SPAR\_SOL\_FILTER\_XX\_UPR

A filter used to determine which variables should be listed in the solution file. A value of "0.5" means that all constraints having  $xx[j] < 0.5$  should be printed, whereas "-0.5" means all constraints having  $xx[j] \leq bux[j] - 0.5$  should be listed. An empty filter means no filter is applied.

Accepted Values: Any valid file name.

Groups: *Data input/output, Solution input/output*

MSK\_SPAR\_STAT\_FILE\_NAME

Statistics file name.

Accepted Values: Any valid file name.

Groups: *Data input/output*

MSK\_SPAR\_STAT\_KEY

Key used when writing the summary file.

Accepted Values: Any valid XML string.

Groups: *Data input/output*

MSK\_SPAR\_STAT\_NAME

Name used when writing the statistics file.

Accepted Values: Any valid XML string.

Groups: *Data input/output*

MSK\_SPAR\_WRITE\_LP\_GEN\_VAR\_NAME

Sometimes when an LP file is written additional variables must be inserted. They will have the prefix denoted by this parameter.

Accepted Values: Any valid string.

Default Value: `xmskgen`

Groups: `Data input/output`

### 11.1.2 Infeasibility report parameters.

- `MSK_IPAR_INFEAS_GENERIC_NAMES`
- `MSK_IPAR_INFEAS_REPORT_LEVEL`
- `MSK_IPAR_LOG_INFEAS_ANA`

### 11.1.3 Logging parameters.

- `MSK_IPAR_LOG`
- `MSK_IPAR_LOG_ANA_PRO`
- `MSK_IPAR_LOG_BI`
- `MSK_IPAR_LOG_BI_FREQ`
- `MSK_IPAR_LOG_CUT_SECOND_OPT`
- `MSK_IPAR_LOG_EXPAND`
- `MSK_IPAR_LOG_FACTOR`
- `MSK_IPAR_LOG_FEAS_REPAIR`
- `MSK_IPAR_LOG_FILE`
- `MSK_IPAR_LOG_HEAD`
- `MSK_IPAR_LOG_INFEAS_ANA`
- `MSK_IPAR_LOG_INTPNT`
- `MSK_IPAR_LOG_MIO`
- `MSK_IPAR_LOG_MIO_FREQ`
- `MSK_IPAR_LOG_OPTIMIZER`
- `MSK_IPAR_LOG_ORDER`
- `MSK_IPAR_LOG_PRESOLVE`
- `MSK_IPAR_LOG_RESPONSE`
- `MSK_IPAR_LOG_SENSITIVITY`
- `MSK_IPAR_LOG_SENSITIVITY_OPT`
- `MSK_IPAR_LOG_SIM`
- `MSK_IPAR_LOG_SIM_FREQ`
- `MSK_IPAR_LOG_STORAGE`

### 11.1.4 Data input/output parameters.

- `MSK_SPAR_BAS_SOL_FILE_NAME`
- `MSK_SPAR_DATA_FILE_NAME`
- `MSK_SPAR_DEBUG_FILE_NAME`
- `MSK_IPAR_INFEAS_REPORT_AUTO`



- *MSK\_SPAR\_INT\_SOL\_FILE\_NAME*
- *MSK\_SPAR\_ITR\_SOL\_FILE\_NAME*
- *MSK\_IPAR\_LOG\_FILE*
- *MSK\_SPAR\_MIO\_DEBUG\_STRING*
- *MSK\_IPAR\_OPF\_MAX\_TERMS\_PER\_LINE*
- *MSK\_IPAR\_OPF\_WRITE\_HEADER*
- *MSK\_IPAR\_OPF\_WRITE\_HINTS*
- *MSK\_IPAR\_OPF\_WRITE\_PARAMETERS*
- *MSK\_IPAR\_OPF\_WRITE\_PROBLEM*
- *MSK\_IPAR\_OPF\_WRITE\_SOL\_BAS*
- *MSK\_IPAR\_OPF\_WRITE\_SOL\_ITG*
- *MSK\_IPAR\_OPF\_WRITE\_SOL\_ITR*
- *MSK\_IPAR\_OPF\_WRITE\_SOLUTIONS*
- *MSK\_SPAR\_PARAM\_COMMENT\_SIGN*
- *MSK\_IPAR\_PARAM\_READ\_CASE\_NAME*
- *MSK\_SPAR\_PARAM\_READ\_FILE\_NAME*
- *MSK\_IPAR\_PARAM\_READ\_IGN\_ERROR*
- *MSK\_SPAR\_PARAM\_WRITE\_FILE\_NAME*
- *MSK\_IPAR\_READ\_DATA\_COMPRESSED*
- *MSK\_IPAR\_READ\_DATA\_FORMAT*
- *MSK\_IPAR\_READ\_DEBUG*
- *MSK\_IPAR\_READ\_KEEP\_FREE\_CON*
- *MSK\_IPAR\_READ\_LP\_DROP\_NEW\_VARS\_IN\_BOU*
- *MSK\_IPAR\_READ\_LP\_QUOTED\_NAMES*
- *MSK\_SPAR\_READ\_MPS\_BOU\_NAME*
- *MSK\_IPAR\_READ\_MPS\_FORMAT*
- *MSK\_SPAR\_READ\_MPS\_OBJ\_NAME*
- *MSK\_SPAR\_READ\_MPS\_RAN\_NAME*
- *MSK\_SPAR\_READ\_MPS\_RHS\_NAME*
- *MSK\_IPAR\_READ\_MPS\_WIDTH*
- *MSK\_IPAR\_READ\_TASK\_IGNORE\_PARAM*
- *MSK\_SPAR\_SENSITIVITY\_FILE\_NAME*
- *MSK\_SPAR\_SENSITIVITY\_RES\_FILE\_NAME*
- *MSK\_SPAR\_SOL\_FILTER\_XC\_LOW*
- *MSK\_SPAR\_SOL\_FILTER\_XC\_UPR*
- *MSK\_SPAR\_SOL\_FILTER\_XX\_LOW*
- *MSK\_SPAR\_SOL\_FILTER\_XX\_UPR*
- *MSK\_IPAR\_SOL\_READ\_NAME\_WIDTH*
- *MSK\_IPAR\_SOL\_READ\_WIDTH*

- *MSK\_SPAR\_STAT\_FILE\_NAME*
- *MSK\_SPAR\_STAT\_KEY*
- *MSK\_SPAR\_STAT\_NAME*
- *MSK\_IPAR\_WRITE\_BAS\_CONSTRAINTS*
- *MSK\_IPAR\_WRITE\_BAS\_HEAD*
- *MSK\_IPAR\_WRITE\_BAS\_VARIABLES*
- *MSK\_IPAR\_WRITE\_DATA\_COMPRESSED*
- *MSK\_IPAR\_WRITE\_DATA\_FORMAT*
- *MSK\_IPAR\_WRITE\_DATA\_PARAM*
- *MSK\_IPAR\_WRITE\_FREE\_CON*
- *MSK\_IPAR\_WRITE\_GENERIC\_NAMES*
- *MSK\_IPAR\_WRITE\_GENERIC\_NAMES\_IO*
- *MSK\_IPAR\_WRITE\_IGNORE\_INCOMPATIBLE\_ITEMS*
- *MSK\_IPAR\_WRITE\_INT\_CONSTRAINTS*
- *MSK\_IPAR\_WRITE\_INT\_HEAD*
- *MSK\_IPAR\_WRITE\_INT\_VARIABLES*
- *MSK\_IPAR\_WRITE\_LP\_FULL\_OBJ*
- *MSK\_SPAR\_WRITE\_LP\_GEN\_VAR\_NAME*
- *MSK\_IPAR\_WRITE\_LP\_LINE\_WIDTH*
- *MSK\_IPAR\_WRITE\_LP\_QUOTED\_NAMES*
- *MSK\_IPAR\_WRITE\_LP\_STRICT\_FORMAT*
- *MSK\_IPAR\_WRITE\_LP\_TERMS\_PER\_LINE*
- *MSK\_IPAR\_WRITE\_MPS\_FORMAT*
- *MSK\_IPAR\_WRITE\_MPS\_INT*
- *MSK\_IPAR\_WRITE\_PRECISION*
- *MSK\_IPAR\_WRITE\_SOL\_BARVARIABLES*
- *MSK\_IPAR\_WRITE\_SOL\_CONSTRAINTS*
- *MSK\_IPAR\_WRITE\_SOL\_HEAD*
- *MSK\_IPAR\_WRITE\_SOL\_IGNORE\_INVALID\_NAMES*
- *MSK\_IPAR\_WRITE\_SOL\_VARIABLES*
- *MSK\_IPAR\_WRITE\_TASK\_INC\_SOL*
- *MSK\_IPAR\_WRITE\_XML\_MODE*

### 11.1.5 Presolve parameters.

- *MSK\_IPAR\_PRESOLVE\_ELIMINATOR\_MAX\_FILL*
- *MSK\_IPAR\_PRESOLVE\_ELIMINATOR\_MAX\_NUM\_TRIES*
- *MSK\_IPAR\_PRESOLVE\_LEVEL*
- *MSK\_IPAR\_PRESOLVE\_LINDEP\_ABS\_WORK\_TRH*
- *MSK\_IPAR\_PRESOLVE\_LINDEP\_REL\_WORK\_TRH*

- *MSK\_IPAR\_PRESOLVE\_LINDEP\_USE*
- *MSK\_DPAR\_PRESOLVE\_TOL\_ABS\_LINDEP*
- *MSK\_DPAR\_PRESOLVE\_TOL\_AIJ*
- *MSK\_DPAR\_PRESOLVE\_TOL\_REL\_LINDEP*
- *MSK\_DPAR\_PRESOLVE\_TOL\_S*
- *MSK\_DPAR\_PRESOLVE\_TOL\_X*
- *MSK\_IPAR\_PRESOLVE\_USE*

### 11.1.6 Interior-point method parameters.

- *MSK\_IPAR\_BI\_IGNORE\_MAX\_ITER*
- *MSK\_IPAR\_BI\_IGNORE\_NUM\_ERROR*
- *MSK\_DPAR\_CHECK\_CONVEXITY\_REL\_TOL*
- *MSK\_IPAR\_INTPNT\_BASIS*
- *MSK\_DPAR\_INTPNT\_CO\_TOL\_DFEAS*
- *MSK\_DPAR\_INTPNT\_CO\_TOL\_INFEAS*
- *MSK\_DPAR\_INTPNT\_CO\_TOL\_MU\_RED*
- *MSK\_DPAR\_INTPNT\_CO\_TOL\_NEAR\_REL*
- *MSK\_DPAR\_INTPNT\_CO\_TOL\_PFEAS*
- *MSK\_DPAR\_INTPNT\_CO\_TOL\_REL\_GAP*
- *MSK\_IPAR\_INTPNT\_DIFF\_STEP*
- *MSK\_IPAR\_INTPNT\_HOTSTART*
- *MSK\_IPAR\_INTPNT\_MAX\_ITERATIONS*
- *MSK\_IPAR\_INTPNT\_MAX\_NUM\_COR*
- *MSK\_IPAR\_INTPNT\_MAX\_NUM\_REFINEMENT\_STEPS*
- *MSK\_DPAR\_INTPNT\_NL\_MERIT\_BAL*
- *MSK\_DPAR\_INTPNT\_NL\_TOL\_DFEAS*
- *MSK\_DPAR\_INTPNT\_NL\_TOL\_MU\_RED*
- *MSK\_DPAR\_INTPNT\_NL\_TOL\_NEAR\_REL*
- *MSK\_DPAR\_INTPNT\_NL\_TOL\_PFEAS*
- *MSK\_DPAR\_INTPNT\_NL\_TOL\_REL\_GAP*
- *MSK\_DPAR\_INTPNT\_NL\_TOL\_REL\_STEP*
- *MSK\_IPAR\_INTPNT\_OFF\_COL\_TRH*
- *MSK\_IPAR\_INTPNT\_ORDER\_METHOD*
- *MSK\_DPAR\_INTPNT\_QO\_TOL\_DFEAS*
- *MSK\_DPAR\_INTPNT\_QO\_TOL\_INFEAS*
- *MSK\_DPAR\_INTPNT\_QO\_TOL\_MU\_RED*
- *MSK\_DPAR\_INTPNT\_QO\_TOL\_NEAR\_REL*
- *MSK\_DPAR\_INTPNT\_QO\_TOL\_PFEAS*
- *MSK\_DPAR\_INTPNT\_QO\_TOL\_REL\_GAP*

- *MSK\_IPAR\_INTPNT\_REGULARIZATION\_USE*
- *MSK\_IPAR\_INTPNT\_SCALING*
- *MSK\_IPAR\_INTPNT\_SOLVE\_FORM*
- *MSK\_IPAR\_INTPNT\_STARTING\_POINT*
- *MSK\_DPAR\_INTPNT\_TOL\_DFEAS*
- *MSK\_DPAR\_INTPNT\_TOL\_DSAFE*
- *MSK\_DPAR\_INTPNT\_TOL\_INFEAS*
- *MSK\_DPAR\_INTPNT\_TOL\_MU\_RED*
- *MSK\_DPAR\_INTPNT\_TOL\_PATH*
- *MSK\_DPAR\_INTPNT\_TOL\_PFEAS*
- *MSK\_DPAR\_INTPNT\_TOL\_PSAFE*
- *MSK\_DPAR\_INTPNT\_TOL\_REL\_GAP*
- *MSK\_DPAR\_INTPNT\_TOL\_REL\_STEP*
- *MSK\_DPAR\_INTPNT\_TOL\_STEP\_SIZE*
- *MSK\_IPAR\_LOG\_INTPNT*
- *MSK\_IPAR\_LOG\_PRESOLVE*
- *MSK\_DPAR\_QCQO\_REFORMULATE\_REL\_DROP\_TOL*

#### 11.1.7 Overall solver parameters.

- *MSK\_IPAR\_BI\_CLEAN\_OPTIMIZER*
- *MSK\_IPAR\_INFEAS\_PREFER\_PRIMAL*
- *MSK\_IPAR\_LICENSE\_WAIT*
- *MSK\_IPAR\_MIO\_MODE*
- *MSK\_IPAR\_OPTIMIZER*
- *MSK\_IPAR\_PRESOLVE\_LEVEL*
- *MSK\_IPAR\_PRESOLVE\_USE*
- *MSK\_IPAR\_PRIMAL\_REPAIR\_OPTIMIZER*
- *MSK\_IPAR\_SENSITIVITY\_ALL*
- *MSK\_IPAR\_SENSITIVITY\_OPTIMIZER*
- *MSK\_IPAR\_SENSITIVITY\_TYPE*
- *MSK\_IPAR\_SOLUTION\_CALLBACK*

#### 11.1.8 Termination criterion parameters.

- *MSK\_DPAR\_BASIS\_REL\_TOL\_S*
- *MSK\_DPAR\_BASIS\_TOL\_S*
- *MSK\_DPAR\_BASIS\_TOL\_X*
- *MSK\_IPAR\_BI\_MAX\_ITERATIONS*
- *MSK\_DPAR\_INTPNT\_CO\_TOL\_DFEAS*

- *MSK\_DPAR\_INTPNT\_CO\_TOL\_INFEAS*
- *MSK\_DPAR\_INTPNT\_CO\_TOL\_MU\_RED*
- *MSK\_DPAR\_INTPNT\_CO\_TOL\_NEAR\_REL*
- *MSK\_DPAR\_INTPNT\_CO\_TOL\_PFEAS*
- *MSK\_DPAR\_INTPNT\_CO\_TOL\_REL\_GAP*
- *MSK\_IPAR\_INTPNT\_MAX\_ITERATIONS*
- *MSK\_DPAR\_INTPNT\_NL\_TOL\_DFEAS*
- *MSK\_DPAR\_INTPNT\_NL\_TOL\_MU\_RED*
- *MSK\_DPAR\_INTPNT\_NL\_TOL\_NEAR\_REL*
- *MSK\_DPAR\_INTPNT\_NL\_TOL\_PFEAS*
- *MSK\_DPAR\_INTPNT\_NL\_TOL\_REL\_GAP*
- *MSK\_DPAR\_INTPNT\_QO\_TOL\_DFEAS*
- *MSK\_DPAR\_INTPNT\_QO\_TOL\_INFEAS*
- *MSK\_DPAR\_INTPNT\_QO\_TOL\_MU\_RED*
- *MSK\_DPAR\_INTPNT\_QO\_TOL\_NEAR\_REL*
- *MSK\_DPAR\_INTPNT\_QO\_TOL\_PFEAS*
- *MSK\_DPAR\_INTPNT\_QO\_TOL\_REL\_GAP*
- *MSK\_DPAR\_INTPNT\_TOL\_DFEAS*
- *MSK\_DPAR\_INTPNT\_TOL\_INFEAS*
- *MSK\_DPAR\_INTPNT\_TOL\_MU\_RED*
- *MSK\_DPAR\_INTPNT\_TOL\_PFEAS*
- *MSK\_DPAR\_INTPNT\_TOL\_REL\_GAP*
- *MSK\_DPAR\_LOWER\_OBJ\_CUT*
- *MSK\_DPAR\_LOWER\_OBJ\_CUT\_FINITE\_TRH*
- *MSK\_DPAR\_MIO\_DISABLE\_TERM\_TIME*
- *MSK\_IPAR\_MIO\_MAX\_NUM\_BRANCHES*
- *MSK\_IPAR\_MIO\_MAX\_NUM\_SOLUTIONS*
- *MSK\_DPAR\_MIO\_MAX\_TIME*
- *MSK\_DPAR\_MIO\_NEAR\_TOL\_REL\_GAP*
- *MSK\_DPAR\_MIO\_REL\_GAP\_CONST*
- *MSK\_DPAR\_MIO\_TOL\_REL\_GAP*
- *MSK\_DPAR\_OPTIMIZER\_MAX\_TIME*
- *MSK\_IPAR\_SIM\_MAX\_ITERATIONS*
- *MSK\_DPAR\_UPPER\_OBJ\_CUT*
- *MSK\_DPAR\_UPPER\_OBJ\_CUT\_FINITE\_TRH*

### 11.1.9 Conic interior-point method parameters.

- *MSK\_DPAR\_INTPNT\_CO\_TOL\_DFEAS*
- *MSK\_DPAR\_INTPNT\_CO\_TOL\_INFEAS*
- *MSK\_DPAR\_INTPNT\_CO\_TOL\_MU\_RED*
- *MSK\_DPAR\_INTPNT\_CO\_TOL\_NEAR\_REL*
- *MSK\_DPAR\_INTPNT\_CO\_TOL\_PFEAS*
- *MSK\_DPAR\_INTPNT\_CO\_TOL\_REL\_GAP*

### 11.1.10 Nonlinear convex method parameters.

- *MSK\_IPAR\_CHECK\_CONVEXITY*
- *MSK\_DPAR\_INTPNT\_NL\_MERIT\_BAL*
- *MSK\_DPAR\_INTPNT\_NL\_TOL\_DFEAS*
- *MSK\_DPAR\_INTPNT\_NL\_TOL\_MU\_RED*
- *MSK\_DPAR\_INTPNT\_NL\_TOL\_NEAR\_REL*
- *MSK\_DPAR\_INTPNT\_NL\_TOL\_PFEAS*
- *MSK\_DPAR\_INTPNT\_NL\_TOL\_REL\_GAP*
- *MSK\_DPAR\_INTPNT\_NL\_TOL\_REL\_STEP*
- *MSK\_DPAR\_INTPNT\_TOL\_INFEAS*
- *MSK\_IPAR\_LOG\_CHECK\_CONVEXITY*

### 11.1.11 Optimization system parameters.

- *MSK\_IPAR\_AUTO\_UPDATE\_SOL\_INFO*
- *MSK\_IPAR\_INTPNT\_MULTI\_THREAD*
- *MSK\_IPAR\_LICENSE\_WAIT*
- *MSK\_IPAR\_LOG\_STORAGE*
- *MSK\_IPAR\_MIO\_MT\_USER\_CB*
- *MSK\_IPAR\_MT\_SPINCOUNT*
- *MSK\_IPAR\_NUM\_THREADS*
- *MSK\_IPAR\_TIMING\_LEVEL*

### 11.1.12 Basis identification parameters.

- *MSK\_IPAR\_BI\_CLEAN\_OPTIMIZER*
- *MSK\_IPAR\_BI\_IGNORE\_MAX\_ITER*
- *MSK\_IPAR\_BI\_IGNORE\_NUM\_ERROR*
- *MSK\_IPAR\_BI\_MAX\_ITERATIONS*
- *MSK\_IPAR\_INTPNT\_BASIS*
- *MSK\_IPAR\_LOG\_BI*
- *MSK\_IPAR\_LOG\_BI\_FREQ*

- *MSK\_DPAR\_SIM\_LU\_TOL\_REL\_PIV*

#### 11.1.13 Analysis parameters.

- *MSK\_IPAR\_ANA\_SOL\_BASIS*
- *MSK\_DPAR\_ANA\_SOL\_INFEAS\_TOL*
- *MSK\_IPAR\_ANA\_SOL\_PRINT\_VIOLATED*
- *MSK\_IPAR\_LOG\_ANA\_PRO*

#### 11.1.14 Data check parameters.

- *MSK\_IPAR\_CHECK\_CONVEXITY*
- *MSK\_DPAR\_DATA\_SYM\_MAT\_TOL*
- *MSK\_DPAR\_DATA\_SYM\_MAT\_TOL\_HUGE*
- *MSK\_DPAR\_DATA\_SYM\_MAT\_TOL\_LARGE*
- *MSK\_DPAR\_DATA\_TOL\_AIJ*
- *MSK\_DPAR\_DATA\_TOL\_AIJ\_HUGE*
- *MSK\_DPAR\_DATA\_TOL\_AIJ\_LARGE*
- *MSK\_DPAR\_DATA\_TOL\_BOUND\_INF*
- *MSK\_DPAR\_DATA\_TOL\_BOUND\_WRN*
- *MSK\_DPAR\_DATA\_TOL\_C\_HUGE*
- *MSK\_DPAR\_DATA\_TOL\_CJ\_LARGE*
- *MSK\_DPAR\_DATA\_TOL\_QIJ*
- *MSK\_DPAR\_DATA\_TOL\_X*
- *MSK\_IPAR\_LOG\_CHECK\_CONVEXITY*
- *MSK\_DPAR\_SEMIDEFINITE\_TOL\_APPROX*

#### 11.1.15 Primal simplex optimizer parameters.

- *MSK\_IPAR\_SIM\_PRIMAL\_CRASH*
- *MSK\_IPAR\_SIM\_PRIMAL\_RESTRICT\_SELECTION*
- *MSK\_IPAR\_SIM\_PRIMAL\_SELECTION*

#### 11.1.16 Progress call-back parameters.

- *MSK\_IPAR\_SOLUTION\_CALLBACK*

#### 11.1.17 License manager parameters.

- *MSK\_IPAR\_CACHE\_LICENSE*
- *MSK\_IPAR\_LICENSE\_DEBUG*
- *MSK\_IPAR\_LICENSE\_PAUSE\_TIME*
- *MSK\_IPAR\_LICENSE\_SUPPRESS\_EXPIRE\_WRNS*

- *MSK\_IPAR\_LICENSE\_WAIT*

#### 11.1.18 Debugging parameters.

- *MSK\_IPAR\_AUTO\_SORT\_A\_BEFORE\_OPT*

#### 11.1.19 Dual simplex optimizer parameters.

- *MSK\_IPAR\_SIM\_DUAL\_CRASH*
- *MSK\_IPAR\_SIM\_DUAL\_RESTRICT\_SELECTION*
- *MSK\_IPAR\_SIM\_DUAL\_SELECTION*

#### 11.1.20 Mixed-integer optimization parameters.

- *MSK\_IPAR\_LOG\_MIO*
- *MSK\_IPAR\_LOG\_MIO\_FREQ*
- *MSK\_IPAR\_MIO\_BRANCH\_DIR*
- *MSK\_IPAR\_MIO\_CONSTRUCT\_SOL*
- *MSK\_IPAR\_MIO\_CUT\_CLIQUE*
- *MSK\_IPAR\_MIO\_CUT\_CMIR*
- *MSK\_IPAR\_MIO\_CUT\_GMI*
- *MSK\_IPAR\_MIO\_CUT\_IMPLIED\_BOUND*
- *MSK\_IPAR\_MIO\_CUT\_KNAPSACK\_COVER*
- *MSK\_IPAR\_MIO\_CUT\_SELECTION\_LEVEL*
- *MSK\_DPAR\_MIO\_DISABLE\_TERM\_TIME*
- *MSK\_IPAR\_MIO\_HEURISTIC\_LEVEL*
- *MSK\_IPAR\_MIO\_MAX\_NUM\_BRANCHES*
- *MSK\_IPAR\_MIO\_MAX\_NUM\_RELAXS*
- *MSK\_IPAR\_MIO\_MAX\_NUM\_SOLUTIONS*
- *MSK\_DPAR\_MIO\_MAX\_TIME*
- *MSK\_DPAR\_MIO\_NEAR\_TOL\_ABS\_GAP*
- *MSK\_DPAR\_MIO\_NEAR\_TOL\_REL\_GAP*
- *MSK\_IPAR\_MIO\_NODE\_OPTIMIZER*
- *MSK\_IPAR\_MIO\_NODE\_SELECTION*
- *MSK\_IPAR\_MIO\_PERSPECTIVE\_REFORMULATE*
- *MSK\_IPAR\_MIO\_PROBING\_LEVEL*
- *MSK\_DPAR\_MIO\_REL\_GAP\_CONST*
- *MSK\_IPAR\_MIO\_RINS\_MAX\_NODES*
- *MSK\_IPAR\_MIO\_ROOT\_OPTIMIZER*
- *MSK\_IPAR\_MIO\_ROOT\_REPEAT\_PREOLVE\_LEVEL*
- *MSK\_DPAR\_MIO\_TOL\_ABS\_GAP*



- *MSK\_DPAR\_MIO\_TOL\_ABS\_RELAX\_INT*
- *MSK\_DPAR\_MIO\_TOL\_FEAS*
- *MSK\_DPAR\_MIO\_TOL\_REL\_DUAL\_BOUND\_IMPROVEMENT*
- *MSK\_DPAR\_MIO\_TOL\_REL\_GAP*
- *MSK\_IPAR\_MIO\_VB\_DETECTION\_LEVEL*

### 11.1.21 Simplex optimizer parameters.

- *MSK\_DPAR\_BASIS\_REL\_TOL\_S*
- *MSK\_IPAR\_BASIS\_SOLVE\_USE\_PLUS\_ONE*
- *MSK\_DPAR\_BASIS\_TOL\_S*
- *MSK\_DPAR\_BASIS\_TOL\_X*
- *MSK\_IPAR\_LOG\_SIM*
- *MSK\_IPAR\_LOG\_SIM\_FREQ*
- *MSK\_IPAR\_LOG\_SIM\_MINOR*
- *MSK\_IPAR\_SENSITIVITY\_OPTIMIZER*
- *MSK\_IPAR\_SIM\_BASIS\_FACTOR\_USE*
- *MSK\_IPAR\_SIM\_DEGEN*
- *MSK\_IPAR\_SIM\_DUAL\_PHASEONE\_METHOD*
- *MSK\_IPAR\_SIM\_EXPLOIT\_DUPVEC*
- *MSK\_IPAR\_SIM\_HOTSTART*
- *MSK\_IPAR\_SIM\_INTEGER*
- *MSK\_DPAR\_SIM\_LU\_TOL\_REL\_PIV*
- *MSK\_IPAR\_SIM\_MAX\_ITERATIONS*
- *MSK\_IPAR\_SIM\_MAX\_NUM\_SETBACKS*
- *MSK\_IPAR\_SIM\_NON\_SINGULAR*
- *MSK\_IPAR\_SIM\_PRIMAL\_PHASEONE\_METHOD*
- *MSK\_IPAR\_SIM\_REFACTOR\_FREQ*
- *MSK\_IPAR\_SIM\_REFORMULATION*
- *MSK\_IPAR\_SIM\_SAVE\_LU*
- *MSK\_IPAR\_SIM\_SCALING*
- *MSK\_IPAR\_SIM\_SCALING\_METHOD*
- *MSK\_IPAR\_SIM\_SOLVE\_FORM*
- *MSK\_IPAR\_SIM\_STABILITY\_PRIORITY*
- *MSK\_IPAR\_SIM\_SWITCH\_OPTIMIZER*
- *MSK\_DPAR\_SIMPLEX\_ABS\_TOL\_PIV*

### 11.1.22 Output information parameters.

- *MSK\_IPAR\_INFEAS\_REPORT\_LEVEL*
- *MSK\_IPAR\_LICENSE\_SUPPRESS\_EXPIRE\_WRNS*
- *MSK\_IPAR\_LOG*
- *MSK\_IPAR\_LOG\_BI*
- *MSK\_IPAR\_LOG\_BI\_FREQ*
- *MSK\_IPAR\_LOG\_CUT\_SECOND\_OPT*
- *MSK\_IPAR\_LOG\_EXPAND*
- *MSK\_IPAR\_LOG\_FACTOR*
- *MSK\_IPAR\_LOG\_FEAS\_REPAIR*
- *MSK\_IPAR\_LOG\_FILE*
- *MSK\_IPAR\_LOG\_HEAD*
- *MSK\_IPAR\_LOG\_INFEAS\_ANA*
- *MSK\_IPAR\_LOG\_INTPNT*
- *MSK\_IPAR\_LOG\_MIO*
- *MSK\_IPAR\_LOG\_MIO\_FREQ*
- *MSK\_IPAR\_LOG\_OPTIMIZER*
- *MSK\_IPAR\_LOG\_ORDER*
- *MSK\_IPAR\_LOG\_RESPONSE*
- *MSK\_IPAR\_LOG\_SENSITIVITY*
- *MSK\_IPAR\_LOG\_SENSITIVITY\_OPT*
- *MSK\_IPAR\_LOG\_SIM*
- *MSK\_IPAR\_LOG\_SIM\_FREQ*
- *MSK\_IPAR\_LOG\_SIM\_MINOR*
- *MSK\_IPAR\_LOG\_STORAGE*
- *MSK\_IPAR\_MAX\_NUM\_WARNINGS*

### 11.1.23 Solution input/output parameters.

- *MSK\_SPAR\_BAS\_SOL\_FILE\_NAME*
- *MSK\_IPAR\_INFEAS\_REPORT\_AUTO*
- *MSK\_SPAR\_INT\_SOL\_FILE\_NAME*
- *MSK\_SPAR\_ITR\_SOL\_FILE\_NAME*
- *MSK\_IPAR\_SOL\_FILTER\_KEEP\_BASIC*
- *MSK\_IPAR\_SOL\_FILTER\_KEEP\_RANGED*
- *MSK\_SPAR\_SOL\_FILTER\_XC\_LOW*
- *MSK\_SPAR\_SOL\_FILTER\_XC\_UPR*
- *MSK\_SPAR\_SOL\_FILTER\_XX\_LOW*
- *MSK\_SPAR\_SOL\_FILTER\_XX\_UPR*

- *MSK\_IPAR\_SOL\_READ\_NAME\_WIDTH*
- *MSK\_IPAR\_SOL\_READ\_WIDTH*
- *MSK\_IPAR\_WRITE\_BAS\_CONSTRAINTS*
- *MSK\_IPAR\_WRITE\_BAS\_HEAD*
- *MSK\_IPAR\_WRITE\_BAS\_VARIABLES*
- *MSK\_IPAR\_WRITE\_INT\_CONSTRAINTS*
- *MSK\_IPAR\_WRITE\_INT\_HEAD*
- *MSK\_IPAR\_WRITE\_INT\_VARIABLES*
- *MSK\_IPAR\_WRITE\_SOL\_BARVARIABLES*
- *MSK\_IPAR\_WRITE\_SOL\_CONSTRAINTS*
- *MSK\_IPAR\_WRITE\_SOL\_HEAD*
- *MSK\_IPAR\_WRITE\_SOL\_IGNORE\_INVALID\_NAMES*
- *MSK\_IPAR\_WRITE\_SOL\_VARIABLES*

## 11.2 Response codes

- *Termination codes*
- *Error codes*
- *Warning codes*

### 11.2.1 Termination Codes

MSK\_RES\_OK (0)

No error occurred.

MSK\_RES\_TRM\_INTERNAL (10030)

The optimizer terminated due to some internal reason. Please contact **MOSEK** support.

MSK\_RES\_TRM\_INTERNAL\_STOP (10031)

The optimizer terminated for internal reasons. Please contact **MOSEK** support.

MSK\_RES\_TRM\_MAX\_ITERATIONS (10000)

The optimizer terminated at the maximum number of iterations.

MSK\_RES\_TRM\_MAX\_NUM\_SETBACKS (10020)

The optimizer terminated as the maximum number of set-backs was reached. This indicates % serious numerical problems and a possibly badly formulated problem.

MSK\_RES\_TRM\_MAX\_TIME (10001)

The optimizer terminated at the maximum amount of time.

MSK\_RES\_TRM\_MIO\_NEAR\_ABS\_GAP (10004)

The mixed-integer optimizer terminated because the near optimal absolute gap tolerance was satisfied.

MSK\_RES\_TRM\_MIO\_NEAR\_REL\_GAP (10003)

The mixed-integer optimizer terminated because the near optimal relative gap tolerance was satisfied.

MSK\_RES\_TRM\_MIO\_NUM\_BRANCHES (10009)

The mixed-integer optimizer terminated as to the maximum number of branches was reached.

**MSK\_RES\_TRM\_MIO\_NUM\_RELAXS (10008)**

The mixed-integer optimizer terminated as the maximum number of relaxations was reached.

**MSK\_RES\_TRM\_NUM\_MAX\_NUM\_INT\_SOLUTIONS (10015)**

The mixed-integer optimizer terminated as the maximum number of feasible solutions was reached.

**MSK\_RES\_TRM\_NUMERICAL\_PROBLEM (10025)**

The optimizer terminated due to numerical problems.

**MSK\_RES\_TRM\_OBJECTIVE\_RANGE (10002)**

The optimizer terminated on the bound of the objective range.

**MSK\_RES\_TRM\_STALL (10006)**

The optimizer is terminated due to slow progress.

Stalling means that numerical problems prevent the optimizer from making reasonable progress and that it make no sense to continue. In many cases this happens if the problem is badly scaled or otherwise ill-conditioned. There is no guarantee that the solution will be (near) feasible or near optimal. However, often stalling happens near the optimum, and the returned solution may be of good quality. Therefore, it is recommended to check the status of then solution. If the solution near optimal the solution is most likely good enough for most practical purposes.

Please note that if a linear optimization problem is solved using the interior-point optimizer with basis identification turned on, the returned basic solution likely to have high accuracy, even though the optimizer stalled.

Some common causes of stalling are a) badly scaled models, b) near feasible or near infeasible problems and c) a non-convex problems. Case c) is only relevant for general non-linear problems. It is not possible in general for **MOSEK** to check if a specific problems is convex since such a check would be NP hard in itself. This implies that care should be taken when solving problems involving general user defined functions.

**MSK\_RES\_TRM\_USER\_CALLBACK (10007)**

The optimizer terminated due to the return of the user-defined call-back function.

## 11.2.2 Error Codes

**MSK\_RES\_ERR\_AD\_INVALID\_CODELIST (3102)**

The code list data was invalid.

**MSK\_RES\_ERR\_API\_ARRAY\_TOO\_SMALL (3001)**

An input array was too short.

**MSK\_RES\_ERR\_API\_CB\_CONNECT (3002)**

Failed to connect a callback object.

**MSK\_RES\_ERR\_API\_FATAL\_ERROR (3005)**

An internal error occurred in the API. Please report this problem.

**MSK\_RES\_ERR\_API\_INTERNAL (3999)**

An internal fatal error occurred in an interface function.

**MSK\_RES\_ERR\_ARG\_IS\_TOO\_LARGE (1227)**

The value of a argument is too small.

**MSK\_RES\_ERR\_ARG\_IS\_TOO\_SMALL (1226)**

The value of a argument is too small.

**MSK\_RES\_ERR\_ARGUMENT\_DIMENSION (1201)**

A function argument is of incorrect dimension.

**MSK\_RES\_ERR\_ARGUMENT\_IS\_TOO\_LARGE (5005)**

The value of a function argument is too large.

**MSK\_RES\_ERR\_ARGUMENT\_LENNEQ (1197)**

Incorrect length of arguments.

MSK\_RES\_ERR\_ARGUMENT\_PERM\_ARRAY (1299)  
An invalid permutation array is specified.

MSK\_RES\_ERR\_ARGUMENT\_TYPE (1198)  
Incorrect argument type.

MSK\_RES\_ERR\_BAR\_VAR\_DIM (3920)  
The dimension of a symmetric matrix variable has to be greater than 0.

MSK\_RES\_ERR\_BASIS (1266)  
An invalid basis is specified. Either too many or too few basis variables are specified.

MSK\_RES\_ERR\_BASIS\_FACTOR (1610)  
The factorization of the basis is invalid.

MSK\_RES\_ERR\_BASIS\_SINGULAR (1615)  
The basis is singular and hence cannot be factored.

MSK\_RES\_ERR\_BLANK\_NAME (1070)  
An all blank name has been specified.

MSK\_RES\_ERR\_CANNOT\_CLONE\_NL (2505)  
A task with a nonlinear function call-back cannot be cloned.

MSK\_RES\_ERR\_CANNOT\_HANDLE\_NL (2506)  
A function cannot handle a task with nonlinear function call-backs.

MSK\_RES\_ERR\_CBF\_DUPLICATE\_ACOORD (7116)  
Duplicate index in ACOORD.

MSK\_RES\_ERR\_CBF\_DUPLICATE\_BCOORD (7115)  
Duplicate index in BCOORD.

MSK\_RES\_ERR\_CBF\_DUPLICATE\_CON (7108)  
Duplicate CON keyword.

MSK\_RES\_ERR\_CBF\_DUPLICATE\_INT (7110)  
Duplicate INT keyword.

MSK\_RES\_ERR\_CBF\_DUPLICATE\_OBJ (7107)  
Duplicate OBJ keyword.

MSK\_RES\_ERR\_CBF\_DUPLICATE\_OBJCOORD (7114)  
Duplicate index in OBJCOORD.

MSK\_RES\_ERR\_CBF\_DUPLICATE\_VAR (7109)  
Duplicate VAR keyword.

MSK\_RES\_ERR\_CBF\_INVALID\_CON\_TYPE (7112)  
Invalid constraint type.

MSK\_RES\_ERR\_CBF\_INVALID\_DOMAIN\_DIMENSION (7113)  
Invalid domain dimension.

MSK\_RES\_ERR\_CBF\_INVALID\_INT\_INDEX (7121)  
Invalid INT index.

MSK\_RES\_ERR\_CBF\_INVALID\_VAR\_TYPE (7111)  
Invalid variable type.

MSK\_RES\_ERR\_CBF\_NO\_VARIABLES (7102)  
No variables are specified.

MSK\_RES\_ERR\_CBF\_NO\_VERSION\_SPECIFIED (7105)  
No version specified.

MSK\_RES\_ERR\_CBF\_OBJ\_SENSE (7101)  
An invalid objective sense is specified.

MSK\_RES\_ERR\_CBF\_PARSE (7100)

An error occurred while parsing an CBF file.

MSK\_RES\_ERR\_CBF\_SYNTAX (7106)

Invalid syntax.

MSK\_RES\_ERR\_CBF\_TOO\_FEW\_CONSTRAINTS (7118)

Too few constraints defined.

MSK\_RES\_ERR\_CBF\_TOO\_FEW\_INTS (7119)

Too few ints are specified.

MSK\_RES\_ERR\_CBF\_TOO\_FEW\_VARIABLES (7117)

Too few variables defined.

MSK\_RES\_ERR\_CBF\_TOO\_MANY\_CONSTRAINTS (7103)

Too many constraints specified.

MSK\_RES\_ERR\_CBF\_TOO\_MANY\_INTS (7120)

Too many ints are specified.

MSK\_RES\_ERR\_CBF\_TOO\_MANY\_VARIABLES (7104)

Too many variables specified.

MSK\_RES\_ERR\_CBF\_UNSUPPORTED (7122)

Unsupported feature is present.

MSK\_RES\_ERR\_CON\_Q\_NOT\_NSD (1294)

The quadratic constraint matrix is not negative semidefinite as expected for a constraint with finite lower bound. This results in a nonconvex problem. The parameter *MSK\_DPAR\_CHECK\_CONVEXITY\_REL\_TOL* can be used to relax the convexity check.

MSK\_RES\_ERR\_CON\_Q\_NOT\_PSD (1293)

The quadratic constraint matrix is not positive semidefinite as expected for a constraint with finite upper bound. This results in a nonconvex problem. The parameter *MSK\_DPAR\_CHECK\_CONVEXITY\_REL\_TOL* can be used to relax the convexity check.

MSK\_RES\_ERR\_CONE\_INDEX (1300)

An index of a non-existing cone has been specified.

MSK\_RES\_ERR\_CONE\_OVERLAP (1302)

One or more of the variables in the cone to be added is already member of another cone. Now assume the variable is  $x_j$  then add a new variable say  $x_k$  and the constraint

$$x_j = x_k$$

and then let  $x_k$  be member of the cone to be appended.

MSK\_RES\_ERR\_CONE\_OVERLAP\_APPEND (1307)

The cone to be appended has one variable which is already member of another cone.

MSK\_RES\_ERR\_CONE\_REP\_VAR (1303)

A variable is included multiple times in the cone.

MSK\_RES\_ERR\_CONE\_SIZE (1301)

A cone with too few members is specified.

MSK\_RES\_ERR\_CONE\_TYPE (1305)

Invalid cone type specified.

MSK\_RES\_ERR\_CONE\_TYPE\_STR (1306)

Invalid cone type specified.

MSK\_RES\_ERR\_DATA\_FILE\_EXT (1055)

The data file format cannot be determined from the file name.

MSK\_RES\_ERR\_DUP\_NAME (1071)

The same name was used multiple times for the same problem item type.

- MSK\_RES\_ERR\_DUPLICATE\_AIJ (1385)**  
An element in the  $A$  matrix is specified twice.
- MSK\_RES\_ERR\_DUPLICATE\_BARVARIABLE\_NAMES (4502)**  
Two barvariable names are identical.
- MSK\_RES\_ERR\_DUPLICATE\_CONE\_NAMES (4503)**  
Two cone names are identical.
- MSK\_RES\_ERR\_DUPLICATE\_CONSTRAINT\_NAMES (4500)**  
Two constraint names are identical.
- MSK\_RES\_ERR\_DUPLICATE\_VARIABLE\_NAMES (4501)**  
Two variable names are identical.
- MSK\_RES\_ERR\_END\_OF\_FILE (1059)**  
End of file reached.
- MSK\_RES\_ERR\_FACTOR (1650)**  
An error occurred while factorizing a matrix.
- MSK\_RES\_ERR\_FEASREPAIR\_CANNOT\_RELAX (1700)**  
An optimization problem cannot be relaxed. This is the case e.g. for general nonlinear optimization problems.
- MSK\_RES\_ERR\_FEASREPAIR\_INCONSISTENT\_BOUND (1702)**  
The upper bound is less than the lower bound for a variable or a constraint. Please correct this before running the feasibility repair.
- MSK\_RES\_ERR\_FEASREPAIR\_SOLVING\_RELAXED (1701)**  
The relaxed problem could not be solved to optimality. Please consult the log file for further details.
- MSK\_RES\_ERR\_FILE\_LICENSE (1007)**  
Invalid license file.
- MSK\_RES\_ERR\_FILE\_OPEN (1052)**  
Error while opening a file.
- MSK\_RES\_ERR\_FILE\_READ (1053)**  
File read error.
- MSK\_RES\_ERR\_FILE\_WRITE (1054)**  
File write error.
- MSK\_RES\_ERR\_FIRST (1261)**  
Invalid `first`.
- MSK\_RES\_ERR\_FIRSTI (1285)**  
Invalid `firsti`.
- MSK\_RES\_ERR\_FIRSTJ (1287)**  
Invalid `firstj`.
- MSK\_RES\_ERR\_FIXED\_BOUND\_VALUES (1425)**  
A fixed constraint/variable has been specified using the bound keys but the numerical value of the lower and upper bound is different.
- MSK\_RES\_ERR\_FLEXLM (1014)**  
The FLEXlm license manager reported an error.
- MSK\_RES\_ERR\_GLOBAL\_INV\_CONIC\_PROBLEM (1503)**  
The global optimizer can only be applied to problems without semidefinite variables.
- MSK\_RES\_ERR\_HUGE\_AIJ (1380)**  
A numerically huge value is specified for an  $a_{i,j}$  element in  $A$ . The parameter `MSK_DPAR_DATA_TOL_AIJ_HUGE` controls when an  $a_{i,j}$  is considered huge.
- MSK\_RES\_ERR\_HUGE\_C (1375)**  
A huge value in absolute size is specified for one  $c_j$ .

**MSK\_RES\_ERR\_IDENTICAL\_TASKS (3101)**

Some tasks related to this function call were identical. Unique tasks were expected.

**MSK\_RES\_ERR\_IN\_ARGUMENT (1200)**

A function argument is incorrect.

**MSK\_RES\_ERR\_INDEX (1235)**

An index is out of range.

**MSK\_RES\_ERR\_INDEX\_ARR\_IS\_TOO\_LARGE (1222)**

An index in an array argument is too large.

**MSK\_RES\_ERR\_INDEX\_ARR\_IS\_TOO\_SMALL (1221)**

An index in an array argument is too small.

**MSK\_RES\_ERR\_INDEX\_IS\_TOO\_LARGE (1204)**

An index in an argument is too large.

**MSK\_RES\_ERR\_INDEX\_IS\_TOO\_SMALL (1203)**

An index in an argument is too small.

**MSK\_RES\_ERR\_INF\_DOU\_INDEX (1219)**

A double information index is out of range for the specified type.

**MSK\_RES\_ERR\_INF\_DOU\_NAME (1230)**

A double information name is invalid.

**MSK\_RES\_ERR\_INF\_INT\_INDEX (1220)**

An integer information index is out of range for the specified type.

**MSK\_RES\_ERR\_INF\_INT\_NAME (1231)**

An integer information name is invalid.

**MSK\_RES\_ERR\_INF\_LINT\_INDEX (1225)**

A long integer information index is out of range for the specified type.

**MSK\_RES\_ERR\_INF\_LINT\_NAME (1234)**

A long integer information name is invalid.

**MSK\_RES\_ERR\_INF\_TYPE (1232)**

The information type is invalid.

**MSK\_RES\_ERR\_INFEAS\_UNDEFINED (3910)**

The requested value is not defined for this solution type.

**MSK\_RES\_ERR\_INFINITE\_BOUND (1400)**

A numerically huge bound value is specified.

**MSK\_RES\_ERR\_INT64\_TO\_INT32\_CAST (3800)**

An 32 bit integer could not cast to a 64 bit integer.

**MSK\_RES\_ERR\_INTERNAL (3000)**

An internal error occurred. Please report this problem.

**MSK\_RES\_ERR\_INTERNAL\_TEST\_FAILED (3500)**

An internal unit test function failed.

**MSK\_RES\_ERR\_INV\_APTRE (1253)**

`aptre[j]` is strictly smaller than `aptrb[j]` for some `j`.

**MSK\_RES\_ERR\_INV\_BK (1255)**

Invalid bound key.

**MSK\_RES\_ERR\_INV\_BKC (1256)**

Invalid bound key is specified for a constraint.

**MSK\_RES\_ERR\_INV\_BKX (1257)**

An invalid bound key is specified for a variable.



MSK\_RES\_ERR\_INV\_CONE\_TYPE (1272)  
Invalid cone type code is encountered.

MSK\_RES\_ERR\_INV\_CONE\_TYPE\_STR (1271)  
Invalid cone type string encountered.

MSK\_RES\_ERR\_INV\_MARKI (2501)  
Invalid value in marki.

MSK\_RES\_ERR\_INV\_MARKJ (2502)  
Invalid value in markj.

MSK\_RES\_ERR\_INV\_NAME\_ITEM (1280)  
An invalid name item code is used.

MSK\_RES\_ERR\_INV\_NUMI (2503)  
Invalid numi.

MSK\_RES\_ERR\_INV\_NUMJ (2504)  
Invalid numj.

MSK\_RES\_ERR\_INV\_OPTIMIZER (1550)  
An invalid optimizer has been chosen for the problem. This means that the simplex or the conic optimizer is chosen to optimize a nonlinear problem.

MSK\_RES\_ERR\_INV\_PROBLEM (1500)  
Invalid problem type. Probably a nonconvex problem has been specified.

MSK\_RES\_ERR\_INV\_QCON\_SUBI (1405)  
Invalid value in qcsubi.

MSK\_RES\_ERR\_INV\_QCON\_SUBJ (1406)  
Invalid value in qcsubj.

MSK\_RES\_ERR\_INV\_QCON\_SUBK (1404)  
Invalid value in qcsubk.

MSK\_RES\_ERR\_INV\_QCON\_VAL (1407)  
Invalid value in qcval.

MSK\_RES\_ERR\_INV\_QOBJ\_SUBI (1401)  
Invalid value in qosubi.

MSK\_RES\_ERR\_INV\_QOBJ\_SUBJ (1402)  
Invalid value in qosubj.

MSK\_RES\_ERR\_INV\_QOBJ\_VAL (1403)  
Invalid value in qoval.

MSK\_RES\_ERR\_INV\_SK (1270)  
Invalid status key code.

MSK\_RES\_ERR\_INV\_SK\_STR (1269)  
Invalid status key string encountered.

MSK\_RES\_ERR\_INV\_SKC (1267)  
Invalid value in skc.

MSK\_RES\_ERR\_INV\_SKN (1274)  
Invalid value in skn.

MSK\_RES\_ERR\_INV\_SKX (1268)  
Invalid value in skx.

MSK\_RES\_ERR\_INV\_VAR\_TYPE (1258)  
An invalid variable type is specified for a variable.

MSK\_RES\_ERR\_INVALID\_ACCMODE (2520)  
An invalid access mode is specified.

MSK\_RES\_ERR\_INVALID\_AIJ (1473)

$a_{i,j}$  contains an invalid floating point value, i.e. a NaN or an infinite value.

MSK\_RES\_ERR\_INVALID\_AMPL\_STUB (3700)

Invalid AMPL stub.

MSK\_RES\_ERR\_INVALID\_BARVAR\_NAME (1079)

An invalid symmetric matrix variable name is used.

MSK\_RES\_ERR\_INVALID\_COMPRESSION (1800)

Invalid compression type.

MSK\_RES\_ERR\_INVALID\_CON\_NAME (1076)

An invalid constraint name is used.

MSK\_RES\_ERR\_INVALID\_CONE\_NAME (1078)

An invalid cone name is used.

MSK\_RES\_ERR\_INVALID\_FILE\_FORMAT\_FOR\_CONES (4005)

The file format does not support a problem with conic constraints.

MSK\_RES\_ERR\_INVALID\_FILE\_FORMAT\_FOR\_GENERAL\_NL (4010)

The file format does not support a problem with general nonlinear terms.

MSK\_RES\_ERR\_INVALID\_FILE\_FORMAT\_FOR\_SYM\_MAT (4000)

The file format does not support a problem with symmetric matrix variables.

MSK\_RES\_ERR\_INVALID\_FILE\_NAME (1056)

An invalid file name has been specified.

MSK\_RES\_ERR\_INVALID\_FORMAT\_TYPE (1283)

Invalid format type.

MSK\_RES\_ERR\_INVALID\_IDX (1246)

A specified index is invalid.

MSK\_RES\_ERR\_INVALID\_IOMODE (1801)

Invalid io mode.

MSK\_RES\_ERR\_INVALID\_MAX\_NUM (1247)

A specified index is invalid.

MSK\_RES\_ERR\_INVALID\_NAME\_IN\_SOL\_FILE (1170)

An invalid name occurred in a solution file.

MSK\_RES\_ERR\_INVALID\_OBJ\_NAME (1075)

An invalid objective name is specified.

MSK\_RES\_ERR\_INVALID\_OBJECTIVE\_SENSE (1445)

An invalid objective sense is specified.

MSK\_RES\_ERR\_INVALID\_PROBLEM\_TYPE (6000)

An invalid problem type.

MSK\_RES\_ERR\_INVALID\_SOL\_FILE\_NAME (1057)

An invalid file name has been specified.

MSK\_RES\_ERR\_INVALID\_STREAM (1062)

An invalid stream is referenced.

MSK\_RES\_ERR\_INVALID\_SURPLUS (1275)

Invalid surplus.

MSK\_RES\_ERR\_INVALID\_SYM\_MAT\_DIM (3950)

A sparse symmetric matrix of invalid dimension is specified.

MSK\_RES\_ERR\_INVALID\_TASK (1064)

The `task` is invalid.

MSK\_RES\_ERR\_INVALID\_UTF8 (2900)  
An invalid UTF8 string is encountered.

MSK\_RES\_ERR\_INVALID\_VAR\_NAME (1077)  
An invalid variable name is used.

MSK\_RES\_ERR\_INVALID\_WCHAR (2901)  
An invalid `wchar` string is encountered.

MSK\_RES\_ERR\_INVALID\_WHICHSQL (1228)  
`whichsol` is invalid.

MSK\_RES\_ERR\_JSON\_DATA (1179)  
Inconsistent data in JSON Task file

MSK\_RES\_ERR\_JSON\_FORMAT (1178)  
Error in an JSON Task file

MSK\_RES\_ERR\_JSON\_MISSING\_DATA (1180)  
Missing data section in JSON task file.

MSK\_RES\_ERR\_JSON\_NUMBER\_OVERFLOW (1177)  
Invalid number entry - wrong type or value overflow.

MSK\_RES\_ERR\_JSON\_STRING (1176)  
Error in JSON string.

MSK\_RES\_ERR\_JSON\_SYNTAX (1175)  
Syntax error in an JSON data

MSK\_RES\_ERR\_LAST (1262)  
Invalid index `last`. A given index was out of expected range.

MSK\_RES\_ERR\_LASTI (1286)  
Invalid `lasti`.

MSK\_RES\_ERR\_LASTJ (1288)  
Invalid `lastj`.

MSK\_RES\_ERR\_LAU\_ARG\_K (7012)  
Invalid argument `k`.

MSK\_RES\_ERR\_LAU\_ARG\_M (7010)  
Invalid argument `m`.

MSK\_RES\_ERR\_LAU\_ARG\_N (7011)  
Invalid argument `n`.

MSK\_RES\_ERR\_LAU\_ARG\_TRANS (7018)  
Invalid argument `trans`.

MSK\_RES\_ERR\_LAU\_ARG\_TRANSA (7015)  
Invalid argument `transa`.

MSK\_RES\_ERR\_LAU\_ARG\_TRANSB (7016)  
Invalid argument `transb`.

MSK\_RES\_ERR\_LAU\_ARG\_UPLO (7017)  
Invalid argument `uplo`.

MSK\_RES\_ERR\_LAU\_INVALID\_LOWER\_TRIANGULAR\_MATRIX (7002)  
An invalid lower triangular matrix.

MSK\_RES\_ERR\_LAU\_INVALID\_SPARSE\_SYMMETRIC\_MATRIX (7019)  
An invalid sparse symmetric matrix is specified. Note only the lower triangular part with no duplicates is specified.

MSK\_RES\_ERR\_LAU\_NOT\_POSITIVE\_DEFINITE (7001)  
A matrix is not positive definite.

MSK\_RES\_ERR\_LAU\_SINGULAR\_MATRIX (7000)

A matrix is singular.

MSK\_RES\_ERR\_LAU\_UNKNOWN (7005)

An unknown error.

MSK\_RES\_ERR\_LICENSE (1000)

Invalid license.

MSK\_RES\_ERR\_LICENSE\_CANNOT\_ALLOCATE (1020)

The license system cannot allocate the memory required.

MSK\_RES\_ERR\_LICENSE\_CANNOT\_CONNECT (1021)

**MOSEK** cannot connect to the license server. Most likely the license server is not up and running.

MSK\_RES\_ERR\_LICENSE\_EXPIRED (1001)

The license has expired.

MSK\_RES\_ERR\_LICENSE\_FEATURE (1018)

A requested feature is not available in the license file(s). Most likely due to an incorrect license system setup.

MSK\_RES\_ERR\_LICENSE\_INVALID\_HOSTID (1025)

The host ID specified in the license file does not match the host ID of the computer.

MSK\_RES\_ERR\_LICENSE\_MAX (1016)

Maximum number of licenses is reached.

MSK\_RES\_ERR\_LICENSE\_MOSEKLM\_DAEMON (1017)

The MOSEKLM license manager daemon is not up and running.

MSK\_RES\_ERR\_LICENSE\_NO\_SERVER\_LINE (1028)

There is no **SERVER** line in the license file. All non-zero license count features need at least one **SERVER** line.

MSK\_RES\_ERR\_LICENSE\_NO\_SERVER\_SUPPORT (1027)

The license server does not support the requested feature. Possible reasons for this error include:

- The feature has expired.
- The feature's start date is later than today's date.
- The version requested is higher than feature's the highest supported version.
- A corrupted license file.

Try restarting the license and inspect the license server debug file, usually called `lmgrd.log`.

MSK\_RES\_ERR\_LICENSE\_SERVER (1015)

The license server is not responding.

MSK\_RES\_ERR\_LICENSE\_SERVER\_VERSION (1026)

The version specified in the checkout request is greater than the highest version number the daemon supports.

MSK\_RES\_ERR\_LICENSE\_VERSION (1002)

The license is valid for another version of **MOSEK**.

MSK\_RES\_ERR\_LINK\_FILE\_DLL (1040)

A file cannot be linked to a stream in the DLL version.

MSK\_RES\_ERR\_LIVING\_TASKS (1066)

All tasks associated with an environment must be deleted before the environment is deleted. There are still some undeleted tasks.

MSK\_RES\_ERR\_LOWER\_BOUND\_IS\_A\_NAN (1390)

The lower bound specified is not a number (nan).

MSK\_RES\_ERR\_LP\_DUP\_SLACK\_NAME (1152)

The name of the slack variable added to a ranged constraint already exists.

**MSK\_RES\_ERR\_LP\_EMPTY (1151)**  
The problem cannot be written to an LP formatted file.

**MSK\_RES\_ERR\_LP\_FILE\_FORMAT (1157)**  
Syntax error in an LP file.

**MSK\_RES\_ERR\_LP\_FORMAT (1160)**  
Syntax error in an LP file.

**MSK\_RES\_ERR\_LP\_FREE\_CONSTRAINT (1155)**  
Free constraints cannot be written in LP file format.

**MSK\_RES\_ERR\_LP\_INCOMPATIBLE (1150)**  
The problem cannot be written to an LP formatted file.

**MSK\_RES\_ERR\_LP\_INVALID\_CON\_NAME (1171)**  
A constraint name is invalid when used in an LP formatted file.

**MSK\_RES\_ERR\_LP\_INVALID\_VAR\_NAME (1154)**  
A variable name is invalid when used in an LP formatted file.

**MSK\_RES\_ERR\_LP\_WRITE\_CONIC\_PROBLEM (1163)**  
The problem contains cones that cannot be written to an LP formatted file.

**MSK\_RES\_ERR\_LP\_WRITE\_GECO\_PROBLEM (1164)**  
The problem contains general convex terms that cannot be written to an LP formatted file.

**MSK\_RES\_ERR\_LU\_MAX\_NUM\_TRIES (2800)**  
Could not compute the LU factors of the matrix within the maximum number of allowed tries.

**MSK\_RES\_ERR\_MAX\_LEN\_IS\_TOO\_SMALL (1289)**  
An maximum length that is too small has been specified.

**MSK\_RES\_ERR\_MAXNUMBARVAR (1242)**  
The maximum number of semidefinite variables specified is smaller than the number of semidefinite variables in the task.

**MSK\_RES\_ERR\_MAXNUMCON (1240)**  
The maximum number of constraints specified is smaller than the number of constraints in the task.

**MSK\_RES\_ERR\_MAXNUMCONE (1304)**  
The value specified for `maxnumcone` is too small.

**MSK\_RES\_ERR\_MAXNUMQNZ (1243)**  
The maximum number of non-zeros specified for the  $Q$  matrices is smaller than the number of non-zeros in the current  $Q$  matrices.

**MSK\_RES\_ERR\_MAXNUMVAR (1241)**  
The maximum number of variables specified is smaller than the number of variables in the task.

**MSK\_RES\_ERR\_MIO\_INTERNAL (5010)**  
A fatal error occurred in the mixed integer optimizer. Please contact **MOSEK** support.

**MSK\_RES\_ERR\_MIO\_INVALID\_NODE\_OPTIMIZER (7131)**  
An invalid node optimizer was selected for the problem type.

**MSK\_RES\_ERR\_MIO\_INVALID\_ROOT\_OPTIMIZER (7130)**  
An invalid root optimizer was selected for the problem type.

**MSK\_RES\_ERR\_MIO\_NO\_OPTIMIZER (1551)**  
No optimizer is available for the current class of integer optimization problems.

**MSK\_RES\_ERR\_MIO\_NOT\_LOADED (1553)**  
The mixed-integer optimizer is not loaded.

**MSK\_RES\_ERR\_MISSING\_LICENSE\_FILE (1008)**  
**MOSEK** cannot license file or a token server. See the **MOSEK** installation manual for details.

MSK\_RES\_ERR\_MIXED\_CONIC\_AND\_NL (1501)

The problem contains nonlinear terms conic constraints. The requested operation cannot be applied to this type of problem.

MSK\_RES\_ERR\_MPS\_CONE\_OVERLAP (1118)

A variable is specified to be a member of several cones.

MSK\_RES\_ERR\_MPS\_CONE\_REPEAT (1119)

A variable is repeated within the CSECTION.

MSK\_RES\_ERR\_MPS\_CONE\_TYPE (1117)

Invalid cone type specified in a CSECTION.

MSK\_RES\_ERR\_MPS\_DUPLICATE\_Q\_ELEMENT (1121)

Duplicate elements is specified in a  $Q$  matrix.

MSK\_RES\_ERR\_MPS\_FILE (1100)

An error occurred while reading an MPS file.

MSK\_RES\_ERR\_MPS\_INV\_BOUND\_KEY (1108)

An invalid bound key occurred in an MPS file.

MSK\_RES\_ERR\_MPS\_INV\_CON\_KEY (1107)

An invalid constraint key occurred in an MPS file.

MSK\_RES\_ERR\_MPS\_INV\_FIELD (1101)

A field in the MPS file is invalid. Probably it is too wide.

MSK\_RES\_ERR\_MPS\_INV\_MARKER (1102)

An invalid marker has been specified in the MPS file.

MSK\_RES\_ERR\_MPS\_INV\_SEC\_NAME (1109)

An invalid section name occurred in an MPS file.

MSK\_RES\_ERR\_MPS\_INV\_SEC\_ORDER (1115)

The sections in the MPS data file are not in the correct order.

MSK\_RES\_ERR\_MPS\_INVALID\_OBJ\_NAME (1128)

An invalid objective name is specified.

MSK\_RES\_ERR\_MPS\_INVALID\_OBJSENSE (1122)

An invalid objective sense is specified.

MSK\_RES\_ERR\_MPS\_MUL\_CON\_NAME (1112)

A constraint name was specified multiple times in the ROWS section.

MSK\_RES\_ERR\_MPS\_MUL\_CSEC (1116)

Multiple CSECTIONs are given the same name.

MSK\_RES\_ERR\_MPS\_MUL\_QOBJ (1114)

The  $Q$  term in the objective is specified multiple times in the MPS data file.

MSK\_RES\_ERR\_MPS\_MUL\_QSEC (1113)

Multiple QSECTIONs are specified for a constraint in the MPS data file.

MSK\_RES\_ERR\_MPS\_NO\_OBJECTIVE (1110)

No objective is defined in an MPS file.

MSK\_RES\_ERR\_MPS\_NON\_SYMMETRIC\_Q (1120)

A non symmetric matrice has been speciefied.

MSK\_RES\_ERR\_MPS\_NULL\_CON\_NAME (1103)

An empty constraint name is used in an MPS file.

MSK\_RES\_ERR\_MPS\_NULL\_VAR\_NAME (1104)

An empty variable name is used in an MPS file.

**MSK\_RES\_ERR\_MPS\_SPLITTED\_VAR (1111)**

All elements in a column of the  $A$  matrix must be specified consecutively. Hence, it is illegal to specify non-zero elements in  $A$  for variable 1, then for variable 2 and then variable 1 again.

**MSK\_RES\_ERR\_MPS\_TAB\_IN\_FIELD2 (1125)**

A tab char occurred in field 2.

**MSK\_RES\_ERR\_MPS\_TAB\_IN\_FIELD3 (1126)**

A tab char occurred in field 3.

**MSK\_RES\_ERR\_MPS\_TAB\_IN\_FIELD5 (1127)**

A tab char occurred in field 5.

**MSK\_RES\_ERR\_MPS\_UNDEF\_CON\_NAME (1105)**

An undefined constraint name occurred in an MPS file.

**MSK\_RES\_ERR\_MPS\_UNDEF\_VAR\_NAME (1106)**

An undefined variable name occurred in an MPS file.

**MSK\_RES\_ERR\_MUL\_A\_ELEMENT (1254)**

An element in  $A$  is defined multiple times.

**MSK\_RES\_ERR\_NAME\_IS\_NULL (1760)**

The name buffer is a NULL pointer.

**MSK\_RES\_ERR\_NAME\_MAX\_LEN (1750)**

A name is longer than the buffer that is supposed to hold it.

**MSK\_RES\_ERR\_NAN\_IN\_BLC (1461)**

$l^c$  contains an invalid floating point value, i.e. a NaN.

**MSK\_RES\_ERR\_NAN\_IN\_BLX (1471)**

$l^x$  contains an invalid floating point value, i.e. a NaN.

**MSK\_RES\_ERR\_NAN\_IN\_BUC (1462)**

$u^c$  contains an invalid floating point value, i.e. a NaN.

**MSK\_RES\_ERR\_NAN\_IN\_BUX (1472)**

$u^x$  contains an invalid floating point value, i.e. a NaN.

**MSK\_RES\_ERR\_NAN\_IN\_C (1470)**

$c$  contains an invalid floating point value, i.e. a NaN.

**MSK\_RES\_ERR\_NAN\_IN\_DOUBLE\_DATA (1450)**

An invalid floating point value was used in some double data.

**MSK\_RES\_ERR\_NEGATIVE\_APPEND (1264)**

Cannot append a negative number.

**MSK\_RES\_ERR\_NEGATIVE\_SURPLUS (1263)**

Negative surplus.

**MSK\_RES\_ERR\_NEWER\_DLL (1036)**

The dynamic link library is newer than the specified version.

**MSK\_RES\_ERR\_NO\_BARS\_FOR\_SOLUTION (3916)**

There is no  $\bar{s}$  available for the solution specified. In particular note there are no  $\bar{s}$  defined for the basic and integer solutions.

**MSK\_RES\_ERR\_NO\_BARX\_FOR\_SOLUTION (3915)**

There is no  $\bar{X}$  available for the solution specified. In particular note there are no  $\bar{X}$  defined for the basic and integer solutions.

**MSK\_RES\_ERR\_NO\_BASIS\_SOL (1600)**

No basic solution is defined.

**MSK\_RES\_ERR\_NO\_DUAL\_FOR\_ITG\_SOL (2950)**

No dual information is available for the integer solution.

MSK\_RES\_ERR\_NO\_DUAL\_INFEAS\_CER (2001)

A certificate of infeasibility is not available.

MSK\_RES\_ERR\_NO\_INIT\_ENV (1063)

`env` is not initialized.

MSK\_RES\_ERR\_NO\_OPTIMIZER\_VAR\_TYPE (1552)

No optimizer is available for this class of optimization problems.

MSK\_RES\_ERR\_NO\_PRIMAL\_INFEAS\_CER (2000)

A certificate of primal infeasibility is not available.

MSK\_RES\_ERR\_NO\_SNX\_FOR\_BAS\_SOL (2953)

$s_n^x$  is not available for the basis solution.

MSK\_RES\_ERR\_NO\_SOLUTION\_IN\_CALLBACK (2500)

The required solution is not available.

MSK\_RES\_ERR\_NON\_UNIQUE\_ARRAY (5000)

An array does not contain unique elements.

MSK\_RES\_ERR\_NONCONVEX (1291)

The optimization problem is nonconvex.

MSK\_RES\_ERR\_NONLINEAR\_EQUALITY (1290)

The model contains a nonlinear equality which defines a nonconvex set.

MSK\_RES\_ERR\_NONLINEAR\_FUNCTIONS\_NOT\_ALLOWED (1428)

An operation that is invalid for problems with nonlinear functions defined has been attempted.

MSK\_RES\_ERR\_NONLINEAR\_RANGED (1292)

Nonlinear constraints with finite lower and upper bound always define a nonconvex feasible set.

MSK\_RES\_ERR\_NR\_ARGUMENTS (1199)

Incorrect number of function arguments.

MSK\_RES\_ERR\_NULL\_ENV (1060)

`env` is a NULL pointer.

MSK\_RES\_ERR\_NULL\_POINTER (1065)

An argument to a function is unexpectedly a NULL pointer.

MSK\_RES\_ERR\_NULL\_TASK (1061)

`task` is a NULL pointer.

MSK\_RES\_ERR\_NUMCONLIM (1250)

Maximum number of constraints limit is exceeded.

MSK\_RES\_ERR\_NUMVARLIM (1251)

Maximum number of variables limit is exceeded.

MSK\_RES\_ERR\_OBJ\_Q\_NOT\_NSD (1296)

The quadratic coefficient matrix in the objective is not negative semidefinite as expected for a maximization problem. The parameter `MSK_DPAR_CHECK_CONVEXITY_REL_TOL` can be used to relax the convexity check.

MSK\_RES\_ERR\_OBJ\_Q\_NOT\_PSD (1295)

The quadratic coefficient matrix in the objective is not positive semidefinite as expected for a minimization problem. The parameter `MSK_DPAR_CHECK_CONVEXITY_REL_TOL` can be used to relax the convexity check.

MSK\_RES\_ERR\_OBJECTIVE\_RANGE (1260)

Empty objective range.

MSK\_RES\_ERR\_OLDER\_DLL (1035)

The dynamic link library is older than the specified version.

MSK\_RES\_ERR\_OPEN\_DL (1030)

A dynamic link library could not be opened.



- MSK\_RES\_ERR\_OPF\_FORMAT (1168)  
Syntax error in an OPF file
- MSK\_RES\_ERR\_OPF\_NEW\_VARIABLE (1169)  
Introducing new variables is now allowed. When a [variables] section is present, it is not allowed to introduce new variables later in the problem.
- MSK\_RES\_ERR\_OPF\_PREMATURE\_EOF (1172)  
Premature end of file in an OPF file.
- MSK\_RES\_ERR\_OPTIMIZER\_LICENSE (1013)  
The optimizer required is not licensed.
- MSK\_RES\_ERR\_OVERFLOW (1590)  
A computation produced an overflow i.e. a very large number.
- MSK\_RES\_ERR\_PARAM\_INDEX (1210)  
Parameter index is out of range.
- MSK\_RES\_ERR\_PARAM\_IS\_TOO\_LARGE (1215)  
The parameter value is too large.
- MSK\_RES\_ERR\_PARAM\_IS\_TOO\_SMALL (1216)  
The parameter value is too small.
- MSK\_RES\_ERR\_PARAM\_NAME (1205)  
The parameter name is not correct.
- MSK\_RES\_ERR\_PARAM\_NAME\_DOUB (1206)  
The parameter name is not correct for a double parameter.
- MSK\_RES\_ERR\_PARAM\_NAME\_INT (1207)  
The parameter name is not correct for an integer parameter.
- MSK\_RES\_ERR\_PARAM\_NAME\_STR (1208)  
The parameter name is not correct for a string parameter.
- MSK\_RES\_ERR\_PARAM\_TYPE (1218)  
The parameter type is invalid.
- MSK\_RES\_ERR\_PARAM\_VALUE\_STR (1217)  
The parameter value string is incorrect.
- MSK\_RES\_ERR\_PLATFORM\_NOT\_LICENSED (1019)  
A requested license feature is not available for the required platform.
- MSK\_RES\_ERR\_POSTSOLVE (1580)  
An error occurred during the postsolve. Please contact **MOSEK** support.
- MSK\_RES\_ERR\_PROBLEM\_ITEM (1281)  
An invalid problem is used.
- MSK\_RES\_ERR\_PROB\_LICENSE (1006)  
The software is not licensed to solve the problem.
- MSK\_RES\_ERR\_QCON\_SUBI\_TOO\_LARGE (1409)  
Invalid value in qconsubi.
- MSK\_RES\_ERR\_QCON\_SUBI\_TOO\_SMALL (1408)  
Invalid value in qconsubi.
- MSK\_RES\_ERR\_QCON\_UPPER\_TRIANGLE (1417)  
An element in the upper triangle of a  $Q^k$  is specified. Only elements in the lower triangle should be specified.
- MSK\_RES\_ERR\_QOBJ\_UPPER\_TRIANGLE (1415)  
An element in the upper triangle of  $Q^o$  is specified. Only elements in the lower triangle should be specified.

MSK\_RES\_ERR\_READ\_FORMAT (1090)

The specified format cannot be read.

MSK\_RES\_ERR\_READ\_LP\_MISSING\_END\_TAG (1159)

Syntax error in LP file. Possibly missing End tag.

MSK\_RES\_ERR\_READ\_LP\_NONEXISTING\_NAME (1162)

A variable never occurred in objective or constraints.

MSK\_RES\_ERR\_REMOVE\_CONE\_VARIABLE (1310)

A variable cannot be removed because it will make a cone invalid.

MSK\_RES\_ERR\_REPAIR\_INVALID\_PROBLEM (1710)

The feasibility repair does not support the specified problem type.

MSK\_RES\_ERR\_REPAIR\_OPTIMIZATION\_FAILED (1711)

Computation the optimal relaxation failed. The cause may have been numerical problems.

MSK\_RES\_ERR\_SEN\_BOUND\_INVALID\_LO (3054)

Analysis of lower bound requested for an index, where no lower bound exists.

MSK\_RES\_ERR\_SEN\_BOUND\_INVALID\_UP (3053)

Analysis of upper bound requested for an index, where no upper bound exists.

MSK\_RES\_ERR\_SEN\_FORMAT (3050)

Syntax error in sensitivity analysis file.

MSK\_RES\_ERR\_SEN\_INDEX\_INVALID (3055)

Invalid range given in the sensitivity file.

MSK\_RES\_ERR\_SEN\_INDEX\_RANGE (3052)

Index out of range in the sensitivity analysis file.

MSK\_RES\_ERR\_SEN\_INVALID\_REGEX (3056)

Syntax error in regexp or regexp longer than 1024.

MSK\_RES\_ERR\_SEN\_NUMERICAL (3058)

Numerical difficulties encountered performing the sensitivity analysis.

MSK\_RES\_ERR\_SEN\_SOLUTION\_STATUS (3057)

No optimal solution found to the original problem given for sensitivity analysis.

MSK\_RES\_ERR\_SEN\_UNDEF\_NAME (3051)

An undefined name was encountered in the sensitivity analysis file.

MSK\_RES\_ERR\_SEN\_UNHANDLED\_PROBLEM\_TYPE (3080)

Sensitivity analysis cannot be performed for the specified problem. Sensitivity analysis is only possible for linear problems.

MSK\_RES\_ERR\_SERVER\_CONNECT (8000)

Failed to connect to remote solver server. The server string or the port string were invalid, or the server did not accept connection.

MSK\_RES\_ERR\_SERVER\_PROTOCOL (8001)

Unexpected message or data from solver server.

MSK\_RES\_ERR\_SERVER\_STATUS (8002)

Server returned non-ok HTTP status code

MSK\_RES\_ERR\_SERVER\_TOKEN (8003)

The job ID specified is incorrect or invalid

MSK\_RES\_ERR\_SIZE\_LICENSE (1005)

The problem is bigger than the license.

MSK\_RES\_ERR\_SIZE\_LICENSE\_CON (1010)

The problem has too many constraints to be solved with the available license.

**MSK\_RES\_ERR\_SIZE\_LICENSE\_INTVAR (1012)**

The problem contains too many integer variables to be solved with the available license.

**MSK\_RES\_ERR\_SIZE\_LICENSE\_NUMCORES (3900)**

The computer contains more cpu cores than the license allows for.

**MSK\_RES\_ERR\_SIZE\_LICENSE\_VAR (1011)**

The problem has too many variables to be solved with the available license.

**MSK\_RES\_ERR\_SOL\_FILE\_INVALID\_NUMBER (1350)**

An invalid number is specified in a solution file.

**MSK\_RES\_ERR\_SOLITEM (1237)**

The solution item number `solitem` is invalid. Please note that `MSK_SOL_ITEM_SNX` is invalid for the basic solution.

**MSK\_RES\_ERR\_SOLVER\_PROBTYPE (1259)**

Problem type does not match the chosen optimizer.

**MSK\_RES\_ERR\_SPACE (1051)**

Out of space.

**MSK\_RES\_ERR\_SPACE\_LEAKING (1080)**

**MOSEK** is leaking memory. This can be due to either an incorrect use of **MOSEK** or a bug.

**MSK\_RES\_ERR\_SPACE\_NO\_INFO (1081)**

No available information about the space usage.

**MSK\_RES\_ERR\_SYM\_MAT\_DUPLICATE (3944)**

A value in a symmetric matrix has been specified more than once.

**MSK\_RES\_ERR\_SYM\_MAT\_HUGE (1482)**

A symmetric matrix contains a huge value in absolute size. The parameter `MSK_DPAR_DATA_SYM_MAT_TOL_HUGE` controls when an  $e_{i,j}$  is considered huge.

**MSK\_RES\_ERR\_SYM\_MAT\_INVALID (1480)**

A symmetric matrix contains an invalid floating point value, i.e. a NaN or an infinite value.

**MSK\_RES\_ERR\_SYM\_MAT\_INVALID\_COL\_INDEX (3941)**

A column index specified for sparse symmetric matrix is invalid.

**MSK\_RES\_ERR\_SYM\_MAT\_INVALID\_ROW\_INDEX (3940)**

A row index specified for sparse symmetric matrix is invalid.

**MSK\_RES\_ERR\_SYM\_MAT\_INVALID\_VALUE (3943)**

The numerical value specified in a sparse symmetric matrix is not a valid floating value.

**MSK\_RES\_ERR\_SYM\_MAT\_NOT\_LOWER\_TRINGULAR (3942)**

Only the lower triangular part of sparse symmetric matrix should be specified.

**MSK\_RES\_ERR\_TASK\_INCOMPATIBLE (2560)**

The Task file is incompatible with this platform. This results from reading a file on a 32 bit platform generated on a 64 bit platform.

**MSK\_RES\_ERR\_TASK\_INVALID (2561)**

The Task file is invalid.

**MSK\_RES\_ERR\_TASK\_WRITE (2562)**

Failed to write the task file.

**MSK\_RES\_ERR\_THREAD\_COND\_INIT (1049)**

Could not initialize a condition.

**MSK\_RES\_ERR\_THREAD\_CREATE (1048)**

Could not create a thread. This error may occur if a large number of environments are created and not deleted again. In any case it is a good practice to minimize the number of environments created.

MSK\_RES\_ERR\_THREAD\_MUTEX\_INIT (1045)

Could not initialize a mutex.

MSK\_RES\_ERR\_THREAD\_MUTEX\_LOCK (1046)

Could not lock a mutex.

MSK\_RES\_ERR\_THREAD\_MUTEX\_UNLOCK (1047)

Could not unlock a mutex.

MSK\_RES\_ERR\_TOCONIC\_CONSTR\_NOT\_CONIC (7153)

The constraint is not conic representable.

MSK\_RES\_ERR\_TOCONIC\_CONSTR\_Q\_NOT\_PSD (7150)

The matrix defining the quadratic part of constraint is not positive semidefinite.

MSK\_RES\_ERR\_TOCONIC\_CONSTRAINT\_FX (7151)

The quadratic constraint is an equality, thus not convex.

MSK\_RES\_ERR\_TOCONIC\_CONSTRAINT\_RA (7152)

The quadratic constraint has finite lower and upper bound, and therefore it is not convex.

MSK\_RES\_ERR\_TOCONIC\_OBJECTIVE\_NOT\_PSD (7155)

The matrix defining the quadratic part of the objective function is not positive semidefinite.

MSK\_RES\_ERR\_TOO\_SMALL\_MAX\_NUM\_NZ (1245)

The maximum number of non-zeros specified is too small.

MSK\_RES\_ERR\_TOO\_SMALL\_MAXNUMANZ (1252)

The maximum number of non-zeros specified for  $A$  is smaller than the number of non-zeros in the current  $A$ .

MSK\_RES\_ERR\_UNB\_STEP\_SIZE (3100)

A step size in an optimizer was unexpectedly unbounded. For instance, if the step-size becomes unbounded in phase 1 of the simplex algorithm then an error occurs. Normally this will happen only if the problem is badly formulated. Please contact **MOSEK** support if this error occurs.

MSK\_RES\_ERR\_UNDEF\_SOLUTION (1265)

**MOSEK** has the following solution types:

- an interior-point solution,
- an basic solution,
- and an integer solution.

Each optimizer may set one or more of these solutions; e.g by default a successful optimization with the interior-point optimizer defines the interior-point solution, and, for linear problems, also the basic solution. This error occurs when asking for a solution or for information about a solution that is not defined.

MSK\_RES\_ERR\_UNDEFINED\_OBJECTIVE\_SENSE (1446)

The objective sense has not been specified before the optimization.

MSK\_RES\_ERR\_UNHANDLED\_SOLUTION\_STATUS (6010)

Unhandled solution status.

MSK\_RES\_ERR\_UNKNOWN (1050)

Unknown error.

MSK\_RES\_ERR\_UPPER\_BOUND\_IS\_A\_NAN (1391)

The upper bound specified is not a number (nan).

MSK\_RES\_ERR\_UPPER\_TRIANGLE (6020)

An element in the upper triangle of a lower triangular matrix is specified.

MSK\_RES\_ERR\_USER\_FUNC\_RET (1430)

An user function reported an error.

- MSK\_RES\_ERR\_USER\_FUNC\_RET\_DATA (1431)  
An user function returned invalid data.
- MSK\_RES\_ERR\_USER\_NLO\_EVAL (1433)  
The user-defined nonlinear function reported an error.
- MSK\_RES\_ERR\_USER\_NLO\_EVAL\_HESSUBI (1440)  
The user-defined nonlinear function reported an invalid subscript in the Hessian.
- MSK\_RES\_ERR\_USER\_NLO\_EVAL\_HESSUBJ (1441)  
The user-defined nonlinear function reported an invalid subscript in the Hessian.
- MSK\_RES\_ERR\_USER\_NLO\_FUNC (1432)  
The user-defined nonlinear function reported an error.
- MSK\_RES\_ERR\_WHICHITEM\_NOT\_ALLOWED (1238)  
*whichitem* is unacceptable.
- MSK\_RES\_ERR\_WHICHSOL (1236)  
The solution defined by *whichsol* does not exists.
- MSK\_RES\_ERR\_WRITE\_LP\_FORMAT (1158)  
Problem cannot be written as an LP file.
- MSK\_RES\_ERR\_WRITE\_LP\_NON\_UNIQUE\_NAME (1161)  
An auto-generated name is not unique.
- MSK\_RES\_ERR\_WRITE\_MPS\_INVALID\_NAME (1153)  
An invalid name is created while writing an MPS file. Usually this will make the MPS file unreadable.
- MSK\_RES\_ERR\_WRITE\_OPF\_INVALID\_VAR\_NAME (1156)  
Empty variable names cannot be written to OPF files.
- MSK\_RES\_ERR\_WRITING\_FILE (1166)  
An error occurred while writing file
- MSK\_RES\_ERR\_XML\_INVALID\_PROBLEM\_TYPE (3600)  
The problem type is not supported by the XML format.
- MSK\_RES\_ERR\_Y\_IS\_UNDEFINED (1449)  
The solution item *y* is undefined.

### 11.2.3 Warning Codes

- MSK\_RES\_WRN\_ANA\_ALMOST\_INT\_BOUNDS (904)  
This warning is issued by the problem analyzer if a constraint is bound nearly integral.
- MSK\_RES\_WRN\_ANA\_C\_ZERO (901)  
This warning is issued by the problem analyzer, if the coefficients in the linear part of the objective are all zero.
- MSK\_RES\_WRN\_ANA\_CLOSE\_BOUNDS (903)  
This warning is issued by problem analyzer, if ranged constraints or variables with very close upper and lower bounds are detected. One should consider treating such constraints as equalities and such variables as constants.
- MSK\_RES\_WRN\_ANA\_EMPTY\_COLS (902)  
This warning is issued by the problem analyzer, if columns, in which all coefficients are zero, are found.
- MSK\_RES\_WRN\_ANA\_LARGE\_BOUNDS (900)  
This warning is issued by the problem analyzer, if one or more constraint or variable bounds are very large. One should consider omitting these bounds entirely by setting them to  $+\text{inf}$  or  $-\text{inf}$ .

MSK\_RES\_WRN\_CONSTRUCT\_INVALID\_SOL\_ITG (807)

The initial value for one or more of the integer variables is not feasible.

MSK\_RES\_WRN\_CONSTRUCT\_NO\_SOL\_ITG (810)

The construct solution requires an integer solution.

MSK\_RES\_WRN\_CONSTRUCT\_SOLUTION\_INFEAS (805)

After fixing the integer variables at the suggested values then the problem is infeasible.

MSK\_RES\_WRN\_DROPPED\_NZ\_QOBJ (201)

One or more non-zero elements were dropped in the Q matrix in the objective.

MSK\_RES\_WRN\_DUPLICATE\_BARVARIABLE\_NAMES (852)

Two barvariable names are identical.

MSK\_RES\_WRN\_DUPLICATE\_CONE\_NAMES (853)

Two cone names are identical.

MSK\_RES\_WRN\_DUPLICATE\_CONSTRAINT\_NAMES (850)

Two constraint names are identical.

MSK\_RES\_WRN\_DUPLICATE\_VARIABLE\_NAMES (851)

Two variable names are identical.

MSK\_RES\_WRN\_ELIMINATOR\_SPACE (801)

The eliminator is skipped at least once due to lack of space.

MSK\_RES\_WRN\_EMPTY\_NAME (502)

A variable or constraint name is empty. The output file may be invalid.

MSK\_RES\_WRN\_IGNORE\_INTEGER (250)

Ignored integer constraints.

MSK\_RES\_WRN\_INCOMPLETE\_LINEAR\_DEPENDENCY\_CHECK (800)

The linear dependency check(s) is incomplete. Normally this is not an important warning unless the optimization problem has been formulated with linear dependencies. Linear dependencies may prevent **MOSEK** from solving the problem.

MSK\_RES\_WRN\_LARGE\_AIJ (62)

A numerically large value is specified for an  $a_{i,j}$  element in  $A$ . The parameter *MSK\_DPAR\_DATA\_TOL\_AIJ\_LARGE* controls when an  $a_{i,j}$  is considered large.

MSK\_RES\_WRN\_LARGE\_BOUND (51)

A numerically large bound value is specified.

MSK\_RES\_WRN\_LARGE\_CJ (57)

A numerically large value is specified for one  $c_j$ .

MSK\_RES\_WRN\_LARGE\_CON\_FX (54)

An equality constraint is fixed to a numerically large value. This can cause numerical problems.

MSK\_RES\_WRN\_LARGE\_LO\_BOUND (52)

A numerically large lower bound value is specified.

MSK\_RES\_WRN\_LARGE\_UP\_BOUND (53)

A numerically large upper bound value is specified.

MSK\_RES\_WRN\_LICENSE\_EXPIRE (500)

The license expires.

MSK\_RES\_WRN\_LICENSE\_FEATURE\_EXPIRE (505)

The license expires.

MSK\_RES\_WRN\_LICENSE\_SERVER (501)

The license server is not responding.

MSK\_RES\_WRN\_LP\_DROP\_VARIABLE (85)

Ignored a variable because the variable was not previously defined. Usually this implies that a variable appears in the bound section but not in the objective or the constraints.

**MSK\_RES\_WRN\_LP\_OLD\_QUAD\_FORMAT (80)**

Missing  $\sqrt{2}$  after quadratic expressions in bound or objective.

**MSK\_RES\_WRN\_MIO\_INFEASIBLE\_FINAL (270)**

The final mixed-integer problem with all the integer variables fixed at their optimal values is infeasible.

**MSK\_RES\_WRN\_MPS\_SPLIT\_BOU\_VECTOR (72)**

A BOUNDS vector is split into several nonadjacent parts in an MPS file.

**MSK\_RES\_WRN\_MPS\_SPLIT\_RAN\_VECTOR (71)**

A RANGE vector is split into several nonadjacent parts in an MPS file.

**MSK\_RES\_WRN\_MPS\_SPLIT\_RHS\_VECTOR (70)**

An RHS vector is split into several nonadjacent parts in an MPS file.

**MSK\_RES\_WRN\_NAME\_MAX\_LEN (65)**

A name is longer than the buffer that is supposed to hold it.

**MSK\_RES\_WRN\_NO\_DUALIZER (950)**

No automatic dualizer is available for the specified problem. The primal problem is solved.

**MSK\_RES\_WRN\_NO\_GLOBAL\_OPTIMIZER (251)**

No global optimizer is available.

**MSK\_RES\_WRN\_NO\_NONLINEAR\_FUNCTION\_WRITE (450)**

The problem contains a general nonlinear function in either the objective or the constraints. Such a nonlinear function cannot be written to a disk file. Note that quadratic terms when inputted explicitly can be written to disk.

**MSK\_RES\_WRN\_NZ\_IN\_UPR\_TRI (200)**

Non-zero elements specified in the upper triangle of a matrix were ignored.

**MSK\_RES\_WRN\_OPEN\_PARAM\_FILE (50)**

The parameter file could not be opened.

**MSK\_RES\_WRN\_PARAM\_IGNORED\_CMIO (516)**

A parameter was ignored by the conic mixed integer optimizer.

**MSK\_RES\_WRN\_PARAM\_NAME\_DOUB (510)**

The parameter name is not recognized as a double parameter.

**MSK\_RES\_WRN\_PARAM\_NAME\_INT (511)**

The parameter name is not recognized as an integer parameter.

**MSK\_RES\_WRN\_PARAM\_NAME\_STR (512)**

The parameter name is not recognized as a string parameter.

**MSK\_RES\_WRN\_PARAM\_STR\_VALUE (515)**

The string is not recognized as a symbolic value for the parameter.

**MSK\_RES\_WRN\_PRESOLVE\_OUTOFSPACE (802)**

The presolve is incomplete due to lack of space.

**MSK\_RES\_WRN\_QUAD\_CONES\_WITH\_ROOT\_FIXED\_AT\_ZERO (930)**

For at least one quadratic cone the root is fixed at (nearly) zero. This may cause problems such as a very large dual solution. Therefore, it is recommended to remove such cones before optimizing the problems, or to fix all the variables in the cone to 0.

**MSK\_RES\_WRN\_RQUAD\_CONES\_WITH\_ROOT\_FIXED\_AT\_ZERO (931)**

For at least one rotated quadratic cone at least one of the root variables are fixed at (nearly) zero. This may cause problems such as a very large dual solution. Therefore, it is recommended to remove such cones before optimizing the problems, or to fix all the variables in the cone to 0.

**MSK\_RES\_WRN\_SOL\_FILE\_IGNORED\_CON (351)**

One or more lines in the constraint section were ignored when reading a solution file.

MSK\_RES\_WRN\_SOL\_FILE\_IGNORED\_VAR (352)

One or more lines in the variable section were ignored when reading a solution file.

MSK\_RES\_WRN\_SOL\_FILTER (300)

Invalid solution filter is specified.

MSK\_RES\_WRN\_SPAR\_MAX\_LEN (66)

A value for a string parameter is longer than the buffer that is supposed to hold it.

MSK\_RES\_WRN\_SYM\_MAT\_LARGE (960)

A numerically large value is specified for an  $e_{i,j}$  element in  $E$ . The parameter `MSK_DPAR_DATA_SYM_MAT_TOL_LARGE` controls when an  $e_{i,j}$  is considered large.

MSK\_RES\_WRN\_TOO\_FEW\_BASIS\_VARS (400)

An incomplete basis has been specified. Too few basis variables are specified.

MSK\_RES\_WRN\_TOO\_MANY\_BASIS\_VARS (405)

A basis with too many variables has been specified.

MSK\_RES\_WRN\_UNDEF\_SOL\_FILE\_NAME (350)

Undefined name occurred in a solution.

MSK\_RES\_WRN\_USING\_GENERIC\_NAMES (503)

Generic names are used because a name is not valid. For instance when writing an LP file the names must not contain blanks or start with a digit.

MSK\_RES\_WRN\_WRITE\_CHANGED\_NAMES (803)

Some names were changed because they were invalid for the output file format.

MSK\_RES\_WRN\_WRITE\_DISCARDED\_CFIX (804)

The fixed objective term could not be converted to a variable and was discarded in the output file.

MSK\_RES\_WRN\_ZERO\_AIJ (63)

One or more zero elements are specified in  $A$ .

MSK\_RES\_WRN\_ZEROS\_IN\_SPARSE\_COL (710)

One or more (near) zero elements are specified in a sparse column of a matrix. It is redundant to specify zero elements. Hence, it may indicate an error.

MSK\_RES\_WRN\_ZEROS\_IN\_SPARSE\_ROW (705)

One or more (near) zero elements are specified in a sparse row of a matrix. Since, it is redundant to specify zero elements then it may indicate an error.

## 11.3 Enumerations

MSKlanguagee

Language selection constants

MSK\_LANG\_ENG

English language selection

MSK\_LANG\_DAN

Danish language selection

MSKaccmodee

Constraint or variable access modes

MSK\_ACC\_VAR

Access data by columns (variable oriented)

MSK\_ACC\_CON

Access data by rows (constraint oriented)

MSKbasindtypee

Basis identification



MSK\_BI\_NEVER

Never do basis identification.

MSK\_BI\_ALWAYS

Basis identification is always performed even if the interior-point optimizer terminates abnormally.

MSK\_BI\_NO\_ERROR

Basis identification is performed if the interior-point optimizer terminates without an error.

MSK\_BI\_IF\_FEASIBLE

Basis identification is not performed if the interior-point optimizer terminates with a problem status saying that the problem is primal or dual infeasible.

MSK\_BI\_RESERVED

Not currently in use.

MSKboundkeye

Bound keys

MSK\_BK\_LO

The constraint or variable has a finite lower bound and an infinite upper bound.

MSK\_BK\_UP

The constraint or variable has an infinite lower bound and a finite upper bound.

MSK\_BK\_FX

The constraint or variable is fixed.

MSK\_BK\_FR

The constraint or variable is free.

MSK\_BK\_RA

The constraint or variable is ranged.

MSKmarke

Mark

MSK\_MARK\_LO

The lower bound is selected for sensitivity analysis.

MSK\_MARK\_UP

The upper bound is selected for sensitivity analysis.

MSKsimdegene

Degeneracy strategies

MSK\_SIM\_DEGEN\_NONE

The simplex optimizer should use no degeneration strategy.

MSK\_SIM\_DEGEN\_FREE

The simplex optimizer chooses the degeneration strategy.

MSK\_SIM\_DEGEN\_AGGRESSIVE

The simplex optimizer should use an aggressive degeneration strategy.

MSK\_SIM\_DEGEN\_MODERATE

The simplex optimizer should use a moderate degeneration strategy.

MSK\_SIM\_DEGEN\_MINIMUM

The simplex optimizer should use a minimum degeneration strategy.

MSKtransposee

Transposed matrix.

MSK\_TRANSPOSE\_NO

No transpose is applied.

MSK\_TRANSPOSE\_YES

A transpose is applied.

MSKuploe

Triangular part of a symmetric matrix.

MSK\_UPLO\_LO

Lower part.

MSK\_UPLO\_UP

Upper part

MSKsimreforme

Problem reformulation.

MSK\_SIM\_REFORMULATION\_ON

Allow the simplex optimizer to reformulate the problem.

MSK\_SIM\_REFORMULATION\_OFF

Disallow the simplex optimizer to reformulate the problem.

MSK\_SIM\_REFORMULATION\_FREE

The simplex optimizer can choose freely.

MSK\_SIM\_REFORMULATION\_AGGRESSIVE

The simplex optimizer should use an aggressive reformulation strategy.

MSKsimdupvece

Exploit duplicate columns.

MSK\_SIM\_EXPLOIT\_DUPVEC\_ON

Allow the simplex optimizer to exploit duplicated columns.

MSK\_SIM\_EXPLOIT\_DUPVEC\_OFF

Disallow the simplex optimizer to exploit duplicated columns.

MSK\_SIM\_EXPLOIT\_DUPVEC\_FREE

The simplex optimizer can choose freely.

MSKsimhotstarte

Hot-start type employed by the simplex optimizer

MSK\_SIM\_HOTSTART\_NONE

The simplex optimizer performs a coldstart.

MSK\_SIM\_HOTSTART\_FREE

The simplex optimizer chooses the hot-start type.

MSK\_SIM\_HOTSTART\_STATUS\_KEYS

Only the status keys of the constraints and variables are used to choose the type of hot-start.

MSKintpnthotstarte

Hot-start type employed by the interior-point optimizers.

MSK\_INTPNT\_HOTSTART\_NONE

The interior-point optimizer performs a coldstart.

MSK\_INTPNT\_HOTSTART\_PRIMAL

The interior-point optimizer exploits the primal solution only.

MSK\_INTPNT\_HOTSTART\_DUAL

The interior-point optimizer exploits the dual solution only.

MSK\_INTPNT\_HOTSTART\_PRIMAL\_DUAL

The interior-point optimizer exploits both the primal and dual solution.

MSKcallbackcodee

Progress call-back codes

**MSK\_CALLBACK\_BEGIN\_ROOT\_CUTGEN**

The call-back function is called when root cut generation is started.

**MSK\_CALLBACK\_IM\_ROOT\_CUTGEN**

The call-back is called from within root cut generation at an intermediate stage.

**MSK\_CALLBACK\_END\_ROOT\_CUTGEN**

The call-back function is called when root cut generation is terminated.

**MSK\_CALLBACK\_BEGIN\_OPTIMIZER**

The call-back function is called when the optimizer is started.

**MSK\_CALLBACK\_END\_OPTIMIZER**

The call-back function is called when the optimizer is terminated.

**MSK\_CALLBACK\_BEGIN\_PRESOLVE**

The call-back function is called when the presolve is started.

**MSK\_CALLBACK\_UPDATE\_PRESOLVE**

The call-back function is called from within the presolve procedure.

**MSK\_CALLBACK\_IM\_PRESOLVE**

The call-back function is called from within the presolve procedure at an intermediate stage.

**MSK\_CALLBACK\_END\_PRESOLVE**

The call-back function is called when the presolve is completed.

**MSK\_CALLBACK\_BEGIN\_INTPNT**

The call-back function is called when the interior-point optimizer is started.

**MSK\_CALLBACK\_INTPNT**

The call-back function is called from within the interior-point optimizer after the information database has been updated.

**MSK\_CALLBACK\_IM\_INTPNT**

The call-back function is called at an intermediate stage within the interior-point optimizer where the information database has not been updated.

**MSK\_CALLBACK\_END\_INTPNT**

The call-back function is called when the interior-point optimizer is terminated.

**MSK\_CALLBACK\_BEGIN\_CONIC**

The call-back function is called when the conic optimizer is started.

**MSK\_CALLBACK\_CONIC**

The call-back function is called from within the conic optimizer after the information database has been updated.

**MSK\_CALLBACK\_IM\_CONIC**

The call-back function is called at an intermediate stage within the conic optimizer where the information database has not been updated.

**MSK\_CALLBACK\_END\_CONIC**

The call-back function is called when the conic optimizer is terminated.

**MSK\_CALLBACK\_PRIMAL\_SIMPLEX**

The call-back function is called from within the primal simplex optimizer.

**MSK\_CALLBACK\_DUAL\_SIMPLEX**

The call-back function is called from within the dual simplex optimizer.

**MSK\_CALLBACK\_BEGIN\_BI**

The basis identification procedure has been started.

**MSK\_CALLBACK\_IM\_BI**

The call-back function is called from within the basis identification procedure at an intermediate point.

**MSK\_CALLBACK\_END\_BI**

The call-back function is called when the basis identification procedure is terminated.

**MSK\_CALLBACK\_BEGIN\_PRIMAL\_BI**

The call-back function is called from within the basis identification procedure when the primal phase is started.

**MSK\_CALLBACK\_IM\_PRIMAL\_BI**

The call-back function is called from within the basis identification procedure at an intermediate point in the primal phase.

**MSK\_CALLBACK\_UPDATE\_PRIMAL\_BI**

The call-back function is called from within the basis identification procedure at an intermediate point in the primal phase.

**MSK\_CALLBACK\_END\_PRIMAL\_BI**

The call-back function is called from within the basis identification procedure when the primal phase is terminated.

**MSK\_CALLBACK\_BEGIN\_DUAL\_BI**

The call-back function is called from within the basis identification procedure when the dual phase is started.

**MSK\_CALLBACK\_IM\_DUAL\_BI**

The call-back function is called from within the basis identification procedure at an intermediate point in the dual phase.

**MSK\_CALLBACK\_UPDATE\_DUAL\_BI**

The call-back function is called from within the basis identification procedure at an intermediate point in the dual phase.

**MSK\_CALLBACK\_END\_DUAL\_BI**

The call-back function is called from within the basis identification procedure when the dual phase is terminated.

**MSK\_CALLBACK\_BEGIN\_SIMPLEX\_BI**

The call-back function is called from within the basis identification procedure when the simplex clean-up phase is started.

**MSK\_CALLBACK\_IM\_SIMPLEX\_BI**

The call-back function is called from within the basis identification procedure at an intermediate point in the simplex clean-up phase. The frequency of the call-backs is controlled by the *MSK\_IPAR\_LOG\_SIM\_FREQ* parameter.

**MSK\_CALLBACK\_BEGIN\_PRIMAL\_SIMPLEX\_BI**

The call-back function is called from within the basis identification procedure when the primal simplex clean-up phase is started.

**MSK\_CALLBACK\_UPDATE\_PRIMAL\_SIMPLEX\_BI**

The call-back function is called from within the basis identification procedure at an intermediate point in the primal simplex clean-up phase. The frequency of the call-backs is controlled by the *MSK\_IPAR\_LOG\_SIM\_FREQ* parameter.

**MSK\_CALLBACK\_END\_PRIMAL\_SIMPLEX\_BI**

The call-back function is called from within the basis identification procedure when the primal clean-up phase is terminated.

**MSK\_CALLBACK\_BEGIN\_PRIMAL\_DUAL\_SIMPLEX\_BI**

The call-back function is called from within the basis identification procedure when the primal-dual simplex clean-up phase is started.

**MSK\_CALLBACK\_UPDATE\_PRIMAL\_DUAL\_SIMPLEX\_BI**

The call-back function is called from within the basis identification procedure at an intermediate point in the primal-dual simplex clean-up phase. The frequency of the call-backs is controlled by the *MSK\_IPAR\_LOG\_SIM\_FREQ* parameter.

**MSK\_CALLBACK\_END\_PRIMAL\_DUAL\_SIMPLEX\_BI**

The call-back function is called from within the basis identification procedure when the primal-dual clean-up phase is terminated.

**MSK\_CALLBACK\_BEGIN\_DUAL\_SIMPLEX\_BI**

The call-back function is called from within the basis identification procedure when the dual simplex clean-up phase is started.

**MSK\_CALLBACK\_UPDATE\_DUAL\_SIMPLEX\_BI**

The call-back function is called from within the basis identification procedure at an intermediate point in the dual simplex clean-up phase. The frequency of the call-backs is controlled by the *MSK\_IPAR\_LOG\_SIM\_FREQ* parameter.

**MSK\_CALLBACK\_END\_DUAL\_SIMPLEX\_BI**

The call-back function is called from within the basis identification procedure when the dual clean-up phase is terminated.

**MSK\_CALLBACK\_END\_SIMPLEX\_BI**

The call-back function is called from within the basis identification procedure when the simplex clean-up phase is terminated.

**MSK\_CALLBACK\_BEGIN\_MIO**

The call-back function is called when the mixed-integer optimizer is started.

**MSK\_CALLBACK\_IM\_MIO**

The call-back function is called at an intermediate point in the mixed-integer optimizer.

**MSK\_CALLBACK\_NEW\_INT\_MIO**

The call-back function is called after a new integer solution has been located by the mixed-integer optimizer.

**MSK\_CALLBACK\_END\_MIO**

The call-back function is called when the mixed-integer optimizer is terminated.

**MSK\_CALLBACK\_BEGIN\_SIMPLEX**

The call-back function is called when the simplex optimizer is started.

**MSK\_CALLBACK\_BEGIN\_DUAL\_SIMPLEX**

The call-back function is called when the dual simplex optimizer started.

**MSK\_CALLBACK\_IM\_DUAL\_SIMPLEX**

The call-back function is called at an intermediate point in the dual simplex optimizer.

**MSK\_CALLBACK\_UPDATE\_DUAL\_SIMPLEX**

The call-back function is called in the dual simplex optimizer.

**MSK\_CALLBACK\_END\_DUAL\_SIMPLEX**

The call-back function is called when the dual simplex optimizer is terminated.

**MSK\_CALLBACK\_BEGIN\_PRIMAL\_SIMPLEX**

The call-back function is called when the primal simplex optimizer is started.

**MSK\_CALLBACK\_IM\_PRIMAL\_SIMPLEX**

The call-back function is called at an intermediate point in the primal simplex optimizer.

**MSK\_CALLBACK\_UPDATE\_PRIMAL\_SIMPLEX**

The call-back function is called in the primal simplex optimizer.

**MSK\_CALLBACK\_END\_PRIMAL\_SIMPLEX**

The call-back function is called when the primal simplex optimizer is terminated.

**MSK\_CALLBACK\_BEGIN\_PRIMAL\_DUAL\_SIMPLEX**

The call-back function is called when the primal-dual simplex optimizer is started.

**MSK\_CALLBACK\_IM\_PRIMAL\_DUAL\_SIMPLEX**

The call-back function is called at an intermediate point in the primal-dual simplex optimizer.

**MSK\_CALLBACK\_UPDATE\_PRIMAL\_DUAL\_SIMPLEX**

The call-back function is called in the primal-dual simplex optimizer.

**MSK\_CALLBACK\_END\_PRIMAL\_DUAL\_SIMPLEX**

The call-back function is called when the primal-dual simplex optimizer is terminated.

**MSK\_CALLBACK\_END\_SIMPLEX**

The call-back function is called when the simplex optimizer is terminated.

**MSK\_CALLBACK\_BEGIN\_INFEAS\_ANA**

The call-back function is called when the infeasibility analyzer is started.

**MSK\_CALLBACK\_END\_INFEAS\_ANA**

The call-back function is called when the infeasibility analyzer is terminated.

**MSK\_CALLBACK\_IM\_PRIMAL\_SENSIVITY**

The call-back function is called at an intermediate stage of the primal sensitivity analysis.

**MSK\_CALLBACK\_IM\_DUAL\_SENSIVITY**

The call-back function is called at an intermediate stage of the dual sensitivity analysis.

**MSK\_CALLBACK\_IM\_MIO\_INTPNT**

The call-back function is called at an intermediate point in the mixed-integer optimizer while running the interior-point optimizer.

**MSK\_CALLBACK\_IM\_MIO\_PRIMAL\_SIMPLEX**

The call-back function is called at an intermediate point in the mixed-integer optimizer while running the primal simplex optimizer.

**MSK\_CALLBACK\_IM\_MIO\_DUAL\_SIMPLEX**

The call-back function is called at an intermediate point in the mixed-integer optimizer while running the dual simplex optimizer.

**MSK\_CALLBACK\_BEGIN\_PRIMAL\_SETUP\_BI**

The call-back function is called when the primal BI setup is started.

**MSK\_CALLBACK\_END\_PRIMAL\_SETUP\_BI**

The call-back function is called when the primal BI setup is terminated.

**MSK\_CALLBACK\_BEGIN\_DUAL\_SETUP\_BI**

The call-back function is called when the dual BI phase is started.

**MSK\_CALLBACK\_END\_DUAL\_SETUP\_BI**

The call-back function is called when the dual BI phase is terminated.

**MSK\_CALLBACK\_BEGIN\_PRIMAL\_SENSITIVITY**

Primal sensitivity analysis is started.

**MSK\_CALLBACK\_END\_PRIMAL\_SENSITIVITY**

Primal sensitivity analysis is terminated.

**MSK\_CALLBACK\_BEGIN\_DUAL\_SENSITIVITY**

Dual sensitivity analysis is started.

**MSK\_CALLBACK\_END\_DUAL\_SENSITIVITY**

Dual sensitivity analysis is terminated.

**MSK\_CALLBACK\_BEGIN\_LICENSE\_WAIT**

Begin waiting for license.

**MSK\_CALLBACK\_END\_LICENSE\_WAIT**

End waiting for license.

**MSK\_CALLBACK\_IM\_LICENSE\_WAIT**

**MOSEK** is waiting for a license.

**MSK\_CALLBACK\_BEGIN\_QCQO\_REFORMULATE**

Begin QCQO reformulation.

MSK\_CALLBACK\_END\_QCQO\_REFORMULATE

End QCQO reformulation.

MSK\_CALLBACK\_IM\_QO\_REFORMULATE

The call-back function is called at an intermediate stage of the conic quadratic reformulation.

MSK\_CALLBACK\_BEGIN\_TO\_CONIC

Begin conic reformulation.

MSK\_CALLBACK\_END\_TO\_CONIC

End conic reformulation.

MSK\_CALLBACK\_BEGIN\_FULL\_CONVEXITY\_CHECK

Begin full convexity check.

MSK\_CALLBACK\_END\_FULL\_CONVEXITY\_CHECK

End full convexity check.

MSK\_CALLBACK\_IM\_FULL\_CONVEXITY\_CHECK

The call-back function is called at an intermediate stage of the full convexity check.

MSK\_CALLBACK\_BEGIN\_PRIMAL\_REPAIR

Begin primal feasibility repair.

MSK\_CALLBACK\_END\_PRIMAL\_REPAIR

End primal feasibility repair.

MSK\_CALLBACK\_BEGIN\_READ

**MOSEK** has started reading a problem file.

MSK\_CALLBACK\_IM\_READ

Intermediate stage in reading.

MSK\_CALLBACK\_END\_READ

**MOSEK** has finished reading a problem file.

MSK\_CALLBACK\_BEGIN\_WRITE

**MOSEK** has started writing a problem file.

MSK\_CALLBACK\_END\_WRITE

**MOSEK** has finished writing a problem file.

MSK\_CALLBACK\_READ\_OPF\_SECTION

A chunk of  $Q$  non-zeros has been read from a problem file.

MSK\_CALLBACK\_IM\_LU

The call-back function is called from within the LU factorization procedure at an intermediate point.

MSK\_CALLBACK\_IM\_ORDER

The call-back function is called from within the matrix ordering procedure at an intermediate point.

MSK\_CALLBACK\_IM\_SIMPLEX

The call-back function is called from within the simplex optimizer at an intermediate point.

MSK\_CALLBACK\_READ\_OPF

The call-back function is called from the OPF reader.

MSK\_CALLBACK\_WRITE\_OPF

The call-back function is called from the OPF writer.

MSK\_CALLBACK\_SOLVING\_REMOTE

The call-back function is called while the task is being solved on a remote server.

MSKcheckconvexitytypee

Types of convexity checks.

**MSK\_CHECK\_CONVEXITY\_NONE**

No convexity check.

**MSK\_CHECK\_CONVEXITY\_SIMPLE**

Perform simple and fast convexity check.

**MSK\_CHECK\_CONVEXITY\_FULL**

Perform a full convexity check.

**MSKcompresstypee**

Compression types

**MSK\_COMPRESS\_NONE**

No compression is used.

**MSK\_COMPRESS\_FREE**

The type of compression used is chosen automatically.

**MSK\_COMPRESS\_GZIP**

The type of compression used is gzip compatible.

**MSKconetypee**

Cone types

**MSK\_CT\_QUAD**

The cone is a quadratic cone.

**MSK\_CT\_RQUAD**

The cone is a rotated quadratic cone.

**MSKnametypee**

Name types

**MSK\_NAME\_TYPE\_GEN**

General names. However, no duplicate and blank names are allowed.

**MSK\_NAME\_TYPE\_MPS**

MPS type names.

**MSK\_NAME\_TYPE\_LP**

LP type names.

**MSKsymmattypee**

Cone types

**MSK\_SYMMAT\_TYPE\_SPARSE**

Sparse symmetric matrix.

**MSKdataformate**

Data format types

**MSK\_DATA\_FORMAT\_EXTENSION**

The file extension is used to determine the data file format.

**MSK\_DATA\_FORMAT\_MPS**

The data file is MPS formatted.

**MSK\_DATA\_FORMAT\_LP**

The data file is LP formatted.

**MSK\_DATA\_FORMAT\_OP**

The data file is an optimization problem formatted file.

**MSK\_DATA\_FORMAT\_XML**

The data file is an XML formatted file.

**MSK\_DATA\_FORMAT\_FREE\_MPS**

The data a free MPS formatted file.



**MSK\_DATA\_FORMAT\_TASK**  
Generic task dump file.

**MSK\_DATA\_FORMAT\_CB**  
Conic benchmark format,

**MSK\_DATA\_FORMAT\_JSON\_TASK**  
JSON based task format.

**MSKdinfiteme**  
Double information items

**MSK\_DINF\_BI\_TIME**  
Time spent within the basis identification procedure since its invocation.

**MSK\_DINF\_BI\_PRIMAL\_TIME**  
Time spent within the primal phase of the basis identification procedure since its invocation.

**MSK\_DINF\_BI\_DUAL\_TIME**  
Time spent within the dual phase basis identification procedure since its invocation.

**MSK\_DINF\_BI\_CLEAN\_TIME**  
Time spent within the clean-up phase of the basis identification procedure since its invocation.

**MSK\_DINF\_BI\_CLEAN\_PRIMAL\_TIME**  
Time spent within the primal clean-up optimizer of the basis identification procedure since its invocation.

**MSK\_DINF\_BI\_CLEAN\_PRIMAL\_DUAL\_TIME**  
Time spent within the primal-dual clean-up optimizer of the basis identification procedure since its invocation.

**MSK\_DINF\_BI\_CLEAN\_DUAL\_TIME**  
Time spent within the dual clean-up optimizer of the basis identification procedure since its invocation.

**MSK\_DINF\_INTPNT\_TIME**  
Time spent within the interior-point optimizer since its invocation.

**MSK\_DINF\_INTPNT\_ORDER\_TIME**  
Order time (in seconds).

**MSK\_DINF\_INTPNT\_PRIMAL\_OBJ**  
Primal objective value reported by the interior-point optimizer.

**MSK\_DINF\_INTPNT\_DUAL\_OBJ**  
Dual objective value reported by the interior-point optimizer.

**MSK\_DINF\_INTPNT\_PRIMAL\_FEAS**  
Primal feasibility measure reported by the interior-point optimizers. (For the interior-point optimizer this measure does not directly related to the original problem because a homogeneous model is employed).

**MSK\_DINF\_INTPNT\_DUAL\_FEAS**  
Dual feasibility measure reported by the interior-point optimizer. (For the interior-point optimizer this measure does not directly related to the original problem because a homogeneous model is employed.)

**MSK\_DINF\_INTPNT\_OPT\_STATUS**  
This measure should converge to +1 if the problem has a primal-dual optimal solution, and converge to -1 if problem is (strictly) primal or dual infeasible. If the measure converges to another constant, or fails to settle, the problem is usually ill-posed.

**MSK\_DINF\_SIM\_TIME**  
Time spent in the simplex optimizer since invoking it.

**MSK\_DINF\_SIM\_PRIMAL\_TIME**  
Time spent in the primal simplex optimizer since invoking it.

MSK\_DINF\_SIM\_DUAL\_TIME

Time spent in the dual simplex optimizer since invoking it.

MSK\_DINF\_SIM\_PRIMAL\_DUAL\_TIME

Time spent in the primal-dual simplex optimizer since invoking it.

MSK\_DINF\_SIM\_OBJ

Objective value reported by the simplex optimizer.

MSK\_DINF\_SIM\_FEAS

Feasibility measure reported by the simplex optimizer.

MSK\_DINF\_MIO\_TIME

Time spent in the mixed-integer optimizer.

MSK\_DINF\_MIO\_ROOT PRESOLVE\_TIME

Time spent in while presolving the root relaxation.

MSK\_DINF\_MIO\_ROOT\_OPTIMIZER\_TIME

Time spent in the optimizer while solving the root relaxation.

MSK\_DINF\_MIO\_OPTIMIZER\_TIME

Total time spent in the optimizer.

MSK\_DINF\_MIO\_HEURISTIC\_TIME

Total time spent in the optimizer.

MSK\_DINF\_TO\_CONIC\_TIME

Time spent in the last to conic reformulation.

MSK\_DINF\_MIO\_CONSTRUCT\_SOLUTION\_OBJ

If **MOSEK** has successfully constructed an integer feasible solution, then this item contains the optimal objective value corresponding to the feasible solution.

MSK\_DINF\_MIO\_OBJ\_INT

The primal objective value corresponding to the best integer feasible solution. Please note that at least one integer feasible solution must have located i.e. check | [MSK\\_DINF\\_MIO\\_NUM\\_INT\\_SOLUTIONS](#) |.

MSK\_DINF\_MIO\_OBJ\_BOUND

The best known bound on the objective function. This value is undefined until at least one relaxation has been solved: To see if this is the case check that | [MSK\\_DINF\\_MIO\\_NUM\\_RELAX](#) | is strictly positive.

MSK\_DINF\_MIO\_OBJ\_REL\_GAP

Given that the mixed-integer optimizer has computed a feasible solution and a bound on the optimal objective value, then this item contains the relative gap defined by

$$\frac{|(\text{objective value of feasible solution}) - (\text{objective bound})|}{\max(\delta, |(\text{objective value of feasible solution})|)}.$$

where  $\delta$  is given by the parameter [MSK\\_DPAR\\_MIO\\_REL\\_GAP\\_CONST](#). Otherwise it has the value  $-1.0$ .

MSK\_DINF\_MIO\_OBJ\_ABS\_GAP

Given the mixed-integer optimizer has computed a feasible solution and a bound on the optimal objective value, then this item contains the absolute gap defined by

$$|(\text{objective value of feasible solution}) - (\text{objective bound})|.$$

Otherwise it has the value  $-1.0$ .

MSK\_DINF\_MIO\_USER\_OBJ\_CUT

If the objective cut is used, then this information item has the value of the cut.

MSK\_DINF\_MIO\_CMIR\_SEPARATION\_TIME

Separation time for CMIR cuts.

MSK\_DINF\_MIO\_CLIQUE\_SEPARATION\_TIME  
 Separation time for clique cuts.

MSK\_DINF\_MIO\_KNAPSACK\_COVER\_SEPARATION\_TIME  
 Separation time for knapsack cover.

MSK\_DINF\_MIO\_GMI\_SEPARATION\_TIME  
 Separation time for GMI cuts.

MSK\_DINF\_MIO\_IMPLIED\_BOUND\_TIME  
 Separation time for implied bound cuts.

MSK\_DINF\_MIO\_ROOT\_CUTGEN\_TIME  
 Total time for cut generation.

MSK\_DINF\_MIO\_PROBING\_TIME  
 Total time for probing.

MSK\_DINF\_OPTIMIZER\_TIME  
 Total time spent in the optimizer since it was invoked.

MSK\_DINF PRESOLVE\_TIME  
 Total time (in seconds) spent in the presolve since it was invoked.

MSK\_DINF\_MIO\_DUAL\_BOUND\_AFTER\_PRESOLVE  
 Value of the dual bound after presolve but before cut generation.

MSK\_DINF PRESOLVE\_ELI\_TIME  
 Total time spent in the eliminator since the presolve was invoked.

MSK\_DINF PRESOLVE\_LINDEP\_TIME  
 Total time spent in the linear dependency checker since the presolve was invoked.

MSK\_DINF\_RD\_TIME  
 Time spent reading the data file.

MSK\_DINF\_SOL\_ITR\_PRIMAL\_OBJ  
 Primal objective value of the interior-point solution.

MSK\_DINF\_SOL\_ITR\_PVIOLCON  
 Maximal primal bound violation for  $x^c$  in the interior-point solution.

MSK\_DINF\_SOL\_ITR\_PVIOLVAR  
 Maximal primal bound violation for  $x^x$  in the interior-point solution.

MSK\_DINF\_SOL\_ITR\_PVIOLBARVAR  
 Maximal primal bound violation for  $\overline{X}$  in the interior-point solution.

MSK\_DINF\_SOL\_ITR\_PVIOLCONES  
 Maximal primal violation for primal conic constraints in the interior-point solution.

MSK\_DINF\_SOL\_ITR\_DUAL\_OBJ  
 Dual objective value of the interior-point solution.

MSK\_DINF\_SOL\_ITR\_DVIOLCON  
 Maximal dual bound violation for  $x^c$  in the interior-point solution.

MSK\_DINF\_SOL\_ITR\_DVIOLVAR  
 Maximal dual bound violation for  $x^x$  in the interior-point solution.

MSK\_DINF\_SOL\_ITR\_DVIOLBARVAR  
 Maximal dual bound violation for  $\overline{X}$  in the interior-point solution.

MSK\_DINF\_SOL\_ITR\_DVIOLCONES  
 Maximal dual violation for dual conic constraints in the interior-point solution.

MSK\_DINF\_SOL\_ITR\_NRM\_XC  
 Infinity norm of  $x^c$  in the interior-point solution.

MSK\_DINF\_SOL\_ITR\_NRM\_XX  
Infinity norm of  $x^x$  in the interior-point solution.

MSK\_DINF\_SOL\_ITR\_NRM\_BARX  
Infinity norm of  $\bar{X}$  in the interior-point solution.

MSK\_DINF\_SOL\_ITR\_NRM\_Y  
Infinity norm of  $y$  in the interior-point solution.

MSK\_DINF\_SOL\_ITR\_NRM\_SLC  
Infinity norm of  $s_l^c$  in the interior-point solution.

MSK\_DINF\_SOL\_ITR\_NRM\_SUC  
Infinity norm of  $s_u^c$  in the interior-point solution.

MSK\_DINF\_SOL\_ITR\_NRM\_SLX  
Infinity norm of  $s_l^x$  in the interior-point solution.

MSK\_DINF\_SOL\_ITR\_NRM\_SUX  
Infinity norm of  $s_u^X$  in the interior-point solution.

MSK\_DINF\_SOL\_ITR\_NRM\_SNX  
Infinity norm of  $s_n^x$  in the interior-point solution.

MSK\_DINF\_SOL\_ITR\_NRM\_BARS  
Infinity norm of  $\bar{S}$  in the interior-point solution.

MSK\_DINF\_SOL\_BAS\_PRIMAL\_OBJ  
Primal objective value of the basic solution.

MSK\_DINF\_SOL\_BAS\_PVIOLCON  
Maximal primal bound violation for  $x^c$  in the basic solution.

MSK\_DINF\_SOL\_BAS\_PVIOLVAR  
Maximal primal bound violation for  $x^x$  in the basic solution.

MSK\_DINF\_SOL\_BAS\_DUAL\_OBJ  
Dual objective value of the basic solution.

MSK\_DINF\_SOL\_BAS\_DVIOLCON  
Maximal dual bound violation for  $x^c$  in the basic solution.

MSK\_DINF\_SOL\_BAS\_DVIOLVAR  
Maximal dual bound violation for  $x^x$  in the basic solution.

MSK\_DINF\_SOL\_BAS\_NRM\_XC  
Infinity norm of  $x^c$  in the basic solution.

MSK\_DINF\_SOL\_BAS\_NRM\_XX  
Infinity norm of  $x^x$  in the basic solution.

MSK\_DINF\_SOL\_BAS\_NRM\_BARX  
Infinity norm of  $\bar{X}$  in the basic solution.

MSK\_DINF\_SOL\_BAS\_NRM\_Y  
Infinity norm of  $y$  in the basic solution.

MSK\_DINF\_SOL\_BAS\_NRM\_SLC  
Infinity norm of  $s_l^c$  in the basic solution.

MSK\_DINF\_SOL\_BAS\_NRM\_SUC  
Infinity norm of  $s_u^c$  in the basic solution.

MSK\_DINF\_SOL\_BAS\_NRM\_SLX  
Infinity norm of  $s_l^x$  in the basic solution.

MSK\_DINF\_SOL\_BAS\_NRM\_SUX  
Infinity norm of  $s_u^X$  in the basic solution.

- MSK\_DINF\_SOL\_ITG\_PRIMAL\_OBJ**  
Primal objective value of the integer solution.
- MSK\_DINF\_SOL\_ITG\_PVIOLCON**  
Maximal primal bound violation for  $x^c$  in the integer solution.
- MSK\_DINF\_SOL\_ITG\_PVIOLVAR**  
Maximal primal bound violation for  $x^x$  in the integer solution.
- MSK\_DINF\_SOL\_ITG\_PVIOLBARVAR**  
Maximal primal bound violation for  $\bar{X}$  in the integer solution.
- MSK\_DINF\_SOL\_ITG\_PVIOLCONES**  
Maximal primal violation for primal conic constraints in the integer solution.
- MSK\_DINF\_SOL\_ITG\_PVIOLITG**  
Maximal violation for the integer constraints in the integer solution.
- MSK\_DINF\_SOL\_ITG\_NRM\_XC**  
Infinity norm of  $x^c$  in the integer solution.
- MSK\_DINF\_SOL\_ITG\_NRM\_XX**  
Infinity norm of  $x^x$  in the integer solution.
- MSK\_DINF\_SOL\_ITG\_NRM\_BARX**  
Infinity norm of  $\bar{X}$  in the integer solution.
- MSK\_DINF\_INTPNT\_FACTOR\_NUM\_FLOPS**  
An estimate of the number of flops used in the factorization.
- MSK\_DINF\_QCQO\_REFORMULATE\_TIME**  
Time spent with conic quadratic reformulation.
- MSK\_DINF\_QCQO\_REFORMULATE\_MAX\_PERTURBATION**  
Maximum absolute diagonal perturbation occurring during the QCQO reformulation.
- MSK\_DINF\_QCQO\_REFORMULATE\_WORST\_CHOLESKY\_DIAG\_SCALING**  
Worst Cholesky diagonal scaling.
- MSK\_DINF\_QCQO\_REFORMULATE\_WORST\_CHOLESKY\_COLUMN\_SCALING**  
Worst Cholesky column scaling.
- MSK\_DINF\_PRIMAL\_REPAIR\_PENALTY\_OBJ**  
The optimal objective value of the penalty function.
- MSKfeaturee**  
License feature
- MSK\_FEATURE\_PTS**  
Base system.
- MSK\_FEATURE\_PTON**  
Nonlinear extension.
- MSKliinfiteme**  
Long integer information items.
- MSK\_LIINF\_MIO\_PRE SOLVED\_ANZ**  
Number of non-zero entries in the constraint matrix of presolved problem.
- MSK\_LIINF\_MIO\_SIMPLEX\_ITER**  
Number of simplex iterations performed by the mixed-integer optimizer.
- MSK\_LIINF\_MIO\_INTPNT\_ITER**  
Number of interior-point iterations performed by the mixed-integer optimizer.
- MSK\_LIINF\_BI\_PRIMAL\_ITER**  
Number of primal pivots performed in the basis identification.

MSK\_LIINF\_BI\_DUAL\_ITER

Number of dual pivots performed in the basis identification.

MSK\_LIINF\_BI\_CLEAN\_PRIMAL\_ITER

Number of primal clean iterations performed in the basis identification.

MSK\_LIINF\_BI\_CLEAN\_PRIMAL\_DUAL\_ITER

Number of primal-dual clean iterations performed in the basis identification.

MSK\_LIINF\_BI\_CLEAN\_DUAL\_ITER

Number of dual clean iterations performed in the basis identification.

MSK\_LIINF\_BI\_CLEAN\_PRIMAL\_DEG\_ITER

Number of primal degenerate clean iterations performed in the basis identification.

MSK\_LIINF\_BI\_CLEAN\_PRIMAL\_DUAL\_SUB\_ITER

Number of primal-dual subproblem clean iterations performed in the basis identification.

MSK\_LIINF\_BI\_CLEAN\_PRIMAL\_DUAL\_DEG\_ITER

Number of primal-dual degenerate clean iterations performed in the basis identification.

MSK\_LIINF\_BI\_CLEAN\_DUAL\_DEG\_ITER

Number of dual degenerate clean iterations performed in the basis identification.

MSK\_LIINF\_INTPNT\_FACTOR\_NUM\_NZ

Number of non-zeros in factorization.

MSK\_LIINF\_RD\_NUMANZ

Number of non-zeros in A that is read.

MSK\_LIINF\_RD\_NUMQNZ

Number of Q non-zeros.

MSK\_LIINF\_MIO\_SIM\_MAXITER\_SETBACKS

Number of times the the simplex optimizer has hit the maximum iteration limit when re-optimizing.

MSKiinfiteme

Integer information items.

MSK\_IINF\_ANA\_PRO\_NUM\_CON

Number of constraints in the problem.

MSK\_IINF\_ANA\_PRO\_NUM\_CON\_LO

Number of constraints with a lower bound and an infinite upper bound.

MSK\_IINF\_ANA\_PRO\_NUM\_CON\_UP

Number of constraints with an upper bound and an infinite lower bound.

MSK\_IINF\_ANA\_PRO\_NUM\_CON\_RA

Number of constraints with finite lower and upper bounds.

MSK\_IINF\_ANA\_PRO\_NUM\_CON\_EQ

Number of equality constraints.

MSK\_IINF\_ANA\_PRO\_NUM\_CON\_FR

Number of unbounded constraints.

MSK\_IINF\_ANA\_PRO\_NUM\_VAR

Number of variables in the problem.

MSK\_IINF\_ANA\_PRO\_NUM\_VAR\_LO

Number of variables with a lower bound and an infinite upper bound.

MSK\_IINF\_ANA\_PRO\_NUM\_VAR\_UP

Number of variables with an upper bound and an infinite lower bound. This value is set by

MSK\_IINF\_ANA\_PRO\_NUM\_VAR\_RA

Number of variables with finite lower and upper bounds.

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MSK_IINF_ANA_PRO_NUM_VAR_EQ	Number of fixed variables.
MSK_IINF_ANA_PRO_NUM_VAR_FR	Number of free variables.
MSK_IINF_ANA_PRO_NUM_VAR_CONT	Number of continuous variables.
MSK_IINF_ANA_PRO_NUM_VAR_BIN	Number of binary (0-1) variables.
MSK_IINF_ANA_PRO_NUM_VAR_INT	Number of general integer variables.
MSK_IINF_OPTIMIZE_RESPONSE	The response code returned by optimize.
MSK_IINF_INTPNT_ITER	Number of interior-point iterations since invoking the interior-point optimizer.
MSK_IINF_INTPNT_FACTOR_DIM_DENSE	Dimension of the dense sub system in factorization.
MSK_IINF_INTPNT_SOLVE_DUAL	Non-zero if the interior-point optimizer is solving the dual problem.
MSK_IINF_MIO_NODE_DEPTH	Depth of the last node solved.
MSK_IINF_MIO_NUMCON	Number of constraints in the problem solved by the mixed-integer optimizer.
MSK_IINF_MIO_NUMVAR	Number of variables in the problem solved by the mixed-integer optimizer.
MSK_IINF_MIO_NUMINT	Number of integer variables in the problem solved by the mixed-integer optimizer.
MSK_IINF_MIO_PRE SOLVED_NUMCONT	Number of continuous variables in the problem solved by the mixed-integer optimizer.
MSK_IINF_MIO_PRE SOLVED_NUMBIN	Number of binary variables in the problem solved by the mixed-integer optimizer.
MSK_IINF_MIO_PRE SOLVED_NUMCON	Number of constraints in the presolved problem.
MSK_IINF_MIO_PRE SOLVED_NUMVAR	Number of variables in the presolved problem.
MSK_IINF_MIO_PRE SOLVED_NUMINT	Number of integer variables in the presolved problem.
MSK_IINF_MIO_CLIQUETABLE_SIZE	Size of the clique table.
MSK_IINF_MIO_CONSTRUCT_SOLUTION	If this item has the value 0, then <b>MOSEK</b> did not try to construct an initial integer feasible solution. If the item has a positive value, then <b>MOSEK</b> successfully constructed an initial integer feasible solution.
MSK_IINF_MIO_CONSTRUCT_NUM_ROUNDINGS	Number of values in the integer solution that is rounded to an integer value.
MSK_IINF_MIO_NUM_INT_SOLUTIONS	Number of integer feasible solutions that has been found.

`MSK_IINF_MIO_OBJ_BOUND_DEFINED`  
Non-zero if a valid objective bound has been found, otherwise zero.

`MSK_IINF_MIO_NUM_ACTIVE_NODES`  
Number of active branch bound nodes.

`MSK_IINF_MIO_NUM_RELAX`  
Number of relaxations solved during the optimization.

`MSK_IINF_MIO_NUM_BRANCH`  
Number of branches performed during the optimization.

`MSK_IINF_MIO_TOTAL_NUM_CUTS`  
Total number of cuts generated by the mixed-integer optimizer.

`MSK_IINF_MIO_NUM_CMIR_CUTS`  
Number of Complemented Mixed Integer Rounding (CMIR) cuts.

`MSK_IINF_MIO_NUM_CLIQUE_CUTS`  
Number of clique cuts.

`MSK_IINF_MIO_NUM_IMPLIED_BOUND_CUTS`  
Number of implied bound cuts.

`MSK_IINF_MIO_NUM_KNAPSACK_COVER_CUTS`  
Number of clique cuts.

`MSK_IINF_MIO_NUM_GOMORY_CUTS`  
Number of Gomory cuts.

`MSK_IINF_MIO_NUM_REPEATED_PRESOLVE`  
Number of times presolve was repeated at root.

`MSK_IINF_MIO_INITIAL_SOLUTION`  
Is non-zero if an initial integer solution is specified.

`MSK_IINF_MIO_USER_OBJ_CUT`  
If it is non-zero, then the objective cut is used.

`MSK_IINF_MIO_RELGAP_SATISFIED`  
Non-zero if relative gap is within tolerances.

`MSK_IINF_MIO_ABSGAP_SATISFIED`  
Non-zero if absolute gap is within tolerances.

`MSK_IINF_MIO_NEAR_RELGAP_SATISFIED`  
Non-zero if relative gap is within relaxed tolerances.

`MSK_IINF_MIO_NEAR_ABSGAP_SATISFIED`  
Non-zero if absolute gap is within relaxed tolerances.

`MSK_IINF_RD_PROTOTYPE`  
Problem type.

`MSK_IINF_RD_NUMCON`  
Number of constraints read.

`MSK_IINF_RD_NUMVAR`  
Number of variables read.

`MSK_IINF_RD_NUMBARVAR`  
Number of variables read.

`MSK_IINF_RD_NUMINTVAR`  
Number of integer-constrained variables read.

`MSK_IINF_RD_NUMQ`  
Number of nonempty Q matrices read.



**MSK\_IINF\_SIM\_DUAL\_DEG\_ITER**  
The number of dual degenerate iterations.

**MSK\_IINF\_SIM\_DUAL\_INF\_ITER**  
The number of iterations taken with dual infeasibility.

**MSK\_IINF\_SIM\_DUAL\_HOTSTART\_LU**  
If 1 then a valid basis factorization of full rank was located and used by the dual simplex algorithm.

**MSK\_IINF\_SIM\_PRIMAL\_ITER**  
Number of primal simplex iterations during the last optimization.

**MSK\_IINF\_SIM\_DUAL\_ITER**  
Number of dual simplex iterations during the last optimization.

**MSK\_IINF\_SIM\_PRIMAL\_DUAL\_ITER**  
Number of primal dual simplex iterations during the last optimization.

**MSK\_IINF\_INTPNT\_NUM\_THREADS**  
Number of threads that the interior-point optimizer is using.

**MSK\_IINF\_SIM\_PRIMAL\_INF\_ITER**  
The number of iterations taken with primal infeasibility.

**MSK\_IINF\_SIM\_PRIMAL\_DUAL\_INF\_ITER**  
The number of master iterations with dual infeasibility taken by the primal dual simplex algorithm.

**MSK\_IINF\_SIM\_PRIMAL\_DEG\_ITER**  
The number of primal degenerate iterations.

**MSK\_IINF\_SIM\_PRIMAL\_DUAL\_DEG\_ITER**  
The number of degenerate major iterations taken by the primal dual simplex algorithm.

**MSK\_IINF\_SIM\_PRIMAL\_HOTSTART**  
If 1 then the primal simplex algorithm is solving from an advanced basis.

**MSK\_IINF\_SIM\_PRIMAL\_HOTSTART\_LU**  
If 1 then a valid basis factorization of full rank was located and used by the primal simplex algorithm.

**MSK\_IINF\_SIM\_DUAL\_HOTSTART**  
If 1 then the dual simplex algorithm is solving from an advanced basis.

**MSK\_IINF\_SIM\_PRIMAL\_DUAL\_HOTSTART**  
If 1 then the primal dual simplex algorithm is solving from an advanced basis.

**MSK\_IINF\_SIM\_PRIMAL\_DUAL\_HOTSTART\_LU**  
If 1 then a valid basis factorization of full rank was located and used by the primal dual simplex algorithm.

**MSK\_IINF\_SOL\_ITR\_PROSTA**  
Problem status of the interior-point solution. Updated after each optimization.

**MSK\_IINF\_SOL\_ITR\_SOLSTA**  
Solution status of the interior-point solution. Updated after each optimization.

**MSK\_IINF\_SOL\_BAS\_PROSTA**  
Problem status of the basic solution. Updated after each optimization.

**MSK\_IINF\_SOL\_BAS\_SOLSTA**  
Solution status of the basic solution. Updated after each optimization.

**MSK\_IINF\_SOL\_ITG\_PROSTA**  
Problem status of the integer solution. Updated after each optimization.

**MSK\_IINF\_SOL\_ITG\_SOLSTA**  
Solution status of the integer solution. Updated after each optimization.

MSK\_IINF\_SIM\_NUMCON

Number of constraints in the problem solved by the simplex optimizer.

MSK\_IINF\_SIM\_NUMVAR

Number of variables in the problem solved by the simplex optimizer.

MSK\_IINF\_OPT\_NUMCON

Number of constraints in the problem solved when the optimizer is called.

MSK\_IINF\_OPT\_NUMVAR

Number of variables in the problem solved when the optimizer is called

MSK\_IINF\_STO\_NUM\_A\_REALLOC

Number of times the storage for storing  $A$  has been changed. A large value may indicate that memory fragmentation may occur.

MSK\_IINF\_RD\_NUMCONE

Number of conic constraints read.

MSK\_IINF\_SIM\_SOLVE\_DUAL

Is non-zero if dual problem is solved.

#### MSKinfypee

Information item types

MSK\_INF\_DOU\_TYPE

Is a double information type.

MSK\_INF\_INT\_TYPE

Is an integer.

MSK\_INF\_LINT\_TYPE

Is a long integer.

#### MSKiomodee

Input/output modes

MSK\_IOMODE\_READ

The file is read-only.

MSK\_IOMODE\_WRITE

The file is write-only. If the file exists then it is truncated when it is opened. Otherwise it is created when it is opened.

MSK\_IOMODE\_READWRITE

The file is to read and written.

#### MSKbranchdire

Specifies the branching direction.

MSK\_BRANCH\_DIR\_FREE

The mixed-integer optimizer decides which branch to choose.

MSK\_BRANCH\_DIR\_UP

The mixed-integer optimizer always chooses the up branch first.

MSK\_BRANCH\_DIR\_DOWN

The mixed-integer optimizer always chooses the down branch first.

MSK\_BRANCH\_DIR\_NEAR

Branch in direction nearest to selected fractional variable.

MSK\_BRANCH\_DIR\_FAR

Branch in direction farthest from selected fractional variable.

MSK\_BRANCH\_DIR\_ROOT\_LP

Chose direction based on root lp value of selected variable.

MSK\_BRANCH\_DIR\_GUIDED

Branch in direction of current incumbent.

MSK\_BRANCH\_DIR\_PSEUDOCOST

Branch based on the pseudocost of the variable.

MSKmiocontsoltypee

Continuous mixed-integer solution type

MSK\_MIO\_CONT\_SOL\_NONE

No interior-point or basic solution are reported when the mixed-integer optimizer is used.

MSK\_MIO\_CONT\_SOL\_ROOT

The reported interior-point and basic solutions are a solution to the root node problem when mixed-integer optimizer is used.

MSK\_MIO\_CONT\_SOL\_ITG

The reported interior-point and basic solutions are a solution to the problem with all integer variables fixed at the value they have in the integer solution. A solution is only reported in case the problem has a primal feasible solution.

MSK\_MIO\_CONT\_SOL\_ITG\_REL

In case the problem is primal feasible then the reported interior-point and basic solutions are a solution to the problem with all integer variables fixed at the value they have in the integer solution. If the problem is primal infeasible, then the solution to the root node problem is reported.

MSKmiomodee

Integer restrictions

MSK\_MIO\_MODE\_IGNORED

The integer constraints are ignored and the problem is solved as a continuous problem.

MSK\_MIO\_MODE\_SATISFIED

Integer restrictions should be satisfied.

MSKmionodeseltypee

Mixed-integer node selection types

MSK\_MIO\_NODE\_SELECTION\_FREE

The optimizer decides the node selection strategy.

MSK\_MIO\_NODE\_SELECTION\_FIRST

The optimizer employs a depth first node selection strategy.

MSK\_MIO\_NODE\_SELECTION\_BEST

The optimizer employs a best bound node selection strategy.

MSK\_MIO\_NODE\_SELECTION\_WORST

The optimizer employs a worst bound node selection strategy.

MSK\_MIO\_NODE\_SELECTION\_HYBRID

The optimizer employs a hybrid strategy.

MSK\_MIO\_NODE\_SELECTION\_PSEUDO

The optimizer employs selects the node based on a pseudo cost estimate.

MSKmpsformate

MPS file format type

MSK\_MPS\_FORMAT\_STRICT

It is assumed that the input file satisfies the MPS format strictly.

MSK\_MPS\_FORMAT\_RELAXED

It is assumed that the input file satisfies a slightly relaxed version of the MPS format.

**MSK\_MPS\_FORMAT\_FREE**

It is assumed that the input file satisfies the free MPS format. This implies that spaces are not allowed in names. Otherwise the format is free.

**MSK\_MPS\_FORMAT\_CPLEX**

The CPLEX compatible version of the MPS format is employed.

**MSKmsgkeye**

Message keys

**MSK\_MSG\_READING\_FILE****MSK\_MSG\_WRITING\_FILE****MSK\_MSG\_MPS\_SELECTED****MSKobjsensee**

Objective sense types

**MSK\_OBJECTIVE\_SENSE\_MINIMIZE**

The problem should be minimized.

**MSK\_OBJECTIVE\_SENSE\_MAXIMIZE**

The problem should be maximized.

**MSKonoffkeye**

On/off

**MSK\_ON**

Switch the option on.

**MSK\_OFF**

Switch the option off.

**MSKoptimizertypee**

Optimizer types

**MSK\_OPTIMIZER\_FREE**

The optimizer is chosen automatically.

**MSK\_OPTIMIZER\_INTPNT**

The interior-point optimizer is used.

**MSK\_OPTIMIZER\_CONIC**

The optimizer for problems having conic constraints.

**MSK\_OPTIMIZER\_PRIMAL\_SIMPLEX**

The primal simplex optimizer is used.

**MSK\_OPTIMIZER\_DUAL\_SIMPLEX**

The dual simplex optimizer is used.

**MSK\_OPTIMIZER\_FREE\_SIMPLEX**

One of the simplex optimizers is used.

**MSK\_OPTIMIZER\_MIXED\_INT**

The mixed-integer optimizer.

**MSKorderingtypee**

Ordering strategies

**MSK\_ORDER\_METHOD\_FREE**

The ordering method is chosen automatically.

**MSK\_ORDER\_METHOD\_APPMINLOC**

Approximate minimum local fill-in ordering is employed.

**MSK\_ORDER\_METHOD\_EXPERIMENTAL**

This option should not be used.

MSK\_ORDER\_METHOD\_TRY\_GRAPHPAR

Always try the graph partitioning based ordering.

MSK\_ORDER\_METHOD\_FORCE\_GRAPHPAR

Always use the graph partitioning based ordering even if it is worse than the approximate minimum local fill ordering.

MSK\_ORDER\_METHOD\_NONE

No ordering is used.

MSKpresolvemodee

Presolve method.

MSK\_PRESOLVE\_MODE\_OFF

The problem is not presolved before it is optimized.

MSK\_PRESOLVE\_MODE\_ON

The problem is presolved before it is optimized.

MSK\_PRESOLVE\_MODE\_FREE

It is decided automatically whether to presolve before the problem is optimized.

MSKparametertypee

Parameter type

MSK\_PAR\_INVALID\_TYPE

Not a valid parameter.

MSK\_PAR\_DOU\_TYPE

Is a double parameter.

MSK\_PAR\_INT\_TYPE

Is an integer parameter.

MSK\_PAR\_STR\_TYPE

Is a string parameter.

MSKproblemiteme

Problem data items

MSK\_PI\_VAR

Item is a variable.

MSK\_PI\_CON

Item is a constraint.

MSK\_PI\_CONE

Item is a cone.

MSKproblemtypede

Problem types

MSK\_PROBTYPE\_LO

The problem is a linear optimization problem.

MSK\_PROBTYPE\_QO

The problem is a quadratic optimization problem.

MSK\_PROBTYPE\_QCQO

The problem is a quadratically constrained optimization problem.

MSK\_PROBTYPE\_GECO

General convex optimization.

MSK\_PROBTYPE\_CONIC

A conic optimization.

**MSK\_PROBTYPE\_MIXED**

General nonlinear constraints and conic constraints. This combination can not be solved by **MOSEK**.

**MSKprostae**

Problem status keys

**MSK\_PRO\_STA\_UNKNOWN**

Unknown problem status.

**MSK\_PRO\_STA\_PRIM\_AND\_DUAL\_FEAS**

The problem is primal and dual feasible.

**MSK\_PRO\_STA\_PRIM\_FEAS**

The problem is primal feasible.

**MSK\_PRO\_STA\_DUAL\_FEAS**

The problem is dual feasible.

**MSK\_PRO\_STA\_NEAR\_PRIM\_AND\_DUAL\_FEAS**

The problem is at least nearly primal and dual feasible.

**MSK\_PRO\_STA\_NEAR\_PRIM\_FEAS**

The problem is at least nearly primal feasible.

**MSK\_PRO\_STA\_NEAR\_DUAL\_FEAS**

The problem is at least nearly dual feasible.

**MSK\_PRO\_STA\_PRIM\_INFEAS**

The problem is primal infeasible.

**MSK\_PRO\_STA\_DUAL\_INFEAS**

The problem is dual infeasible.

**MSK\_PRO\_STA\_PRIM\_AND\_DUAL\_INFEAS**

The problem is primal and dual infeasible.

**MSK\_PRO\_STA\_ILL\_POSED**

The problem is ill-posed. For example, it may be primal and dual feasible but have a positive duality gap.

**MSK\_PRO\_STA\_PRIM\_INFEAS\_OR\_UNBOUNDED**

The problem is either primal infeasible or unbounded. This may occur for mixed-integer problems.

**MSKxmlwriteroutputtypee**

XML writer output mode

**MSK\_WRITE\_XML\_MODE\_ROW**

Write in row order.

**MSK\_WRITE\_XML\_MODE\_COL**

Write in column order.

**MSKrescodetypee**

Response code type

**MSK\_RESPONSE\_OK**

The response code is OK.

**MSK\_RESPONSE\_WRN**

The response code is a warning.

**MSK\_RESPONSE\_TRM**

The response code is an optimizer termination status.

**MSK\_RESPONSE\_ERR**

The response code is an error.

MSK\_RESPONSE\_UNK

The response code does not belong to any class.

MSKscalingtypee

Scaling type

MSK\_SCALING\_FREE

The optimizer chooses the scaling heuristic.

MSK\_SCALING\_NONE

No scaling is performed.

MSK\_SCALING\_MODERATE

A conservative scaling is performed.

MSK\_SCALING\_AGGRESSIVE

A very aggressive scaling is performed.

MSKscalingmethode

Scaling method

MSK\_SCALING\_METHOD\_POW2

Scales only with power of 2 leaving the mantissa untouched.

MSK\_SCALING\_METHOD\_FREE

The optimizer chooses the scaling heuristic.

MSKsensitivitytypee

Sensitivity types

MSK\_SENSITIVITY\_TYPE\_BASIS

Basis sensitivity analysis is performed.

MSK\_SENSITIVITY\_TYPE\_OPTIMAL\_PARTITION

Optimal partition sensitivity analysis is performed.

MSKsimseltypee

Simplex selection strategy

MSK\_SIM\_SELECTION\_FREE

The optimizer chooses the pricing strategy.

MSK\_SIM\_SELECTION\_FULL

The optimizer uses full pricing.

MSK\_SIM\_SELECTION\_ASE

The optimizer uses approximate steepest-edge pricing.

MSK\_SIM\_SELECTION\_DEVEX

The optimizer uses devex steepest-edge pricing (or if it is not available an approximate steep-edge selection).

MSK\_SIM\_SELECTION\_SE

The optimizer uses steepest-edge selection (or if it is not available an approximate steep-edge selection).

MSK\_SIM\_SELECTION\_PARTIAL

The optimizer uses a partial selection approach. The approach is usually beneficial if the number of variables is much larger than the number of constraints.

MSKsoliteme

Solution items

MSK\_SOL\_ITEM\_XC

Solution for the constraints.

MSK\_SOL\_ITEM\_XX

Variable solution.

MSK\_SOL\_ITEM\_Y  
Lagrange multipliers for equations.

MSK\_SOL\_ITEM\_SLC  
Lagrange multipliers for lower bounds on the constraints.

MSK\_SOL\_ITEM\_SUC  
Lagrange multipliers for upper bounds on the constraints.

MSK\_SOL\_ITEM\_SLX  
Lagrange multipliers for lower bounds on the variables.

MSK\_SOL\_ITEM\_SUX  
Lagrange multipliers for upper bounds on the variables.

MSK\_SOL\_ITEM\_SNX  
Lagrange multipliers corresponding to the conic constraints on the variables.

**MSKsolstae**

Solution status keys

MSK\_SOL\_STA\_UNKNOWN  
Status of the solution is unknown.

MSK\_SOL\_STA\_OPTIMAL  
The solution is optimal.

MSK\_SOL\_STA\_PRIM\_FEAS  
The solution is primal feasible.

MSK\_SOL\_STA\_DUAL\_FEAS  
The solution is dual feasible.

MSK\_SOL\_STA\_PRIM\_AND\_DUAL\_FEAS  
The solution is both primal and dual feasible.

MSK\_SOL\_STA\_NEAR\_OPTIMAL  
The solution is nearly optimal.

MSK\_SOL\_STA\_NEAR\_PRIM\_FEAS  
The solution is nearly primal feasible.

MSK\_SOL\_STA\_NEAR\_DUAL\_FEAS  
The solution is nearly dual feasible.

MSK\_SOL\_STA\_NEAR\_PRIM\_AND\_DUAL\_FEAS  
The solution is nearly both primal and dual feasible.

MSK\_SOL\_STA\_PRIM\_INFEAS\_CER  
The solution is a certificate of primal infeasibility.

MSK\_SOL\_STA\_DUAL\_INFEAS\_CER  
The solution is a certificate of dual infeasibility.

MSK\_SOL\_STA\_NEAR\_PRIM\_INFEAS\_CER  
The solution is almost a certificate of primal infeasibility.

MSK\_SOL\_STA\_NEAR\_DUAL\_INFEAS\_CER  
The solution is almost a certificate of dual infeasibility.

MSK\_SOL\_STA\_PRIM\_ILLPOSED\_CER  
The solution is a certificate that the primal problem is illposed.

MSK\_SOL\_STA\_DUAL\_ILLPOSED\_CER  
The solution is a certificate that the dual problem is illposed.

MSK\_SOL\_STA\_INTEGER\_OPTIMAL  
The primal solution is integer optimal.



MSK\_SOL\_STA\_NEAR\_INTEGER\_OPTIMAL

The primal solution is near integer optimal.

**MSKsoltypee**

Solution types

MSK\_SOL\_BAS

The basic solution.

MSK\_SOL\_ITR

The interior solution.

MSK\_SOL\_ITG

The integer solution.

**MSKsolveforme**

Solve primal or dual form

MSK\_SOLVE\_FREE

The optimizer is free to solve either the primal or the dual problem.

MSK\_SOLVE\_PRIMAL

The optimizer should solve the primal problem.

MSK\_SOLVE\_DUAL

The optimizer should solve the dual problem.

**MSKstakeye**

Status keys

MSK\_SK\_UNK

The status for the constraint or variable is unknown.

MSK\_SK\_BAS

The constraint or variable is in the basis.

MSK\_SK\_SUPBAS

The constraint or variable is super basic.

MSK\_SK\_LOW

The constraint or variable is at its lower bound.

MSK\_SK\_UPR

The constraint or variable is at its upper bound.

MSK\_SK\_FIX

The constraint or variable is fixed.

MSK\_SK\_INF

The constraint or variable is infeasible in the bounds.

**MSKstartpointtypee**

Starting point types

MSK\_STARTING\_POINT\_FREE

The starting point is chosen automatically.

MSK\_STARTING\_POINT\_GUESS

The optimizer guesses a starting point.

MSK\_STARTING\_POINT\_CONSTANT

The optimizer constructs a starting point by assigning a constant value to all primal and dual variables. This starting point is normally robust.

MSK\_STARTING\_POINT\_SATISFY\_BOUNDS

The starting point is chosen to satisfy all the simple bounds on nonlinear variables. If this starting point is employed, then more care than usual should be employed when choosing the bounds on the nonlinear variables. In particular very tight bounds should be avoided.

MSKstreamtypee

Stream types

MSK\_STREAM\_LOG

Log stream. Contains the aggregated contents of all other streams. This means that a message written to any other stream will also be written to this stream.

MSK\_STREAM\_MSG

Message stream. Log information relating to performance and progress of the optimization is written to this stream.

MSK\_STREAM\_ERR

Error stream. Error messages are written to this stream.

MSK\_STREAM\_WRN

Warning stream. Warning messages are written to this stream.

MSKvaluee

Integer values

MSK\_MAX\_STR\_LEN

Maximum string length allowed in **MOSEK**.

MSK\_LICENSE\_BUFFER\_LENGTH

The length of a license key buffer.

MSKvariabletypee

Variable types

MSK\_VAR\_TYPE\_CONT

Is a continuous variable.

MSK\_VAR\_TYPE\_INT

Is an integer variable.

## SUPPORTED FILE FORMATS

**MOSEK** supports a range of problem and solution formats listed in [Table 12.1](#) and [Table 12.2](#). The **Task format** is **MOSEK**'s native binary format and it supports all features that **MOSEK** supports. The **OPF format** is **MOSEK**'s human-readable alternative that supports nearly all features (everything except semidefinite problems). In general, text formats are significantly slower to read, but can be examined and edited directly in any text editor.

### Problem formats

See [Table 12.1](#).

Table 12.1: List of supported file formats for optimization problems.

Format Type	Ext.	Binary/Text	LP	QP	CQO	SDP
<i>LP</i>	lp	plain text	X	X		
<i>MPS</i>	mps	plain text	X	X		
<i>OPF</i>	opf	plain text	X	X	X	
<i>CBF</i>	cbf	plain text	X		X	X
<i>Osil</i>	xml	xml text	X	X		
<i>Task format</i>	task	binary	X	X	X	X
<i>Jtask format</i>	jtask	text	X	X	X	X

### Solution formats

See [Table 12.2](#).

Table 12.2: List of supported solution formats.

Format Type	Ext.	Binary/Text	Description
<i>SOL</i>	sol	plain text	Interior Solution
	bas	plain text	Basic Solution
	int	plain text	Integer
<i>Jsol format</i>	jsol	text	Solution

### Compression

**MOSEK** supports GZIP compression of files. Problem files with an additional `.gz` extension are assumed to be compressed when read, and are automatically compressed when written. For example, a file called

problem.mps.gz

will be considered as a GZIP compressed MPS file.

## 12.1 The LP File Format

**MOSEK** supports the LP file format with some extensions. The LP format is not a completely well-defined standard and hence different optimization packages may interpret the same LP file in slightly different ways. **MOSEK** tries to emulate as closely as possible CPLEX's behavior, but tries to stay backward compatible.

The LP file format can specify problems on the form

$$\begin{array}{llll} \text{minimize/maximize} & & c^T x + \frac{1}{2} q^o(x) & \\ \text{subject to} & l^c \leq & Ax + \frac{1}{2} q(x) & \leq u^c, \\ & l^x \leq & x & \leq u^x, \\ & & x_{\mathcal{J}} & \text{integer,} \end{array}$$

where

- $x \in \mathbb{R}^n$  is the vector of decision variables.
- $c \in \mathbb{R}^n$  is the linear term in the objective.
- $q^o : \mathbb{R}^n \rightarrow \mathbb{R}$  is the quadratic term in the objective where

$$q^o(x) = x^T Q^o x$$

and it is assumed that

$$Q^o = (Q^o)^T.$$

- $A \in \mathbb{R}^{m \times n}$  is the constraint matrix.
- $l^c \in \mathbb{R}^m$  is the lower limit on the activity for the constraints.
- $u^c \in \mathbb{R}^m$  is the upper limit on the activity for the constraints.
- $l^x \in \mathbb{R}^n$  is the lower limit on the activity for the variables.
- $u^x \in \mathbb{R}^n$  is the upper limit on the activity for the variables.
- $q : \mathbb{R}^n \rightarrow \mathbb{R}$  is a vector of quadratic functions. Hence,

$$q_i(x) = x^T Q^i x$$

where it is assumed that

$$Q^i = (Q^i)^T.$$

- $\mathcal{J} \subseteq \{1, 2, \dots, n\}$  is an index set of the integer constrained variables.

### 12.1.1 File Sections

An LP formatted file contains a number of sections specifying the objective, constraints, variable bounds, and variable types. The section keywords may be any mix of upper and lower case letters.

#### Objective Function

The first section beginning with one of the keywords

```
max
maximum
maximize
min
minimum
minimize
```

defines the objective sense and the objective function, i.e.

$$c^T x + \frac{1}{2} x^T Q^o x.$$

The objective may be given a name by writing

```
myname:
```

before the expressions. If no name is given, then the objective is named `obj`.

The objective function contains linear and quadratic terms. The linear terms are written as:

```
4 x1 + x2 - 0.1 x3
```

and so forth. The quadratic terms are written in square brackets ( `[ ]` ) and are either squared or multiplied as in the examples

```
x1^2
```

and

```
x1 * x2
```

There may be zero or more pairs of brackets containing quadratic expressions.

An example of an objective section is

```
minimize
myobj: 4 x1 + x2 - 0.1 x3 + [ x1^2 + 2.1 x1 * x2 ]/2
```

Please note that the quadratic expressions are multiplied with  $\frac{1}{2}$ , so that the above expression means

$$\text{minimize } 4x_1 + x_2 - 0.1 \cdot x_3 + \frac{1}{2}(x_1^2 + 2.1 \cdot x_1 \cdot x_2)$$

If the same variable occurs more than once in the linear part, the coefficients are added, so that `4 x1 + 2 x1` is equivalent to `6 x1`. In the quadratic expressions `x1 * x2` is equivalent to `x2 * x1` and, as in the linear part, if the same variables multiplied or squared occur several times their coefficients are added.

## Constraints

The second section beginning with one of the keywords

```
subj to
subject to
s.t.
st
```

defines the linear constraint matrix  $A$  and the quadratic matrices  $Q^i$ .

A constraint contains a name (optional), expressions adhering to the same rules as in the objective and a bound:

```
subject to
con1: x1 + x2 + [ x3^2 ]/2 <= 5.1
```

The bound type (here  $\leq$ ) may be any of  $<$ ,  $\leq$ ,  $=$ ,  $>$ ,  $\geq$  ( $<$  and  $\leq$  mean the same), and the bound may be any number.

In the standard LP format it is not possible to define more than one bound, but **MOSEK** supports defining ranged constraints by using double-colon ( $::$ ) instead of a single-colon ( $:$ ) after the constraint name, i.e.

$$-5 \leq x_1 + x_2 \leq 5 \quad (12.1)$$

may be written as

```
con:: -5 < x_1 + x_2 < 5
```

By default **MOSEK** writes ranged constraints this way.

If the files must adhere to the LP standard, ranged constraints must either be split into upper bounded and lower bounded constraints or be written as an equality with a slack variable. For example the expression (12.1) may be written as

$$x_1 + x_2 - sl_1 = 0, \quad -5 \leq sl_1 \leq 5.$$

## Bounds

Bounds on the variables can be specified in the bound section beginning with one of the keywords

```
bound
bounds
```

The bounds section is optional but should, if present, follow the **subject to** section. All variables listed in the bounds section must occur in either the objective or a constraint.

The default lower and upper bounds are 0 and  $+\infty$ . A variable may be declared free with the keyword **free**, which means that the lower bound is  $-\infty$  and the upper bound is  $+\infty$ . Furthermore it may be assigned a finite lower and upper bound. The bound definitions for a given variable may be written in one or two lines, and bounds can be any number or  $\pm\infty$  (written as **+inf/-inf/+infinity/-infinity**) as in the example

```
bounds
x1 free
x2 <= 5
0.1 <= x2
x3 = 42
2 <= x4 < +inf
```

## Variable Types

The final two sections are optional and must begin with one of the keywords

```
bin
binaries
binary
```

and

```
gen
general
```

Under **general** all integer variables are listed, and under **binary** all binary (integer variables with bounds 0 and 1) are listed:

```

general
x1 x2
binary
x3 x4

```

Again, all variables listed in the binary or general sections must occur in either the objective or a constraint.

### Terminating Section

Finally, an LP formatted file must be terminated with the keyword

```
end
```

## 12.1.2 LP File Examples

### Linear example lo1.lp

```

\ File: lo1.lp
maximize
obj: 3 x1 + x2 + 5 x3 + x4
subject to
c1: 3 x1 + x2 + 2 x3 = 30
c2: 2 x1 + x2 + 3 x3 + x4 >= 15
c3: 2 x2 + 3 x4 <= 25
bounds
0 <= x1 <= +infinity
0 <= x2 <= 10
0 <= x3 <= +infinity
0 <= x4 <= +infinity
end

```

### Mixed integer example milo1.lp

```

maximize
obj: x1 + 6.4e-01 x2
subject to
c1: 5e+01 x1 + 3.1e+01 x2 <= 2.5e+02
c2: 3e+00 x1 - 2e+00 x2 >= -4e+00
bounds
0 <= x1 <= +infinity
0 <= x2 <= +infinity
general
x1 x2
end

```

## 12.1.3 LP Format peculiarities

### Comments

Anything on a line after a \ is ignored and is treated as a comment.

## Names

A name for an objective, a constraint or a variable may contain the letters *a-z*, *A-Z*, the digits *0-9* and the characters

`!"#$%&()/,.;?@_'\`|~`

The first character in a name must not be a number, a period or the letter *e* or *E*. Keywords must not be used as names.

**MOSEK** accepts any character as valid for names, except `\0`. A name that is not allowed in LP file will be changed and a warning will be issued.

The algorithm for making names LP valid works as follows: The name is interpreted as an **utf-8** string. For a unicode character *c*:

- If *c*==`_` (underscore), the output is `__` (two underscores).
- If *c* is a valid LP name character, the output is just *c*.
- If *c* is another character in the ASCII range, the output is `_XX`, where *XX* is the hexadecimal code for the character.
- If *c* is a character in the range *127-65535*, the output is `_uXXXX`, where *XXXX* is the hexadecimal code for the character.
- If *c* is a character above 65535, the output is `_UXXXXXXXX`, where *XXXXXXXX* is the hexadecimal code for the character.

Invalid **utf-8** substrings are escaped as `_XX'`, and if a name starts with a period, *e* or *E*, that character is escaped as `_XX`.

## Variable Bounds

Specifying several upper or lower bounds on one variable is possible but **MOSEK** uses only the tightest bounds. If a variable is fixed (with `=`), then it is considered the tightest bound.

## MOSEK Extensions to the LP Format

Some optimization software packages employ a more strict definition of the LP format than the one used by **MOSEK**. The limitations imposed by the strict LP format are the following:

- Quadratic terms in the constraints are not allowed.
- Names can be only 16 characters long.
- Lines must not exceed 255 characters in length.

If an LP formatted file created by **MOSEK** should satisfy the strict definition, then the parameter

- `MSK_IPAR_WRITE_LP_STRICT_FORMAT`

should be set; note, however, that some problems cannot be written correctly as a strict LP formatted file. For instance, all names are truncated to 16 characters and hence they may lose their uniqueness and change the problem.

To get around some of the inconveniences converting from other problem formats, **MOSEK** allows lines to contain 1024 characters and names may have any length (shorter than the 1024 characters).

Internally in **MOSEK** names may contain any (printable) character, many of which cannot be used in LP names. Setting the parameters

- `MSK_IPAR_READ_LP_QUOTED_NAMES` and
- `MSK_IPAR_WRITE_LP_QUOTED_NAMES`



allows **MOSEK** to use quoted names. The first parameter tells **MOSEK** to remove quotes from quoted names e.g, "x1", when reading LP formatted files. The second parameter tells **MOSEK** to put quotes around any semi-illegal name (names beginning with a number or a period) and fully illegal name (containing illegal characters). As double quote is a legal character in the LP format, quoting semi-illegal names makes them legal in the pure LP format as long as they are still shorter than 16 characters. Fully illegal names are still illegal in a pure LP file.

### 12.1.4 The strict LP format

The LP format is not a formal standard and different vendors have slightly different interpretations of the LP format. To make **MOSEK**'s definition of the LP format more compatible with the definitions of other vendors, use the parameter setting

- `MSK_IPAR_WRITE_LP_STRICT_FORMAT = MSK_ON`

This setting may lead to truncation of some names and hence to an invalid LP file. The simple solution to this problem is to use the parameter setting

- `MSK_IPAR_WRITE_GENERIC_NAMES = MSK_ON`

which will cause all names to be renamed systematically in the output file.

### 12.1.5 Formatting of an LP File

A few parameters control the visual formatting of LP files written by **MOSEK** in order to make it easier to read the files. These parameters are

- `MSK_IPAR_WRITE_LP_LINE_WIDTH`
- `MSK_IPAR_WRITE_LP_TERMS_PER_LINE`

The first parameter sets the maximum number of characters on a single line. The default value is 80 corresponding roughly to the width of a standard text document.

The second parameter sets the maximum number of terms per line; a term means a sign, a coefficient, and a name (for example + 42 elephants). The default value is 0, meaning that there is no maximum.

### Unnamed Constraints

Reading and writing an LP file with **MOSEK** may change it superficially. If an LP file contains unnamed constraints or objective these are given their generic names when the file is read (however unnamed constraints in **MOSEK** are written without names).

## 12.2 The MPS File Format

**MOSEK** supports the standard MPS format with some extensions. For a detailed description of the MPS format see the book by Nazareth [Naz87].

### 12.2.1 MPS File Structure

The version of the MPS format supported by **MOSEK** allows specification of an optimization problem of the form

$$\begin{aligned} l^c &\leq Ax + q(x) &&\leq u^c, \\ l^x &\leq x &&\leq u^x, \\ &x \in \mathcal{K}, \\ &x_{\mathcal{J}} \text{ integer}, \end{aligned} \tag{12.2}$$

where

- $x \in \mathbb{R}^n$  is the vector of decision variables.
- $A \in \mathbb{R}^{m \times n}$  is the constraint matrix.
- $l^c \in \mathbb{R}^m$  is the lower limit on the activity for the constraints.
- $u^c \in \mathbb{R}^m$  is the upper limit on the activity for the constraints.
- $l^x \in \mathbb{R}^n$  is the lower limit on the activity for the variables.
- $u^x \in \mathbb{R}^n$  is the upper limit on the activity for the variables.
- $q : \mathbb{R}^n \rightarrow \mathbb{R}$  is a vector of quadratic functions. Hence,

$$q_i(x) = \frac{1}{2} x^T Q^i x$$

where it is assumed that

$$Q^i = (Q^i)^T.$$

Please note the explicit  $\frac{1}{2}$  in the quadratic term and that  $Q^i$  is required to be symmetric.

- $\mathcal{K}$  is a convex cone.
- $\mathcal{J} \subseteq \{1, 2, \dots, n\}$  is an index set of the integer-constrained variables.

An MPS file with one row and one column can be illustrated like this:

```
*          1          2          3          4          5          6
*23456789012345678901234567890123456789012345678901234567890
NAME          [name]
OBJSENSE
[objsense]
OBJNAME
[objname]
ROWS
? [cname1]
COLUMNS
[vname1] [cname1] [value1] [vname3] [value2]
RHS
[name] [cname1] [value1] [cname2] [value2]
RANGES
[name] [cname1] [value1] [cname2] [value2]
QSECTION      [cname1]
[vname1] [vname2] [value1] [vname3] [value2]
QMATRIX
[vname1] [vname2] [value1]
QUADOBJ
[vname1] [vname2] [value1]
QCMATRIX      [cname1]
[vname1] [vname2] [value1]
BOUNDS
?? [name] [vname1] [value1]
CSECTION      [kname1] [value1] [ktype]
[vname1]
ENDATA
```

Here the names in capitals are keywords of the MPS format and names in brackets are custom defined names or values. A couple of notes on the structure:

- Fields: All items surrounded by brackets appear in *fields*. The fields named “valueN” are numerical values. Hence, they must have the format

```
[+|-]XXXXXXXX.XXXXXX[[e|E][+|-]XXX]
```

where

```
.. code-block:: text
```

```
X = [0|1|2|3|4|5|6|7|8|9].
```

- Sections: The MPS file consists of several sections where the names in capitals indicate the beginning of a new section. For example, COLUMNS denotes the beginning of the columns section.
- Comments: Lines starting with an \* are comment lines and are ignored by **MOSEK**.
- Keys: The question marks represent keys to be specified later.
- Extensions: The sections QSECTION and CSECTION are specific **MOSEK** extensions of the MPS format. The sections QMATRIX, QUADOBJ and QCMATRIX are included for sake of compatibility with other vendors extensions to the MPS format.

The standard MPS format is a fixed format, i.e. everything in the MPS file must be within certain fixed positions. **MOSEK** also supports a *free format*. See Section 12.2.9 for details.

### Linear example lo1.mps

A concrete example of a MPS file is presented below:

```
* File: lo1.mps
NAME          lo1
OBJSENSE
    MAX
ROWS
N   obj
E   c1
G   c2
L   c3
COLUMNS
    x1      obj      3
    x1      c1       3
    x1      c2       2
    x2      obj      1
    x2      c1       1
    x2      c2       1
    x2      c3       2
    x3      obj      5
    x3      c1       2
    x3      c2       3
    x4      obj      1
    x4      c2       1
    x4      c3       3
RHS
    rhs     c1      30
    rhs     c2      15
    rhs     c3      25
RANGES
BOUNDS
UP bound    x2      10
ENDATA
```

Subsequently each individual section in the MPS format is discussed.

### Section NAME

In this section a name ([name]) is assigned to the problem.

**OBJSENSE (optional)**

This is an optional section that can be used to specify the sense of the objective function. The **OBJSENSE** section contains one line at most which can be one of the following

```
MIN
MINIMIZE
MAX
MAXIMIZE
```

It should be obvious what the implication is of each of these four lines.

**OBJNAME (optional)**

This is an optional section that can be used to specify the name of the row that is used as objective function. The **OBJNAME** section contains one line at most which has the form

```
objname
```

`objname` should be a valid row name.

**ROWS**

A record in the **ROWS** section has the form

```
? [cname1]
```

where the requirements for the fields are as follows:

Field	Starting Position	Max Width	required	Description
?	2	1	Yes	Constraint key
[cname1]	5	8	Yes	Constraint name

Hence, in this section each constraint is assigned an unique name denoted by `[cname1]`. Please note that `[cname1]` starts in position 5 and the field can be at most 8 characters wide. An initial key `?` must be present to specify the type of the constraint. The key can have the values E, G, L, or N with the following interpretation:

Constraint type	$l_i^c$	$u_i^c$
E	finite	$l_i^c$
G	finite	$\infty$
L	$-\infty$	finite
N	$-\infty$	$\infty$

In the MPS format an objective vector is not specified explicitly, but one of the constraints having the key N will be used as the objective vector  $c$ . In general, if multiple N type constraints are specified, then the first will be used as the objective vector  $c$ .

**COLUMNS**

In this section the elements of  $A$  are specified using one or more records having the form:

```
[vname1] [cname1] [value1] [cname2] [value2]
```

where the requirements for each field are as follows:

Field	Starting Position	Max Width	required	Description
[vname1]	5	8	Yes	Variable name
[cname1]	15	8	Yes	Constraint name
[value1]	25	12	Yes	Numerical value
[cname2]	40	8	No	Constraint name
[value2]	50	12	No	Numerical value

Hence, a record specifies one or two elements  $a_{ij}$  of  $A$  using the principle that [vname1] and [cname1] determines  $j$  and  $i$  respectively. Please note that [cname1] must be a constraint name specified in the ROWS section. Finally, [value1] denotes the numerical value of  $a_{ij}$ . Another optional element is specified by [cname2], and [value2] for the variable specified by [vname1]. Some important comments are:

- All elements belonging to one variable must be grouped together.
- Zero elements of  $A$  should not be specified.
- At least one element for each variable should be specified.

### RHS (optional)

A record in this section has the format

[name]	[cname1]	[value1]	[cname2]	[value2]
--------	----------	----------	----------	----------

where the requirements for each field are as follows:

Field	Starting Position	Max Width	required	Description
[name]	5	8	Yes	Name of the RHS vector
[cname1]	15	8	Yes	Constraint name
[value1]	25	12	Yes	Numerical value
[cname2]	40	8	No	Constraint name
[value2]	50	12	No	Numerical value

The interpretation of a record is that [name] is the name of the RHS vector to be specified. In general, several vectors can be specified. [cname1] denotes a constraint name previously specified in the ROWS section. Now, assume that this name has been assigned to the  $i$  th constraint and  $v_1$  denotes the value specified by [value1], then the interpretation of  $v_1$  is:

Constraint	$l_i^c$	$u_i^c$
type		
E	$v_1$	$v_1$
G	$v_1$	
L		$v_1$
N		

An optional second element is specified by [cname2] and [value2] and is interpreted in the same way. Please note that it is not necessary to specify zero elements, because elements are assumed to be zero.

### RANGES (optional)

A record in this section has the form

[name]	[cname1]	[value1]	[cname2]	[value2]
--------	----------	----------	----------	----------

where the requirements for each fields are as follows:

Field	Starting Position	Max Width	required	Description
[name]	5	8	Yes	Name of the RANGE vector
[cname1]	15	8	Yes	Constraint name
[value1]	25	12	Yes	Numerical value
[cname2]	40	8	No	Constraint name
[value2]	50	12	No	Numerical value

The records in this section are used to modify the bound vectors for the constraints, i.e. the values in  $l^c$  and  $u^c$ . A record has the following interpretation: [name] is the name of the RANGE vector and [cname1] is a valid constraint name. Assume that [cname1] is assigned to the  $i$  th constraint and let  $v_1$  be the value specified by [value1], then a record has the interpretation:

Constraint type	Sign of $v_1$	$l_i^c$	$u_i^c$
E	—	$u_i^c + v_1$	
E	+		$l_i^c + v_1$
G	— or +	$l_i^c +  v_1 $	
L	— or +	$u_i^c -  v_1 $	
N			

### QSECTION (optional)

Within the QSECTION the label [cname1] must be a constraint name previously specified in the ROWS section. The label [cname1] denotes the constraint to which the quadratic term belongs. A record in the QSECTION has the form

[vname1]	[vname2]	[value1]	[vname3]	[value2]
----------	----------	----------	----------	----------

where the requirements for each field are:

Field	Starting Position	Max Width	required	Description
[vname1]	5	8	Yes	Variable name
[vname2]	15	8	Yes	Variable name
[value1]	25	12	Yes	Numerical value
[vname3]	40	8	No	Variable name
[value2]	50	12	No	Numerical value

A record specifies one or two elements in the lower triangular part of the  $Q^i$  matrix where [cname1] specifies the  $i$ . Hence, if the names [vname1] and [vname2] have been assigned to the  $k$  th and  $j$  th variable, then  $Q_{kj}^i$  is assigned the value given by [value1]. An optional second element is specified in the same way by the fields [vname1], [vname3], and [value2].

The example

$$\begin{array}{ll} \text{minimize} & -x_2 + \frac{1}{2}(2x_1^2 - 2x_1x_3 + 0.2x_2^2 + 2x_3^2) \\ \text{subject to} & x_1 + x_2 + x_3 \geq 1, \\ & x \geq 0 \end{array}$$

has the following MPS file representation

```
* File: qo1.mps
NAME          qo1
ROWS
N  obj
G  c1
COLUMNS
x1      c1      1.0
x2      obj     -1.0
x2      c1      1.0
x3      c1      1.0
RHS
rhs      c1      1.0
QSECTION      obj
x1      x1      2.0
x1      x3     -1.0
x2      x2      0.2
x3      x3      2.0
ENDATA
```

Regarding the QSECTIONS please note that:

- Only one QSECTION is allowed for each constraint.
- The QSECTIONS can appear in an arbitrary order after the COLUMNS section.
- All variable names occurring in the QSECTION must already be specified in the COLUMNS section.
- All entries specified in a QSECTION are assumed to belong to the lower triangular part of the quadratic term of  $Q$ .

### QMATRIX/QUADOBJ (optional)

The QMATRIX and QUADOBJ sections allow to define the quadratic term of the objective function. They differ in how the quadratic term of the objective function is stored:

- QMATRIX It stores all the nonzeros coefficients, without taking advantage of the symmetry of the  $Q$  matrix.
- QUADOBJ It only store the upper diagonal nonzero elements of the  $Q$  matrix.

A record in both sections has the form:

[vname1]	[vname2]	[value1]
----------	----------	----------

where the requirements for each field are:

Field	Starting Position	Max Width	required	Description
[vname1]	5	8	Yes	Variable name
[vname2]	15	8	Yes	Variable name
[value1]	25	12	Yes	Numerical value

A record specifies one elements of the  $Q$  matrix in the objective function. Hence, if the names [vname1] and [vname2] have been assigned to the  $k$ th and  $j$ th variable, then  $Q_{kj}$  is assigned the value given by [value1]. Note that a line must appear for each off-diagonal coefficient if using a QMATRIX section, while only one entry is required in a QUADOBJ section. The quadratic part of the objective function will be evaluated as  $1/2x^T Qx$ .

The example

$$\begin{aligned}
 &\text{minimize} && -x_2 + \frac{1}{2}(2x_1^2 - 2x_1x_3 + 0.2x_2^2 + 2x_3^2) \\
 &\text{subject to} && x_1 + x_2 + x_3 \geq 1, \\
 &&& x \geq 0
 \end{aligned}$$

has the following MPS file representation using QMATRIX

```

* File: qo1_matrix.mps
NAME          qo1_qmatrix
ROWS
  N  obj
  G  c1
COLUMNS
  x1      c1      1.0
  x2      obj     -1.0
  x2      c1      1.0
  x3      c1      1.0
RHS
  rhs     c1      1.0
QMATRIX
  x1      x1      2.0
  x1      x3     -1.0
  x3      x1     -1.0
  x2      x2      0.2
  x3      x3      2.0
ENDATA

```

or the following using QUADOBJ

```
* File: qo1_quadobj.mps
NAME          qo1_quadobj
ROWS
  N  obj
  G  c1
COLUMNS
  x1      c1      1.0
  x2      obj     -1.0
  x2      c1      1.0
  x3      c1      1.0
RHS
  rhs     c1      1.0
QUADOBJ
  x1      x1      2.0
  x1      x3     -1.0
  x2      x2      0.2
  x3      x3      2.0
ENDATA
```

Please also note that:

- A QMATRIX/QUADOBJ section can appear in an arbitrary order after the COLUMNS section.
- All variable names occurring in the QMATRIX/QUADOBJ section must already be specified in the COLUMNS section.

### 12.2.2 QCMATRIX (optional)

A QCMATRIX section allows to specify the quadratic part of a given constraints. Within the QCMATRIX the label [cname1] must be a constraint name previously specified in the ROWS section. The label [cname1] denotes the constraint to which the quadratic term belongs. A record in the QSECTION has the form

[vname1]	[vname2]	[value1]
----------	----------	----------

where the requirements for each field are:

Field	Starting Position	Max Width	required	Description
[vname1]	5	8	Yes	Variable name
[vname2]	15	8	Yes	Variable name
[value1]	25	12	Yes	Numerical value

A record specifies an entry of the  $Q^i$  matrix where [cname1] specifies the  $i$ . Hence, if the names [vname1] and [vname2] have been assigned to the  $k$  th and  $j$  th variable, then  $Q_{kj}^i$  is assigned the value given by [value1]. Moreover, the quadratic term is represented as  $1/2x^T Qx$ .

The example

$$\begin{array}{ll}
 \text{minimize} & x_2 \\
 \text{subject to} & x_1 + x_2 + x_3 \geq 1, \\
 & \frac{1}{2}(-2x_1x_3 + 0.2x_2^2 + 2x_3^2) \leq 10, \\
 & x \geq 0
 \end{array}$$

has the following MPS file representation

```
* File: qo1.mps
NAME          qo1
ROWS
  N  obj
  G  c1
  L  q1
COLUMNS
```



x1	c1	1.0
x2	obj	-1.0
x2	c1	1.0
x3	c1	1.0
RHS		
rhs	c1	1.0
rhs	q1	10.0
QCMATRIX		
	q1	
x1	x1	2.0
x1	x3	-1.0
x3	x1	-1.0
x2	x2	0.2
x3	x3	2.0
ENDATA		

Regarding the QCMATRIXs please note that:

- Only one QCMATRIX is allowed for each constraint.
- The QCMATRIXs can appear in an arbitrary order after the COLUMNS section.
- All variable names occurring in the QSECTION must already be specified in the COLUMNS section.
- A QCMATRIX does not exploit the symmetry of  $Q$ : an off-diagonal entry  $(i, j)$  should appear twice.

### 12.2.3 BOUNDS (optional)

In the BOUNDS section changes to the default bounds vectors  $l^x$  and  $u^x$  are specified. The default bounds vectors are  $l^x = 0$  and  $u^x = \infty$ . Moreover, it is possible to specify several sets of bound vectors. A record in this section has the form

??	[name]	[vname1]	[value1]
----	--------	----------	----------

where the requirements for each field are:

Field	Starting Position	Max Width	Required	Description
??	2	2	Yes	Bound key
[name]	5	8	Yes	Name of the BOUNDS vector
[vname1]	15	8	Yes	Variable name
[value1]	25	12	No	Numerical value

Hence, a record in the BOUNDS section has the following interpretation: [name] is the name of the bound vector and [vname1] is the name of the variable which bounds are modified by the record. ?? and [value1] are used to modify the bound vectors according to the following table:

??	$l_j^x$	$u_j^x$	Made integer (added to $\mathcal{J}$ )
FR	$-\infty$	$\infty$	No
FX	$v_1$	$v_1$	No
LO	$v_1$	unchanged	No
MI	$-\infty$	unchanged	No
PL	unchanged	$\infty$	No
UP	unchanged	$v_1$	No
BV	0	1	Yes
LI	$\lceil v_1 \rceil$	unchanged	Yes
UI	unchanged	$\lfloor v_1 \rfloor$	Yes

$v_1$  is the value specified by [value1].

### 12.2.4 CSECTION (optional)

The purpose of the CSECTION is to specify the constraint

$$x \in \mathcal{K}.$$

in (12.2). It is assumed that  $\mathcal{K}$  satisfies the following requirements. Let

$$x^t \in \mathbb{R}^{n^t}, \quad t = 1, \dots, k$$

be vectors comprised of parts of the decision variables  $x$  so that each decision variable is a member of exactly **one** vector  $x^t$ , for example

$$x^1 = \begin{bmatrix} x_1 \\ x_4 \\ x_7 \end{bmatrix} \quad \text{and} \quad x^2 = \begin{bmatrix} x_6 \\ x_5 \\ x_3 \\ x_2 \end{bmatrix}.$$

Next define

$$\mathcal{K} := \{x \in \mathbb{R}^n : \quad x^t \in \mathcal{K}_t, \quad t = 1, \dots, k\}$$

where  $\mathcal{K}_t$  must have one of the following forms

- $\mathbb{R}$  set:

$$\mathcal{K}_t = \{x \in \mathbb{R}^{n^t}\}.$$

- Quadratic cone:

$$\mathcal{K}_t = \left\{ x \in \mathbb{R}^{n^t} : x_1 \geq \sqrt{\sum_{j=2}^{n^t} x_j^2} \right\}. \quad (12.3)$$

- Rotated quadratic cone:

$$\mathcal{K}_t = \left\{ x \in \mathbb{R}^{n^t} : 2x_1x_2 \geq \sum_{j=3}^{n^t} x_j^2, \quad x_1, x_2 \geq 0 \right\}. \quad (12.4)$$

In general, only quadratic and rotated quadratic cones are specified in the MPS file whereas membership of the  $\mathbb{R}$  set is not. If a variable is not a member of any other cone then it is assumed to be a member of an  $\mathbb{R}$  cone.

Next, let us study an example. Assume that the quadratic cone

$$x_4 \geq \sqrt{x_5^2 + x_8^2}$$

and the rotated quadratic cone

$$x_3x_7 \geq x_1^2 + x_0^2, \quad x_3, x_7 \geq 0,$$

should be specified in the MPS file. One CSECTION is required for each cone and they are specified as follows:

```

*          1          2          3          4          5          6
*23456789012345678901234567890123456789012345678901234567890
CSECTION      konea      0.0      QUAD
x4
x5
x8
CSECTION      koneb      0.0      RQUAD
x7
x3
x1
x0

```

This first CSECTION specifies the cone (12.3) which is given the name `konea`. This is a quadratic cone which is specified by the keyword `QUAD` in the CSECTION header. The 0.0 value in the CSECTION header is not used by the `QUAD` cone.

The second CSECTION specifies the rotated quadratic cone (12.4). Please note the keyword `RQUAD` in the CSECTION which is used to specify that the cone is a rotated quadratic cone instead of a quadratic cone. The 0.0 value in the CSECTION header is not used by the `RQUAD` cone.

In general, a CSECTION header has the format

```
CSECTION      [kname1]      [value1]      [ktype]
```

where the requirement for each field are as follows:

Field	Starting Position	Max Width	Required	Description
[kname1]	5	8	Yes	Name of the cone
[value1]	15	12	No	Cone parameter
[ktype]	25		Yes	Type of the cone.

The possible cone type keys are:

Cone type key	Members	Interpretation.
QUAD	$\leq 1$	Quadratic cone i.e. (12.3).
RQUAD	$\leq 2$	Rotated quadratic cone i.e. (12.4).

Please note that a quadratic cone must have at least one member whereas a rotated quadratic cone must have at least two members. A record in the CSECTION has the format

```
[vname1]
```

where the requirements for each field are

Field	Starting Position	Max Width	required	Description
[vname1]	2	8	Yes	A valid variable name

The most important restriction with respect to the CSECTION is that a variable must occur in only one CSECTION.

### 12.2.5 ENDATA

This keyword denotes the end of the MPS file.

### 12.2.6 Integer Variables

Using special bound keys in the BOUNDS section it is possible to specify that some or all of the variables should be integer-constrained i.e. be members of  $\mathcal{J}$ . However, an alternative method is available.

This method is available only for backward compatibility and we recommend that it is not used. This method requires that markers are placed in the COLUMNS section as in the example:

```
COLUMNS
x1      obj      -10.0      c1      0.7
x1      c2        0.5      c3      1.0
x1      c4        0.1
* Start of integer-constrained variables.
MARK000 'MARKER'          'INTORG'
x2      obj      -9.0      c1      1.0
x2      c2      0.8333333333 c3      0.66666667
x2      c4        0.25
x3      obj      1.0      c6      2.0
MARK001 'MARKER'          'INTEND'
```

- End of integer-constrained variables.

Please note that special marker lines are used to indicate the start and the end of the integer variables. Furthermore be aware of the following

- **IMPORTANT:** All variables between the markers are assigned a default lower bound of 0 and a default upper bound of 1. **This may not be what is intended.** If it is not intended, the correct bounds should be defined in the `BOUNDS` section of the MPS formatted file.
- **MOSEK** ignores field 1, i.e. `MARK0001` and `MARK001`, however, other optimization systems require them.
- Field 2, i.e. `MARKER`, must be specified including the single quotes. This implies that no row can be assigned the name `MARKER`.
- Field 3 is ignored and should be left blank.
- Field 4, i.e. `INTORG` and `INTEND`, must be specified.
- It is possible to specify several such integer marker sections within the `COLUMNS` section.

### 12.2.7 General Limitations

- An MPS file should be an ASCII file.

### 12.2.8 Interpretation of the MPS Format

Several issues related to the MPS format are not well-defined by the industry standard. However, **MOSEK** uses the following interpretation:

- If a matrix element in the `COLUMNS` section is specified multiple times, then the multiple entries are added together.
- If a matrix element in a `QSECTION` section is specified multiple times, then the multiple entries are added together.

### 12.2.9 The Free MPS Format

**MOSEK** supports a free format variation of the MPS format. The free format is similar to the MPS file format but less restrictive, e.g. it allows longer names. However, it also presents two main limitations:

- A name must not contain any blanks.
- By default a line in the MPS file must not contain more than 1024 characters. However, by modifying the parameter `MSK_IPAR_READ_MPS_WIDTH` an arbitrary large line width will be accepted.

To use the free MPS format instead of the default MPS format the **MOSEK** parameter `MSK_IPAR_READ_MPS_FORMAT` should be changed.

## 12.3 The OPF Format

The *Optimization Problem Format (OPF)* is an alternative to LP and MPS files for specifying optimization problems. It is row-oriented, inspired by the CPLEX LP format.

Apart from containing objective, constraints, bounds etc. it may contain complete or partial solutions, comments and extra information relevant for solving the problem. It is designed to be easily read and modified by hand and to be forward compatible with possible future extensions.

### Intended use

The OPF file format is meant to replace several other files:

- The LP file format: Any problem that can be written as an LP file can be written as an OPF file too; furthermore it naturally accommodates ranged constraints and variables as well as arbitrary characters in names, fixed expressions in the objective, empty constraints, and conic constraints.
- Parameter files: It is possible to specify integer, double and string parameters along with the problem (or in a separate OPF file).
- Solution files: It is possible to store a full or a partial solution in an OPF file and later reload it.

### 12.3.1 The File Format

The format uses tags to structure data. A simple example with the basic sections may look like this:

```
[comment]
This is a comment. You may write almost anything here...
[/comment]

# This is a single-line comment.

[objective min 'myobj']
x + 3 y + x^2 + 3 y^2 + z + 1
[/objective]

[constraints]
[con 'con01'] 4 <= x + y  [/con]
[/constraints]

[bounds]
[b] -10 <= x,y <= 10  [/b]

[cone quad] x,y,z [/cone]
[/bounds]
```

A scope is opened by a tag of the form `[tag]` and closed by a tag of the form `[/tag]`. An opening tag may accept a list of unnamed and named arguments, for examples:

```
[tag value] tag with one unnamed argument [/tag]
[tag arg=value] tag with one named argument in quotes [/tag]
```

Unnamed arguments are identified by their order, while named arguments may appear in any order, but never before an unnamed argument. The `value` can be a quoted, single-quoted or double-quoted text string, i.e.

```
[tag 'value']      single-quoted value [/tag]
[tag arg='value']  single-quoted value [/tag]
[tag "value"]     double-quoted value [/tag]
[tag arg="value"]  double-quoted value [/tag]
```

## Sections

The recognized tags are

[comment]

A comment section. This can contain *almost* any text: Between single quotes (') or double quotes (") any text may appear. Outside quotes the markup characters ([ and ]) must be prefixed by backslashes. Both single and double quotes may appear alone or inside a pair of quotes if it is prefixed by a backslash.

[objective]

The objective function: This accepts one or two parameters, where the first one (in the above example `min`) is either `min` or `max` (regardless of case) and defines the objective sense, and the second one (above `myobj`), if present, is the objective name. The section may contain linear and quadratic expressions. If several objectives are specified, all but the last are ignored.

[constraints]

This does not directly contain any data, but may contain the subsection `con` defining a linear constraint.

[`con`] defines a single constraint; if an argument is present ([`con NAME`]) this is used as the name of the constraint, otherwise it is given a null-name. The section contains a constraint definition written as linear and quadratic expressions with a lower bound, an upper bound, with both or with an equality. Examples:

```
[constraints]
[con 'con1'] 0 <= x + y      [/con]
[con 'con2'] 0 >= x + y      [/con]
[con 'con3'] 0 <= x + y <= 10 [/con]
[con 'con4']      x + y = 10 [/con]
[/constraints]
```

Constraint names are unique. If a constraint is specified which has the same name as a previously defined constraint, the new constraint replaces the existing one.

[bounds]

This does not directly contain any data, but may contain the subsections `b` (linear bounds on variables) and `cone` (quadratic cone).

[`b`]. Bound definition on one or several variables separated by comma (,). An upper or lower bound on a variable replaces any earlier defined bound on that variable. If only one bound (upper or lower) is given only this bound is replaced. This means that upper and lower bounds can be specified separately. So the OPF bound definition:

```
[b] x,y >= -10 [/b]
[b] x,y <= 10  [/b]
```

results in the bound  $-10 \leq x, y \leq 10$ .

[`cone`]. currently supports the *quadratic cone* and the *rotated quadratic cone*.

A conic constraint is defined as a set of variables which belong to a single unique cone.

- A quadratic cone of  $n$  variables  $x_1, \dots, x_n$  defines a constraint of the form

$$x_1^2 > \sum_{i=2}^n x_i^2.$$

- A rotated quadratic cone of  $n$  variables  $x_1, \dots, x_n$  defines a constraint of the form

$$x_1 x_2 > \sum_{i=3}^n x_i^2.$$

A `[bounds]`-section example:

```
[bounds]
[b]  0 <= x,y <= 10  [/b] # ranged bound
[b] 10 >= x,y >=  0  [/b] # ranged bound
[b]  0 <= x,y <= inf [/b] # using inf
[b]      x,y free    [/b] # free variables
# Let (x,y,z,w) belong to the cone K
[cone quad] x,y,z,w  [/cone] # quadratic cone
[cone rquad] x,y,z,w [/cone] # rotated quadratic cone
[/bounds]
```

By default all variables are free.

`[variables]`

This defines an ordering of variables as they should appear in the problem. This is simply a space-separated list of variable names.

`[integer]`

This contains a space-separated list of variables and defines the constraint that the listed variables must be integer values.

`[hints]`

This may contain only non-essential data; for example estimates of the number of variables, constraints and non-zeros. Placed before all other sections containing data this may reduce the time spent reading the file.

In the `hints` section, any subsection which is not recognized by **MOSEK** is simply ignored. In this section a hint in a subsection is defined as follows:

```
[hint ITEM] value [/hint]
```

where `ITEM` may be replaced by `numvar` (number of variables), `numcon` (number of linear/quadratic constraints), `numanz` (number of linear non-zeros in constraints) and `numqnz` (number of quadratic non-zeros in constraints).

`[solutions]`

This section can contain a set of full or partial solutions to a problem. Each solution must be specified using a `[solution]`-section, i.e.

```
[solutions]
[solution]...[/solution] #solution 1
[solution]...[/solution] #solution 2
#other solutions....
[solution]...[/solution] #solution n
[/solutions]
```

Note that a `[solution]`-section must be always specified inside a `[solutions]`-section. The syntax of a `[solution]`-section is the following:

```
[solution SOLTYPE status=STATUS]...[/solution]
```

where `SOLTYPE` is one of the strings

- `interior`, a non-basic solution,
- `basic`, a basic solution,
- `integer`, an integer solution,

and `STATUS` is one of the strings

- `UNKNOWN`,
- `OPTIMAL`,
- `INTEGER_OPTIMAL`,
- `PRIM_FEAS`,
- `DUAL_FEAS`,
- `PRIM_AND_DUAL_FEAS`,
- `NEAR_OPTIMAL`,
- `NEAR_PRIM_FEAS`,
- `NEAR_DUAL_FEAS`,
- `NEAR_PRIM_AND_DUAL_FEAS`,
- `PRIM_INFEAS_CER`,
- `DUAL_INFEAS_CER`,
- `NEAR_PRIM_INFEAS_CER`,
- `NEAR_DUAL_INFEAS_CER`,
- `NEAR_INTEGER_OPTIMAL`.

Most of these values are irrelevant for input solutions; when constructing a solution for simplex hot-start or an initial solution for a mixed integer problem the safe setting is `UNKNOWN`.

A `[solution]`-section contains `[con]` and `[var]` sections. Each `[con]` and `[var]` section defines solution information for a single variable or constraint, specified as list of `KEYWORD/value` pairs, in any order, written as

```
KEYWORD=value
```

Allowed keywords are as follows:

- `sk`. The status of the item, where the `value` is one of the following strings:
  - `LOW`, the item is on its lower bound.
  - `UPR`, the item is on its upper bound.
  - `FIX`, it is a fixed item.
  - `BAS`, the item is in the basis.



- SUPBAS, the item is super basic.
- UNK, the status is unknown.
- INF, the item is outside its bounds (infeasible).
- **lv1** Defines the level of the item.
- **s1** Defines the level of the dual variable associated with its lower bound.
- **su** Defines the level of the dual variable associated with its upper bound.
- **sn** Defines the level of the variable associated with its cone.
- **y** Defines the level of the corresponding dual variable (for constraints only).

A **[var]** section should always contain the items **sk**, **lv1**, **s1** and **su**. Items **s1** and **su** are not required for **integer** solutions.

A **[con]** section should always contain **sk**, **lv1**, **s1**, **su** and **y**.

An example of a solution section

```
[solution basic status=UNKNOWN]
[var x0] sk=LOW    lv1=5.0      [/var]
[var x1] sk=UPR    lv1=10.0     [/var]
[var x2] sk=SUPBAS lv1=2.0    s1=1.5 su=0.0 [/var]

[con c0] sk=LOW    lv1=3.0 y=0.0 [/con]
[con c0] sk=UPR    lv1=0.0 y=5.0 [/con]
[/solution]
```

- **[vendor]** This contains solver/vendor specific data. It accepts one argument, which is a vendor ID – for **MOSEK** the ID is simply **mosek** – and the section contains the subsection **parameters** defining solver parameters. When reading a vendor section, any unknown vendor can be safely ignored. This is described later.

Comments using the **#** may appear anywhere in the file. Between the **#** and the following line-break any text may be written, including markup characters.

## Numbers

Numbers, when used for parameter values or coefficients, are written in the usual way by the **printf** function. That is, they may be prefixed by a sign (+ or -) and may contain an integer part, decimal part and an exponent. The decimal point is always **.** (a dot). Some examples are

```
1
1.0
.0
1.
1e10
1e+10
1e-10
```

Some *invalid* examples are

```
e10    # invalid, must contain either integer or decimal part
.       # invalid
.e10   # invalid
```

More formally, the following standard regular expression describes numbers as used:

```
[+|-]?([0-9]+[.][0-9]*|.[0-9]+)([eE][+|-]?[0-9]+)?
```

## Names

Variable names, constraint names and objective name may contain arbitrary characters, which in some cases must be enclosed by quotes (single or double) that in turn must be preceded by a backslash. Unquoted names must begin with a letter (a-z or A-Z) and contain only the following characters: the letters a-z and A-Z, the digits 0-9, braces { and } and underscore (\_).

Some examples of legal names:

```
an_unquoted_name
another_name{123}
'single quoted name'
"double quoted name"
"name with \"quote\" in it"
"name with []s in it"
```

### 12.3.2 Parameters Section

In the `vendor` section solver parameters are defined inside the `parameters` subsection. Each parameter is written as

```
[p PARAMETER_NAME] value [/p]
```

where `PARAMETER_NAME` is replaced by a **MOSEK** parameter name, usually of the form `MSK_IPAR_...`, `MSK_DPAR_...` or `MSK_SPAR_...`, and the `value` is replaced by the value of that parameter; both integer values and named values may be used. Some simple examples are

```
[vendor mosek]
[parameters]
[p MSK_IPAR_OPF_MAX_TERMS_PER_LINE] 10      [/p]
[p MSK_IPAR_OPF_WRITE_PARAMETERS]    MSK_ON [/p]
[p MSK_DPAR_DATA_TOL_BOUND_INF]      1.0e18 [/p]
[/parameters]
[/vendor]
```

### 12.3.3 Writing OPF Files from MOSEK

To write an OPF file set the parameter `MSK_IPAR_WRITE_DATA_FORMAT` to `MSK_DATA_FORMAT_OP` as this ensures that OPF format is used.

Then modify the following parameters to define what the file should contain:

<code>MSK_IPAR_OPF_WRITE_SOL_BAS</code>	Include basic solution, if defined.
<code>MSK_IPAR_OPF_WRITE_SOL_ITG</code>	Include integer solution, if defined.
<code>MSK_IPAR_OPF_WRITE_SOL_ITR</code>	Include interior solution, if defined.
<code>MSK_IPAR_OPF_WRITE_SOLUTIONS</code>	Include solutions if they are defined. If this is off, no solutions are included.
<code>MSK_IPAR_OPF_WRITE_HEADER</code>	Include a small header with comments.
<code>MSK_IPAR_OPF_WRITE_PROBLEM</code>	Include the problem itself — objective, constraints and bounds.
<code>MSK_IPAR_OPF_WRITE_PARAMETERS</code>	Include all parameter settings.
<code>MSK_IPAR_OPF_WRITE_HINTS</code>	Include hints about the size of the problem.

### 12.3.4 Examples

This section contains a set of small examples written in OPF and describing how to formulate linear, quadratic and conic problems.

**Linear Example** lo1.opf

Consider the example:

$$\begin{array}{llllll} \text{maximize} & 3x_0 & + & 1x_1 & + & 5x_2 & + & 1x_3 \\ \text{subject to} & 3x_0 & + & 1x_1 & + & 2x_2 & & = & 30, \\ & 2x_0 & + & 1x_1 & + & 3x_2 & + & 1x_3 & \geq & 15, \\ & & & 2x_1 & & & + & 3x_3 & \leq & 25, \end{array}$$

having the bounds

$$\begin{array}{llll} 0 & \leq & x_0 & \leq \infty, \\ 0 & \leq & x_1 & \leq 10, \\ 0 & \leq & x_2 & \leq \infty, \\ 0 & \leq & x_3 & \leq \infty. \end{array}$$

In the OPF format the example is displayed as shown in [Listing 12.1](#).

Listing 12.1: Example of an OPF file for a linear problem.

```
[comment]
  The lo1 example in OPF format
[/comment]

[hints]
  [hint NUMVAR] 4 [/hint]
  [hint NUMCON] 3 [/hint]
  [hint NUMANZ] 9 [/hint]
[/hints]

[variables disallow_new_variables]
  x1 x2 x3 x4
[/variables]

[objective maximize 'obj']
  3 x1 + x2 + 5 x3 + x4
[/objective]

[constraints]
  [con 'c1'] 3 x1 + x2 + 2 x3 = 30 [/con]
  [con 'c2'] 2 x1 + x2 + 3 x3 + x4 >= 15 [/con]
  [con 'c3'] 2 x2 + 3 x4 <= 25 [/con]
[/constraints]

[bounds]
  [b] 0 <= * [/b]
  [b] 0 <= x2 <= 10 [/b]
[/bounds]
```

**Quadratic Example** qo1.opf

An example of a quadratic optimization problem is

$$\begin{array}{ll} \text{minimize} & x_1^2 + 0.1x_2^2 + x_3^2 - x_1x_3 - x_2 \\ \text{subject to} & 1 \leq x_1 + x_2 + x_3, \\ & x \geq 0. \end{array}$$

This can be formulated in opf as shown below.

Listing 12.2: Example of an OPF file for a quadratic problem.

```
[comment]
  The qo1 example in OPF format
[/comment]

[hints]
  [hint NUMVAR] 3 [/hint]
  [hint NUMCON] 1 [/hint]
  [hint NUMANZ] 3 [/hint]
  [hint NUMQNZ] 4 [/hint]
[/hints]

[variables disallow_new_variables]
  x1 x2 x3
[/variables]

[objective minimize 'obj']
  # The quadratic terms are often written with a factor of 1/2 as here,
  # but this is not required.

  - x2 + 0.5 ( 2.0 x1 ^ 2 - 2.0 x3 * x1 + 0.2 x2 ^ 2 + 2.0 x3 ^ 2 )
[/objective]

[constraints]
  [con 'c1'] 1.0 <= x1 + x2 + x3 [/con]
[/constraints]

[bounds]
  [b] 0 <= * [/b]
[/bounds]
```

**Conic Quadratic Example** cqo1.opf

Consider the example:

$$\begin{aligned}
 &\text{minimize} && x_3 + x_4 + x_5 \\
 &\text{subject to} && x_0 + x_1 + 2x_2 = 1, \\
 & && x_0, x_1, x_2 \geq 0, \\
 & && x_3 \geq \sqrt{x_0^2 + x_1^2}, \\
 & && 2x_4x_5 \geq x_2^2.
 \end{aligned}$$

Please note that the type of the cones is defined by the parameter to `[cone ...]`; the content of the cone-section is the names of variables that belong to the cone. The resulting OPF file is in [Listing 12.3](#).

Listing 12.3: Example of an OPF file for a conic quadratic problem.

```
[comment]
  The cqo1 example in OPF format.
[/comment]

[hints]
  [hint NUMVAR] 6 [/hint]
  [hint NUMCON] 1 [/hint]
  [hint NUMANZ] 3 [/hint]
[/hints]

[variables disallow_new_variables]
  x1 x2 x3 x4 x5 x6
[/variables]
```

```

[objective minimize 'obj']
  x4 + x5 + x6
[/objective]

[constraints]
  [con 'c1']  x1 + x2 + 2e+00 x3 = 1e+00 [/con]
[/constraints]

[bounds]
  # We let all variables default to the positive orthant
  [b] 0 <= * [/b]

  # ...and change those that differ from the default
  [b] x4,x5,x6 free [/b]

  # Define quadratic cone:  $x_4 \geq \sqrt{x_1^2 + x_2^2}$ 
  [cone quad 'k1'] x4, x1, x2 [/cone]

  # Define rotated quadratic cone:  $2 x_5 x_6 \geq x_3^2$ 
  [cone rquad 'k2'] x5, x6, x3 [/cone]
[/bounds]

```

### Mixed Integer Example `mil01.opf`

Consider the mixed integer problem:

$$\begin{aligned}
 &\text{maximize} && x_0 + 0.64x_1 \\
 &\text{subject to} && 50x_0 + 31x_1 \leq 250, \\
 & && 3x_0 - 2x_1 \geq -4, \\
 & && x_0, x_1 \geq 0 \quad \text{and integer}
 \end{aligned}$$

This can be implemented in OPF with the file in [Listing 12.4](#).

Listing 12.4: Example of an OPF file for a mixed-integer linear problem.

```

[comment]
  The mil01 example in OPF format
[/comment]

[hints]
  [hint NUMVAR] 2 [/hint]
  [hint NUMCON] 2 [/hint]
  [hint NUMANZ] 4 [/hint]
[/hints]

[variables disallow_new_variables]
  x1 x2
[/variables]

[objective maximize 'obj']
  x1 + 6.4e-1 x2
[/objective]

[constraints]
  [con 'c1'] 5e+1 x1 + 3.1e+1 x2 <= 2.5e+2 [/con]
  [con 'c2'] -4 <= 3 x1 - 2 x2 [/con]
[/constraints]

[bounds]
  [b] 0 <= * [/b]
[/bounds]

```

```
[integer]
  x1 x2
[/integer]
```

## 12.4 The CBF Format

This document constitutes the technical reference manual of the *Conic Benchmark Format* with file extension: `.cbf` or `.CBF`. It unifies linear, second-order cone (also known as conic quadratic) and semidefinite optimization with mixed-integer variables. The format has been designed with benchmark libraries in mind, and therefore focuses on compact and easily parsable representations. The problem structure is separated from the problem data, and the format moreover facilitates benchmarking of hotstart capability through sequences of changes.

### 12.4.1 How Instances Are Specified

This section defines the spectrum of conic optimization problems that can be formulated in terms of the keywords of the CBF format.

In the CBF format, conic optimization problems are considered in the following form:

$$\begin{aligned}
 & \min / \max && g^{obj} \\
 & \text{s.t.} && \begin{aligned} & g_i \in \mathcal{K}_i, & i \in \mathcal{I}, \\ & G_i \in \mathcal{K}_i, & i \in \mathcal{I}^{PSD}, \\ & x_j \in \mathcal{K}_j, & j \in \mathcal{J}, \\ & \bar{X}_j \in \mathcal{K}_j, & j \in \mathcal{J}^{PSD}. \end{aligned}
 \end{aligned} \tag{12.5}$$

- **Variables** are either scalar variables,  $x_j$  for  $j \in \mathcal{J}$ , or variables,  $\bar{X}_j$  for  $j \in \mathcal{J}^{PSD}$ . Scalar variables can also be declared as integer.
- **Constraints** are affine expressions of the variables, either scalar-valued  $g_i$  for  $i \in \mathcal{I}$ , or matrix-valued  $G_i$  for  $i \in \mathcal{I}^{PSD}$

$$\begin{aligned}
 g_i &= \sum_{j \in \mathcal{J}^{PSD}} \langle F_{ij}, X_j \rangle + \sum_{j \in \mathcal{J}} a_{ij} x_j + b_i, \\
 G_i &= \sum_{j \in \mathcal{J}} x_j H_{ij} + D_i.
 \end{aligned}$$

- The **objective function** is a scalar-valued affine expression of the variables, either to be minimized or maximized. We refer to this expression as  $g^{obj}$

$$g^{obj} = \sum_{j \in \mathcal{J}^{PSD}} \langle F_j^{obj}, X_j \rangle + \sum_{j \in \mathcal{J}} a_j^{obj} x_j + b^{obj}.$$

CBF format can represent the following cones  $\mathcal{K}$ :

- **Free domain** - A cone in the linear family defined by

$$\{x \in \mathbb{R}^n\}, \text{ for } n \geq 1.$$

- **Positive orthant** - A cone in the linear family defined by

$$\{x \in \mathbb{R}^n \mid x_j \geq 0 \text{ for } j = 1, \dots, n\}, \text{ for } n \geq 1.$$

- **Negative orthant** - A cone in the linear family defined by

$$\{x \in \mathbb{R}^n \mid x_j \leq 0 \text{ for } j = 1, \dots, n\}, \text{ for } n \geq 1.$$

- **Fixpoint zero** - A cone in the linear family defined by

$$\{x \in \mathbb{R}^n \mid x_j = 0 \text{ for } j = 1, \dots, n\}, \text{ for } n \geq 1.$$

- **Quadratic cone** - A cone in the second-order cone family defined by

$$\left\{ \begin{pmatrix} p \\ x \end{pmatrix} \in \mathbb{R} \times \mathbb{R}^{n-1}, p^2 \geq x^T x, p \geq 0 \right\}, \text{ for } n \geq 2.$$

- **Rotated quadratic cone** - A cone in the second-order cone family defined by

$$\left\{ \begin{pmatrix} p \\ q \\ x \end{pmatrix} \in \mathbb{R} \times \mathbb{R} \times \mathbb{R}^{n-2}, 2pq \geq x^T x, p \geq 0, q \geq 0 \right\}, \text{ for } n \geq 3.$$

### 12.4.2 The Structure of CBF Files

This section defines how information is written in the CBF format, without being specific about the type of information being communicated.

All information items belong to exactly one of the three groups of information. These information groups, and the order they must appear in, are:

1. File format.
2. Problem structure.
3. Problem data.

The first group, file format, provides information on how to interpret the file. The second group, problem structure, provides the information needed to deduce the type and size of the problem instance. Finally, the third group, problem data, specifies the coefficients and constants of the problem instance.

#### Information items

The format is composed as a list of information items. The first line of an information item is the **KEYWORD**, revealing the type of information provided. The second line - of some keywords only - is the **HEADER**, typically revealing the size of information that follows. The remaining lines are the **BODY** holding the actual information to be specified.

KEYWORD
BODY
KEYWORD
HEADER
BODY

The **KEYWORD** determines how each line in the **HEADER** and **BODY** is structured. Moreover, the number of lines in the **BODY** follows either from the **KEYWORD**, the **HEADER**, or from another information item required to precede it.

### Embedded hotstart-sequences

A sequence of problem instances, based on the same problem structure, is within a single file. This is facilitated via the **CHANGE** within the problem data information group, as a separator between the information items of each instance. The information items following a **CHANGE** keyword are appending to, or changing (e.g., setting coefficients back to their default value of zero), the problem data of the preceding instance.

The sequence is intended for benchmarking of hotstart capability, where the solvers can reuse their internal state and solution (subject to the achieved accuracy) as warmpoint for the succeeding instance. Whenever this feature is unsupported or undesired, the keyword **CHANGE** should be interpreted as the end of file.

### File encoding and line width restrictions

The format is based on the US-ASCII printable character set with two extensions as listed below. Note, by definition, that none of these extensions can be misinterpreted as printable US-ASCII characters:

- A line feed marks the end of a line, carriage returns are ignored.
- Comment-lines may contain unicode characters in UTF-8 encoding.

The line width is restricted to 512 bytes, with 3 bytes reserved for the potential carriage return, line feed and null-terminator.

Integers and floating point numbers must follow the ISO C decimal string representation in the standard C locale. The format does not impose restrictions on the magnitude of, or number of significant digits in numeric data, but the use of 64-bit integers and 64-bit IEEE 754 floating point numbers should be sufficient to avoid loss of precision.

### Comment-line and whitespace rules

The format allows single-line comments respecting the following rule:

- Lines having first byte equal to '#' (US-ASCII 35) are comments, and should be ignored. Comments are only allowed between information items.

Given that a line is not a comment-line, whitespace characters should be handled according to the following rules:

- Leading and trailing whitespace characters should be ignored.
  - The separator between multiple pieces of information on one line, is either one or more whitespace characters.
- Lines containing only whitespace characters are empty, and should be ignored. Empty lines are only allowed between information items.

## 12.4.3 Problem Specification

### The problem structure

The problem structure defines the objective sense, whether it is minimization and maximization. It also defines the index sets,  $\mathcal{J}$ ,  $\mathcal{J}^{PSD}$ ,  $\mathcal{I}$  and  $\mathcal{I}^{PSD}$ , which are all numbered from zero,  $\{0, 1, \dots\}$ , and empty until explicitly constructed.

- **Scalar variables** are constructed in vectors restricted to a conic domain, such as  $(x_0, x_1) \in \mathbb{R}_+^2$ ,  $(x_2, x_3, x_4) \in \mathcal{Q}^3$ , etc. In terms of the Cartesian product, this generalizes to

$$x \in \mathcal{K}_1^{n_1} \times \mathcal{K}_2^{n_2} \times \dots \times \mathcal{K}_k^{n_k}$$



which in the CBF format becomes:

```
VAR
n k
K1 n1
K2 n2
...
Kk nk
```

where  $\sum_i n_i = n$  is the total number of scalar variables. The list of supported cones is found in [Table 12.3](#). Integrality of scalar variables can be specified afterwards.

- **PSD variables** are constructed one-by-one. That is,  $X_j \succeq \mathbf{0}^{n_j \times n_j}$  for  $j \in \mathcal{J}^{PSD}$ , constructs a matrix-valued variable of size  $n_j \times n_j$  restricted to be symmetric positive semidefinite. In the CBF format, this list of constructions becomes:

```
PSDVAR
N
n1
n2
...
nN
```

where  $N$  is the total number of PSD variables.

- **Scalar constraints** are constructed in vectors restricted to a conic domain, such as  $(g_0, g_1) \in \mathbb{R}_+^2$ ,  $(g_2, g_3, g_4) \in \mathcal{Q}^3$ , etc. In terms of the Cartesian product, this generalizes to

$$g \in \mathcal{K}_1^{m_1} \times \mathcal{K}_2^{m_2} \times \dots \times \mathcal{K}_k^{m_k}$$

which in the CBF format becomes:

```
CON
m k
K1 m1
K2 m2
..
Kk mk
```

where  $\sum_i m_i = m$  is the total number of scalar constraints. The list of supported cones is found in [Table 12.3](#).

- **PSD constraints** are constructed one-by-one. That is,  $G_i \succeq \mathbf{0}^{m_i \times m_i}$  for  $i \in \mathcal{I}^{PSD}$ , constructs a matrix-valued affine expressions of size  $m_i \times m_i$  restricted to be symmetric positive semidefinite. In the CBF format, this list of constructions becomes

```
PSDCON
M
m1
m2
..
mM
```

where  $M$  is the total number of PSD constraints.

With the objective sense, variables (with integer indications) and constraints, the definitions of the many affine expressions follow in problem data.

## Problem data

The problem data defines the coefficients and constants of the affine expressions of the problem instance. These are considered zero until explicitly defined, implying that instances with no keywords from this

information group are, in fact, valid. Duplicating or conflicting information is a failure to comply with the standard. Consequently, two coefficients written to the same position in a matrix (or to transposed positions in a symmetric matrix) is an error.

The affine expressions of the objective,  $g^{obj}$ , of the scalar constraints,  $g_i$ , and of the PSD constraints,  $G_i$ , are defined separately. The following notation uses the standard trace inner product for matrices,  $\langle X, Y \rangle = \sum_{i,j} X_{ij}Y_{ij}$ .

- The affine expression of the objective is defined as

$$g^{obj} = \sum_{j \in \mathcal{J}^{PSD}} \langle F_j^{obj}, X_j \rangle + \sum_{j \in \mathcal{J}} a_j^{obj} x_j + b^{obj},$$

in terms of the symmetric matrices,  $F_j^{obj}$ , and scalars,  $a_j^{obj}$  and  $b^{obj}$ .

- The affine expressions of the scalar constraints are defined, for  $i \in \mathcal{I}$ , as

$$g_i = \sum_{j \in \mathcal{J}^{PSD}} \langle F_{ij}, X_j \rangle + \sum_{j \in \mathcal{J}} a_{ij} x_j + b_i,$$

in terms of the symmetric matrices,  $F_{ij}$ , and scalars,  $a_{ij}$  and  $b_i$ .

- The affine expressions of the PSD constraints are defined, for  $i \in \mathcal{I}^{PSD}$ , as

$$G_i = \sum_{j \in \mathcal{J}} x_j H_{ij} + D_i,$$

in terms of the symmetric matrices,  $H_{ij}$  and  $D_i$ .

## List of cones

The format uses an explicit syntax for symmetric positive semidefinite cones as shown above. For scalar variables and constraints, constructed in vectors, the supported conic domains and their minimum sizes are given as follows.

Table 12.3: Cones available in the CBF format

Name	CBF keyword	Cone family
Free domain	F	linear
Positive orthant	L+	linear
Negative orthant	L-	linear
Fixpoint zero	L=	linear
Quadratic cone	Q	second-order
Rotated quadratic cone	QR	second-order

## 12.4.4 File Format Keywords

### VER

*Description:* The version of the Conic Benchmark Format used to write the file.

**HEADER:** None

**BODY:** One line formatted as:

INT
-----

This is the version number.

Must appear exactly once in a file, as the first keyword.

## OBJSENSE

*Description:* Define the objective sense.

HEADER: None

BODY: One line formatted as:

STR
-----

having MIN indicates minimize, and MAX indicates maximize. Capital letters are required.

Must appear exactly once in a file.

## PSDVAR

*Description:* Construct the PSD variables.

HEADER: One line formatted as:

INT
-----

This is the number of PSD variables in the problem.

BODY: A list of lines formatted as:

INT
-----

This indicates the number of rows (equal to the number of columns) in the matrix-valued PSD variable. The number of lines should match the number stated in the header.

## VAR

*Description:* Construct the scalar variables.

HEADER: One line formatted as:

INT INT
---------

This is the number of scalar variables, followed by the number of conic domains they are restricted to.

BODY: A list of lines formatted as:

STR INT
---------

This indicates the cone name (see [Table 12.3](#)), and the number of scalar variables restricted to this cone. These numbers should add up to the number of scalar variables stated first in the header. The number of lines should match the second number stated in the header.

## INT

*Description:* Declare integer requirements on a selected subset of scalar variables.

HEADER: one line formatted as:

INT
-----

This is the number of integer scalar variables in the problem.

BODY: a list of lines formatted as:

INT
-----

This indicates the scalar variable index  $j \in \mathcal{J}$ . The number of lines should match the number stated in the header.

Can only be used after the keyword **VAR**.

## PSDCON

*Description:* Construct the PSD constraints.

**HEADER:** One line formatted as:

INT
-----

This is the number of PSD constraints in the problem.

**BODY:** A list of lines formatted as:

INT
-----

This indicates the number of rows (equal to the number of columns) in the matrix-valued affine expression of the PSD constraint. The number of lines should match the number stated in the header.

Can only be used after these keywords: **PSDVAR**, **VAR**.

## CON

*Description:* Construct the scalar constraints.

**HEADER:** One line formatted as:

INT INT
---------

This is the number of scalar constraints, followed by the number of conic domains they restrict to.

**BODY:** A list of lines formatted as:

STR INT
---------

This indicates the cone name (see [Table 12.3](#)), and the number of affine expressions restricted to this cone. These numbers should add up to the number of scalar constraints stated first in the header. The number of lines should match the second number stated in the header.

Can only be used after these keywords: **PSDVAR**, **VAR**

## OBJFCOORD

*Description:* Input sparse coordinates (quadruplets) to define the symmetric matrices  $F_j^{obj}$ , as used in the objective.

**HEADER:** One line formatted as:

INT
-----

This is the number of coordinates to be specified.

**BODY:** A list of lines formatted as:

INT INT INT REAL
------------------

This indicates the PSD variable index  $j \in \mathcal{J}^{PSD}$ , the row index, the column index and the coefficient value. The number of lines should match the number stated in the header.

## OBJACOORD

*Description:* Input sparse coordinates (pairs) to define the scalars,  $a_j^{obj}$ , as used in the objective.

HEADER: One line formatted as:

INT
-----

This is the number of coordinates to be specified.

BODY: A list of lines formatted as:

INT REAL
----------

This indicates the scalar variable index  $j \in \mathcal{J}$  and the coefficient value. The number of lines should match the number stated in the header.

## OBJBCOORD

*Description:* Input the scalar,  $b^{obj}$ , as used in the objective.

HEADER: None.

BODY: One line formatted as:

REAL
------

This indicates the coefficient value.

## FCOORD

*Description:* Input sparse coordinates (quintuplets) to define the symmetric matrices,  $F_{ij}$ , as used in the scalar constraints.

HEADER: One line formatted as:

INT
-----

This is the number of coordinates to be specified.

BODY: A list of lines formatted as:

INT INT INT INT REAL
----------------------

This indicates the scalar constraint index  $i \in \mathcal{I}$ , the PSD variable index  $j \in \mathcal{J}^{PSD}$ , the row index, the column index and the coefficient value. The number of lines should match the number stated in the header.

## ACOORD

*Description:* Input sparse coordinates (triplets) to define the scalars,  $a_{ij}$ , as used in the scalar constraints.

HEADER: One line formatted as:

INT
-----

This is the number of coordinates to be specified.

BODY: A list of lines formatted as:

INT INT REAL
--------------

This indicates the scalar constraint index  $i \in \mathcal{I}$ , the scalar variable index  $j \in \mathcal{J}$  and the coefficient value. The number of lines should match the number stated in the header.

## BCOORD

*Description:* Input sparse coordinates (pairs) to define the scalars,  $b_i$ , as used in the scalar constraints.

HEADER: One line formatted as:

INT
-----

This is the number of coordinates to be specified.

BODY: A list of lines formatted as:

INT REAL
----------

This indicates the scalar constraint index  $i \in \mathcal{I}$  and the coefficient value. The number of lines should match the number stated in the header.

## HCOORD

*Description:* Input sparse coordinates (quintuplets) to define the symmetric matrices,  $H_{ij}$ , as used in the PSD constraints.

HEADER: One line formatted as:

INT
-----

This is the number of coordinates to be specified.

BODY: A list of lines formatted as

INT INT INT INT REAL
----------------------

This indicates the PSD constraint index  $i \in \mathcal{I}^{PSD}$ , the scalar variable index  $j \in \mathcal{J}$ , the row index, the column index and the coefficient value. The number of lines should match the number stated in the header.

## DCOORD

*Description:* Input sparse coordinates (quadruplets) to define the symmetric matrices,  $D_i$ , as used in the PSD constraints.

HEADER: One line formatted as

INT
-----

This is the number of coordinates to be specified.

BODY: A list of lines formatted as:

INT INT INT REAL
------------------

This indicates the PSD constraint index  $i \in \mathcal{I}^{PSD}$ , the row index, the column index and the coefficient value. The number of lines should match the number stated in the header.

## CHANGE

Start of a new instance specification based on changes to the previous. Can be interpreted as the end of file when the hotstart-sequence is unsupported or undesired.

BODY: None

Header: None

## 12.4.5 CBF Format Examples

### Minimal Working Example

The conic optimization problem (12.6), has three variables in a quadratic cone - first one is integer - and an affine expression in domain 0 (equality constraint).

$$\begin{aligned} & \text{minimize} && 5.1 x_0 \\ & \text{subject to} && 6.2 x_1 + 7.3 x_2 - 8.4 \in \{0\} \\ & && x \in \mathcal{Q}^3, x_0 \in \mathbb{Z}. \end{aligned} \tag{12.6}$$

Its formulation in the Conic Benchmark Format begins with the version of the CBF format used, to safeguard against later revisions.

```
VER
1
```

Next follows the problem structure, consisting of the objective sense, the number and domain of variables, the indices of integer variables, and the number and domain of scalar-valued affine expressions (i.e., the equality constraint).

```
OBJSENSE
MIN

VAR
3 1
Q 3

INT
1
0

CON
1 1
L= 1
```

Finally follows the problem data, consisting of the coefficients of the objective, the coefficients of the constraints, and the constant terms of the constraints. All data is specified on a sparse coordinate form.

```
OBJACOORD
1
0 5.1

ACOORD
2
0 1 6.2
0 2 7.3

BCOORD
1
0 -8.4
```

This concludes the example.

### Mixing Linear, Second-order and Semidefinite Cones

The conic optimization problem (12.7), has a semidefinite cone, a quadratic cone over unordered subindices, and two equality constraints.

$$\begin{aligned}
 & \text{minimize} && \left\langle \begin{bmatrix} 2 & 1 & 0 \\ 1 & 2 & 1 \\ 0 & 1 & 2 \end{bmatrix}, X_1 \right\rangle + x_1 \\
 & \text{subject to} && \left\langle \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}, X_1 \right\rangle + x_1 &= 1.0, \\
 & && \left\langle \begin{bmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{bmatrix}, X_1 \right\rangle + x_0 + x_2 &= 0.5, \\
 & && x_1 \geq \sqrt{x_0^2 + x_2^2}, \\
 & && X_1 \succeq \mathbf{0}.
 \end{aligned} \tag{12.7}$$

The equality constraints are easily rewritten to the conic form,  $(g_0, g_1) \in \{0\}^2$ , by moving constants such that the right-hand-side becomes zero. The quadratic cone does not fit under the `VAR` keyword in this variable permutation. Instead, it takes a scalar constraint  $(g_2, g_3, g_4) = (x_1, x_0, x_2) \in \mathcal{Q}^3$ , with scalar variables constructed as  $(x_0, x_1, x_2) \in \mathbb{R}^3$ . Its formulation in the CBF format is reported in the following list

```

# File written using this version of the Conic Benchmark Format:
#   | Version 1.
VER
1

# The sense of the objective is:
#   | Minimize.
OBJSENSE
MIN

# One PSD variable of this size:
#   | Three times three.
PSDVAR
1
3

# Three scalar variables in this one conic domain:
#   | Three are free.
VAR
3 1
F 3

# Five scalar constraints with affine expressions in two conic domains:
#   | Two are fixed to zero.
#   | Three are in conic quadratic domain.
CON
5 2
L= 2
Q 3

# Five coordinates in F^{obj}_j coefficients:
#   | F^{obj}[0][0,0] = 2.0
#   | F^{obj}[0][1,0] = 1.0
#   | and more...
OBJFCOORD
5
0 0 0 2.0
0 1 0 1.0
0 1 1 2.0

```



```

0 2 1 1.0
0 2 2 2.0

# One coordinate in a^{obj}_j coefficients:
#   | a^{obj}[1] = 1.0
OBJCOORD
1
1 1.0

# Nine coordinates in F_ij coefficients:
#   | F[0,0][0,0] = 1.0
#   | F[0,0][1,1] = 1.0
#   | and more...
FCOORD
9
0 0 0 0 1.0
0 0 1 1 1.0
0 0 2 2 1.0
1 0 0 0 1.0
1 0 1 0 1.0
1 0 2 0 1.0
1 0 1 1 1.0
1 0 2 1 1.0
1 0 2 2 1.0

# Six coordinates in a_ij coefficients:
#   | a[0,1] = 1.0
#   | a[1,0] = 1.0
#   | and more...
ACCOORD
6
0 1 1.0
1 0 1.0
1 2 1.0
2 1 1.0
3 0 1.0
4 2 1.0

# Two coordinates in b_i coefficients:
#   | b[0] = -1.0
#   | b[1] = -0.5
BCOORD
2
0 -1.0
1 -0.5

```

### Mixing Semidefinite Variables and Linear Matrix Inequalities

The standard forms in semidefinite optimization are usually based either on semidefinite variables or linear matrix inequalities. In the CBF format, both forms are supported and can even be mixed as shown in.

$$\begin{aligned}
 & \text{minimize} && \left\langle \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}, X_1 \right\rangle + x_1 + x_2 + 1 \\
 & \text{subject to} && \left\langle \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix}, X_1 \right\rangle - x_1 - x_2 \geq 0.0, \\
 & && x_1 \begin{bmatrix} 0 & 1 \\ 1 & 3 \end{bmatrix} + x_2 \begin{bmatrix} 3 & 1 \\ 1 & 0 \end{bmatrix} - \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \succeq \mathbf{0}, \\
 & && X_1 \succeq \mathbf{0}.
 \end{aligned} \tag{12.8}$$

Its formulation in the CBF format is written in what follows

```
# File written using this version of the Conic Benchmark Format:
#       | Version 1.
VER
1

# The sense of the objective is:
#       | Minimize.
OBJSENSE
MIN

# One PSD variable of this size:
#       | Two times two.
PSDVAR
1
2

# Two scalar variables in this one conic domain:
#       | Two are free.
VAR
2 1
F 2

# One PSD constraint of this size:
#       | Two times two.
PSDCON
1
2

# One scalar constraint with an affine expression in this one conic domain:
#       | One is greater than or equal to zero.
CON
1 1
L+ 1

# Two coordinates in  $F^{\{obj\}}_j$  coefficients:
#       |  $F^{\{obj\}}[0][0,0] = 1.0$ 
#       |  $F^{\{obj\}}[0][1,1] = 1.0$ 
OBJFCOORD
2
0 0 0 1.0
0 1 1 1.0

# Two coordinates in  $a^{\{obj\}}_j$  coefficients:
#       |  $a^{\{obj\}}[0] = 1.0$ 
#       |  $a^{\{obj\}}[1] = 1.0$ 
OBJACOORD
2
0 1.0
1 1.0

# One coordinate in  $b^{\{obj\}}$  coefficient:
#       |  $b^{\{obj\}} = 1.0$ 
OBJBCOORD
1.0

# One coordinate in  $F_{ij}$  coefficients:
#       |  $F[0,0][1,0] = 1.0$ 
FCOORD
1
0 0 1 0 1.0

# Two coordinates in  $a_{ij}$  coefficients:
#       |  $a[0,0] = -1.0$ 
```

```
#      | a[0,1] = -1.0
ACCOORD
2
0 0 -1.0
0 1 -1.0

# Four coordinates in H_ij coefficients:
#      | H[0,0][1,0] = 1.0
#      | H[0,0][1,1] = 3.0
#      | and more...
HCOORD
4
0 0 1 0 1.0
0 0 1 1 3.0
0 1 0 0 3.0
0 1 1 0 1.0

# Two coordinates in D_i coefficients:
#      | D[0][0,0] = -1.0
#      | D[0][1,1] = -1.0
DCCOORD
2
0 0 0 -1.0
0 1 1 -1.0
```

### Optimization Over a Sequence of Objectives

The linear optimization problem (12.9), is defined for a sequence of objectives such that hotstarting from one to the next might be advantages.

$$\begin{aligned}
 & \text{maximize}_k && g_k^{obj} \\
 & \text{subject to} && 50x_0 + 31 \leq 250, \\
 & && 3x_0 - 2x_1 \geq -4, \\
 & && x \in \mathbb{R}_+^2,
 \end{aligned} \tag{12.9}$$

given,

1.  $g_0^{obj} = x_0 + 0.64x_1$ .
2.  $g_1^{obj} = 1.11x_0 + 0.76x_1$ .
3.  $g_2^{obj} = 1.11x_0 + 0.85x_1$ .

Its formulation in the CBF format is reported in [Listing 12.5](#).

Listing 12.5: Problem (12.9) in CBF format.

```
# File written using this version of the Conic Benchmark Format:
#      | Version 1.
VER
1

# The sense of the objective is:
#      | Maximize.
OBJSENSE
MAX

# Two scalar variables in this one conic domain:
#      | Two are nonnegative.
VAR
2 1
L+ 2
```

```
# Two scalar constraints with affine expressions in these two conic domains:
#   | One is in the nonpositive domain.
#   | One is in the nonnegative domain.
CON
2 2
L- 1
L+ 1

# Two coordinates in a^{obj}_j coefficients:
#   | a^{obj}[0] = 1.0
#   | a^{obj}[1] = 0.64
OBJACCOORD
2
0 1.0
1 0.64

# Four coordinates in a_ij coefficients:
#   | a[0,0] = 50.0
#   | a[1,0] = 3.0
#   | and more...
ACCOORD
4
0 0 50.0
1 0 3.0
0 1 31.0
1 1 -2.0

# Two coordinates in b_i coefficients:
#   | b[0] = -250.0
#   | b[1] = 4.0
BCCOORD
2
0 -250.0
1 4.0

# New problem instance defined in terms of changes.
CHANGE

# Two coordinate changes in a^{obj}_j coefficients. Now it is:
#   | a^{obj}[0] = 1.11
#   | a^{obj}[1] = 0.76
OBJACCOORD
2
0 1.11
1 0.76

# New problem instance defined in terms of changes.
CHANGE

# One coordinate change in a^{obj}_j coefficients. Now it is:
#   | a^{obj}[0] = 1.11
#   | a^{obj}[1] = 0.85
OBJACCOORD
1
1 0.85
```

## 12.5 The XML (OSiL) Format

**MOSEK** can write data in the standard OSiL xml format. For a definition of the OSiL format please see <http://www.optimizationservices.org/>.

Only linear constraints (possibly with integer variables) are supported. By default output files with the extension `.xml` are written in the OSiL format.

The parameter `MSK_IPAR_WRITE_XML_MODE` controls if the linear coefficients in the  $A$  matrix are written in row or column order.

## 12.6 The Task Format

The Task format is **MOSEK**'s native binary format. It contains a complete image of a **MOSEK** task, i.e.

- Problem data: Linear, conic quadratic, semidefinite and quadratic data
- Problem item names: Variable names, constraints names, cone names etc.
- Parameter settings
- Solutions

There are a few things to be aware of:

- The task format *does not* support General Convex problems since these are defined by arbitrary user-defined functions.
- Status of a solution read from a file will *always* be unknown.

The format is based on the *TAR* (USTar) file format. This means that the individual pieces of data in a `.task` file can be examined by unpacking it as a *TAR* file. Please note that the inverse may not work: Creating a file using *TAR* will most probably not create a valid **MOSEK** Task file since the order of the entries is important.

## 12.7 The JSON Format

**MOSEK** provides the possibility to read/write problems in valid JSON format.

JSON (JavaScript Object Notation) is a lightweight data-interchange format. It is easy for humans to read and write. It is easy for machines to parse and generate. It is based on a subset of the JavaScript Programming Language, Standard ECMA-262 3rd Edition - December 1999. JSON is a text format that is completely language independent but uses conventions that are familiar to programmers of the C-family of languages, including C, C++, C#, Java, JavaScript, Perl, Python, and many others. These properties make JSON an ideal data-interchange language.

The official JSON website <http://www.json.org> provides plenty of information along with the format definition.

**MOSEK** defines two JSON-like formats:

- *jtask*
- *jsol*

**Warning:** Despite being text-based human-readable formats, *jtask* and *jsol* files will include no indentation and no new-lines, in order to keep the files as compact as possible. We therefore strongly advise to use JSON viewer tools to inspect *jtask* and *jsol* files.

### 12.7.1 *jtask* format

It stores a problem instance. The *jtask* format contains the same information as a *task format*.

Even though a *jtask* file is human-readable, we do not recommend users to create it by hand, but to rely on MOSEK.

### 12.7.2 *jsol* format

It stores a problem solution. The *jsol* format contains all solutions and information items.

### 12.7.3 A *jtask* example

In Listing 12.6 we present a file in the *jtask* format that corresponds to the sample problem from `lo1.lp`. The listing has been formatted for readability.

Listing 12.6: A formatted *jtask* file for the `lo1.lp` example.

```
{
  "$schema": "http://mosek.com/json/schema#",
  "Task/INFO": {
    "taskname": "lo1",
    "numvar": 4,
    "numcon": 3,
    "numcone": 0,
    "numbarvar": 0,
    "numanz": 9,
    "numsymmat": 0,
    "mosekver": [
      8,
      0,
      0,
      9
    ]
  },
  "Task/data": {
    "var": {
      "name": [
        "x1",
        "x2",
        "x3",
        "x4"
      ],
      "bk": [
        "lo",
        "ra",
        "lo",
        "lo"
      ],
      "b1": [
        0.0,
        0.0,
        0.0,
        0.0
      ],
      "bu": [
        1e+30,
        1e+1,
        1e+30,
        1e+30
      ]
    },
  },
}
```

```

        "type": [
            "cont",
            "cont",
            "cont",
            "cont"
        ]
    },
    "con": {
        "name": [
            "c1",
            "c2",
            "c3"
        ],
        "bk": [
            "fx",
            "lo",
            "up"
        ],
        "bl": [
            3e+1,
            1.5e+1,
            -1e+30
        ],
        "bu": [
            3e+1,
            1e+30,
            2.5e+1
        ]
    },
    "objective": {
        "sense": "max",
        "name": "obj",
        "c": {
            "subj": [
                0,
                1,
                2,
                3
            ],
            "val": [
                3e+0,
                1e+0,
                5e+0,
                1e+0
            ]
        }
    },
    "cfix": 0.0
},
"A": {
    "subi": [
        0,
        0,
        0,
        1,
        1,
        1,
        1,
        1,
        2,
        2
    ],
    "subj": [
        0,
        1,

```

```

        2,
        0,
        1,
        2,
        3,
        1,
        3
    ],
    "val": [
        3e+0,
        1e+0,
        2e+0,
        2e+0,
        1e+0,
        3e+0,
        1e+0,
        2e+0,
        3e+0
    ]
}
},
"Task/parameters": {
    "iparam": {
        "ANA_SOL_BASIS": "ON",
        "ANA_SOL_PRINT_VIOLATED": "OFF",
        "AUTO_SORT_A_BEFORE_OPT": "OFF",
        "AUTO_UPDATE_SOL_INFO": "OFF",
        "BASIS_SOLVE_USE_PLUS_ONE": "OFF",
        "BI_CLEAN_OPTIMIZER": "OPTIMIZER_FREE",
        "BI_IGNORE_MAX_ITER": "OFF",
        "BI_IGNORE_NUM_ERROR": "OFF",
        "BI_MAX_ITERATIONS": 1000000,
        "CACHE_LICENSE": "ON",
        "CHECK_CONVEXITY": "CHECK_CONVEXITY_FULL",
        "COMPRESS_STATFILE": "ON",
        "CONCURRENT_NUM_OPTIMIZERS": 2,
        "CONCURRENT_PRIORITY_DUAL_SIMPLEX": 2,
        "CONCURRENT_PRIORITY_FREE_SIMPLEX": 3,
        "CONCURRENT_PRIORITY_INTPNT": 4,
        "CONCURRENT_PRIORITY_PRIMAL_SIMPLEX": 1,
        "FEASREPAIR_OPTIMIZE": "FEASREPAIR_OPTIMIZE_NONE",
        "INFEAS_GENERIC_NAMES": "OFF",
        "INFEAS_PREFER_PRIMAL": "ON",
        "INFEAS_REPORT_AUTO": "OFF",
        "INFEAS_REPORT_LEVEL": 1,
        "INTPNT_BASIS": "BI_ALWAYS",
        "INTPNT_DIFF_STEP": "ON",
        "INTPNT_FACTOR_DEBUG_LVL": 0,
        "INTPNT_FACTOR_METHOD": 0,
        "INTPNT_HOTSTART": "INTPNT_HOTSTART_NONE",
        "INTPNT_MAX_ITERATIONS": 400,
        "INTPNT_MAX_NUM_COR": -1,
        "INTPNT_MAX_NUM_REFINEMENT_STEPS": -1,
        "INTPNT_OFF_COL_TRH": 40,
        "INTPNT_ORDER_METHOD": "ORDER_METHOD_FREE",
        "INTPNT_REGULARIZATION_USE": "ON",
        "INTPNT_SCALING": "SCALING_FREE",
        "INTPNT_SOLVE_FORM": "SOLVE_FREE",
        "INTPNT_STARTING_POINT": "STARTING_POINT_FREE",
        "LIC_TRH_EXPIRY_WRN": 7,
        "LICENSE_DEBUG": "OFF",
        "LICENSE_PAUSE_TIME": 0,
        "LICENSE_SUPPRESS_EXPIRE_WRNS": "OFF",
    }
}

```



```

"LICENSE_WAIT": "OFF",
"LOG": 10,
"LOG_ANA_PRO": 1,
"LOG_BI": 4,
"LOG_BI_FREQ": 2500,
"LOG_CHECK_CONVEXITY": 0,
"LOG_CONCURRENT": 1,
"LOG_CUT_SECOND_OPT": 1,
"LOG_EXPAND": 0,
"LOG_FACTOR": 1,
"LOG_FEAS_REPAIR": 1,
"LOG_FILE": 1,
"LOG_HEAD": 1,
"LOG_INFEAS_ANA": 1,
"LOG_INTPNT": 4,
"LOG_MIO": 4,
"LOG_MIO_FREQ": 1000,
"LOG_OPTIMIZER": 1,
"LOG_ORDER": 1,
"LOG_PRESOLVE": 1,
"LOG_RESPONSE": 0,
"LOG_SENSITIVITY": 1,
"LOG_SENSITIVITY_OPT": 0,
"LOG_SIM": 4,
"LOG_SIM_FREQ": 1000,
"LOG_SIM_MINOR": 1,
"LOG_STORAGE": 1,
"MAX_NUM_WARNINGS": 10,
"MIO_BRANCH_DIR": "BRANCH_DIR_FREE",
"MIO_CONSTRUCT_SOL": "OFF",
"MIO_CUT_CLIQUE": "ON",
"MIO_CUT_CMIR": "ON",
"MIO_CUT_GMI": "ON",
"MIO_CUT_KNAPSACK_COVER": "OFF",
"MIO_HEURISTIC_LEVEL": -1,
"MIO_MAX_NUM_BRANCHES": -1,
"MIO_MAX_NUM_RELAXS": -1,
"MIO_MAX_NUM_SOLUTIONS": -1,
"MIO_MODE": "MIO_MODE_SATISFIED",
"MIO_MT_USER_CB": "ON",
"MIO_NODE_OPTIMIZER": "OPTIMIZER_FREE",
"MIO_NODE_SELECTION": "MIO_NODE_SELECTION_FREE",
"MIO_PERSPECTIVE_REFORMULATE": "ON",
"MIO_PROBING_LEVEL": -1,
"MIO_RINS_MAX_NODES": -1,
"MIO_ROOT_OPTIMIZER": "OPTIMIZER_FREE",
"MIO_ROOT_REPEAT_PRESOLVE_LEVEL": -1,
"MT_SPINCOUNT": 0,
"NUM_THREADS": 0,
"OPF_MAX_TERMS_PER_LINE": 5,
"OPF_WRITE_HEADER": "ON",
"OPF_WRITE_HINTS": "ON",
"OPF_WRITE_PARAMETERS": "OFF",
"OPF_WRITE_PROBLEM": "ON",
"OPF_WRITE_SOL_BAS": "ON",
"OPF_WRITE_SOL_ITG": "ON",
"OPF_WRITE_SOL_ITR": "ON",
"OPF_WRITE_SOLUTIONS": "OFF",
"OPTIMIZER": "OPTIMIZER_FREE",
"PARAM_READ_CASE_NAME": "ON",
"PARAM_READ_IGN_ERROR": "OFF",
"PRESOLVE_ELIMINATOR_MAX_FILL": -1,
"PRESOLVE_ELIMINATOR_MAX_NUM_TRIES": -1,

```

```

"PRESOLVE_LEVEL":-1,
"PRESOLVE_LINDEP_ABS_WORK_TRH":100,
"PRESOLVE_LINDEP_REL_WORK_TRH":100,
"PRESOLVE_LINDEP_USE":"ON",
"PRESOLVE_MAX_NUM_REDUCTIONS":-1,
"PRESOLVE_USE":"PRESOLVE_MODE_FREE",
"PRIMAL_REPAIR_OPTIMIZER":"OPTIMIZER_FREE",
"QO_SEPARABLE_REFORMULATION":"OFF",
"READ_DATA_COMPRESSED":"COMPRESS_FREE",
"READ_DATA_FORMAT":"DATA_FORMAT_EXTENSION",
"READ_DEBUG":"OFF",
"READ_KEEP_FREE_CON":"OFF",
"READ_LP_DROP_NEW_VARS_IN_BOU":"OFF",
"READ_LP_QUOTED_NAMES":"ON",
"READ_MPS_FORMAT":"MPS_FORMAT_FREE",
"READ_MPS_WIDTH":1024,
"READ_TASK_IGNORE_PARAM":"OFF",
"SENSITIVITY_ALL":"OFF",
"SENSITIVITY_OPTIMIZER":"OPTIMIZER_FREE_SIMPLEX",
"SENSITIVITY_TYPE":"SENSITIVITY_TYPE_BASIS",
"SIM_BASIS_FACTOR_USE":"ON",
"SIM_DEGEN":"SIM_DEGEN_FREE",
"SIM_DUAL_CRASH":90,
"SIM_DUAL_PHASEONE_METHOD":0,
"SIM_DUAL_RESTRICT_SELECTION":50,
"SIM_DUAL_SELECTION":"SIM_SELECTION_FREE",
"SIM_EXPLOIT_DUPVEC":"SIM_EXPLOIT_DUPVEC_OFF",
"SIM_HOTSTART":"SIM_HOTSTART_FREE",
"SIM_HOTSTART_LU":"ON",
"SIM_INTEGER":0,
"SIM_MAX_ITERATIONS":10000000,
"SIM_MAX_NUM_SETBACKS":250,
"SIM_NON_SINGULAR":"ON",
"SIM_PRIMAL_CRASH":90,
"SIM_PRIMAL_PHASEONE_METHOD":0,
"SIM_PRIMAL_RESTRICT_SELECTION":50,
"SIM_PRIMAL_SELECTION":"SIM_SELECTION_FREE",
"SIM_REFACTOR_FREQ":0,
"SIM_REFORMULATION":"SIM_REFORMULATION_OFF",
"SIM_SAVE_LU":"OFF",
"SIM_SCALING":"SCALING_FREE",
"SIM_SCALING_METHOD":"SCALING_METHOD_POW2",
"SIM_SOLVE_FORM":"SOLVE_FREE",
"SIM_STABILITY_PRIORITY":50,
"SIM_SWITCH_OPTIMIZER":"OFF",
"SOL_FILTER_KEEP_BASIC":"OFF",
"SOL_FILTER_KEEP_RANGED":"OFF",
"SOL_READ_NAME_WIDTH":-1,
"SOL_READ_WIDTH":1024,
"SOLUTION_CALLBACK":"OFF",
"TIMING_LEVEL":1,
"WRITE_BAS_CONSTRAINTS":"ON",
"WRITE_BAS_HEAD":"ON",
"WRITE_BAS_VARIABLES":"ON",
"WRITE_DATA_COMPRESSED":0,
"WRITE_DATA_FORMAT":"DATA_FORMAT_EXTENSION",
"WRITE_DATA_PARAM":"OFF",
"WRITE_FREE_CON":"OFF",
"WRITE_GENERIC_NAMES":"OFF",
"WRITE_GENERIC_NAMES_IO":1,
"WRITE_IGNORE_INCOMPATIBLE_CONIC_ITEMS":"OFF",
"WRITE_IGNORE_INCOMPATIBLE_ITEMS":"OFF",
"WRITE_IGNORE_INCOMPATIBLE_NL_ITEMS":"OFF",

```

```

    "WRITE_IGNORE_INCOMPATIBLE_PSD_ITEMS": "OFF",
    "WRITE_INT_CONSTRAINTS": "ON",
    "WRITE_INT_HEAD": "ON",
    "WRITE_INT_VARIABLES": "ON",
    "WRITE_LP_FULL_OBJ": "ON",
    "WRITE_LP_LINE_WIDTH": 80,
    "WRITE_LP_QUOTED_NAMES": "ON",
    "WRITE_LP_STRICT_FORMAT": "OFF",
    "WRITE_LP_TERMS_PER_LINE": 10,
    "WRITE_MPS_FORMAT": "MPS_FORMAT_FREE",
    "WRITE_MPS_INT": "ON",
    "WRITE_PRECISION": 15,
    "WRITE_SOL_BARVARIABLES": "ON",
    "WRITE_SOL_CONSTRAINTS": "ON",
    "WRITE_SOL_HEAD": "ON",
    "WRITE_SOL_IGNORE_INVALID_NAMES": "OFF",
    "WRITE_SOL_VARIABLES": "ON",
    "WRITE_TASK_INC_SOL": "ON",
    "WRITE_XML_MODE": "WRITE_XML_MODE_ROW"
  },
  "dparam": {
    "ANA_SOL_INFEAS_TOL": 1e-6,
    "BASIS_REL_TOL_S": 1e-12,
    "BASIS_TOL_S": 1e-6,
    "BASIS_TOL_X": 1e-6,
    "CHECK_CONVEXITY_REL_TOL": 1e-10,
    "DATA_TOL_AIJ": 1e-12,
    "DATA_TOL_AIJ_HUGE": 1e+20,
    "DATA_TOL_AIJ_LARGE": 1e+10,
    "DATA_TOL_BOUND_INF": 1e+16,
    "DATA_TOL_BOUND_WRN": 1e+8,
    "DATA_TOL_C_HUGE": 1e+16,
    "DATA_TOL_CJ_LARGE": 1e+8,
    "DATA_TOL_QIJ": 1e-16,
    "DATA_TOL_X": 1e-8,
    "FEASREPAIR_TOL": 1e-10,
    "INTPNT_CO_TOL_DFEAS": 1e-8,
    "INTPNT_CO_TOL_INFEAS": 1e-10,
    "INTPNT_CO_TOL_MU_RED": 1e-8,
    "INTPNT_CO_TOL_NEAR_REL": 1e+3,
    "INTPNT_CO_TOL_PFEAS": 1e-8,
    "INTPNT_CO_TOL_REL_GAP": 1e-7,
    "INTPNT_NL_MERIT_BAL": 1e-4,
    "INTPNT_NL_TOL_DFEAS": 1e-8,
    "INTPNT_NL_TOL_MU_RED": 1e-12,
    "INTPNT_NL_TOL_NEAR_REL": 1e+3,
    "INTPNT_NL_TOL_PFEAS": 1e-8,
    "INTPNT_NL_TOL_REL_GAP": 1e-6,
    "INTPNT_NL_TOL_REL_STEP": 9.95e-1,
    "INTPNT_QO_TOL_DFEAS": 1e-8,
    "INTPNT_QO_TOL_INFEAS": 1e-10,
    "INTPNT_QO_TOL_MU_RED": 1e-8,
    "INTPNT_QO_TOL_NEAR_REL": 1e+3,
    "INTPNT_QO_TOL_PFEAS": 1e-8,
    "INTPNT_QO_TOL_REL_GAP": 1e-8,
    "INTPNT_TOL_DFEAS": 1e-8,
    "INTPNT_TOL_DSAFE": 1e+0,
    "INTPNT_TOL_INFEAS": 1e-10,
    "INTPNT_TOL_MU_RED": 1e-16,
    "INTPNT_TOL_PATH": 1e-8,
    "INTPNT_TOL_PFEAS": 1e-8,
    "INTPNT_TOL_PSAFE": 1e+0,
    "INTPNT_TOL_REL_GAP": 1e-8,

```

```

    "INTPNT_TOL_REL_STEP":9.999e-1,
    "INTPNT_TOL_STEP_SIZE":1e-6,
    "LOWER_OBJ_CUT":-1e+30,
    "LOWER_OBJ_CUT_FINITE_TRH":-5e+29,
    "MIO_DISABLE_TERM_TIME":-1e+0,
    "MIO_MAX_TIME":-1e+0,
    "MIO_MAX_TIME_APRX_OPT":6e+1,
    "MIO_NEAR_TOL_ABS_GAP":0.0,
    "MIO_NEAR_TOL_REL_GAP":1e-3,
    "MIO_REL_GAP_CONST":1e-10,
    "MIO_TOL_ABS_GAP":0.0,
    "MIO_TOL_ABS_RELAX_INT":1e-5,
    "MIO_TOL_FEAS":1e-6,
    "MIO_TOL_REL_DUAL_BOUND_IMPROVEMENT":0.0,
    "MIO_TOL_REL_GAP":1e-4,
    "MIO_TOL_X":1e-6,
    "OPTIMIZER_MAX_TIME":-1e+0,
    "PRESOLVE_TOL_ABS_LINDEP":1e-6,
    "PRESOLVE_TOL_AIJ":1e-12,
    "PRESOLVE_TOL_REL_LINDEP":1e-10,
    "PRESOLVE_TOL_S":1e-8,
    "PRESOLVE_TOL_X":1e-8,
    "QCQO_REFORMULATE_REL_DROP_TOL":1e-15,
    "SEMIDEFINITE_TOL_APPROX":1e-10,
    "SIM_LU_TOL_REL_PIV":1e-2,
    "SIMPLEX_ABS_TOL_PIV":1e-7,
    "UPPER_OBJ_CUT":1e+30,
    "UPPER_OBJ_CUT_FINITE_TRH":5e+29
  },
  "sparam":{
    "BAS_SOL_FILE_NAME":"",
    "DATA_FILE_NAME":"examples/tools/data/lo1.mps",
    "DEBUG_FILE_NAME":"",
    "INT_SOL_FILE_NAME":"",
    "ITR_SOL_FILE_NAME":"",
    "MIO_DEBUG_STRING":"",
    "PARAM_COMMENT_SIGN":"%%",
    "PARAM_READ_FILE_NAME":"",
    "PARAM_WRITE_FILE_NAME":"",
    "READ_MPS_BOU_NAME":"",
    "READ_MPS_OBJ_NAME":"",
    "READ_MPS_RAN_NAME":"",
    "READ_MPS_RHS_NAME":"",
    "SENSITIVITY_FILE_NAME":"",
    "SENSITIVITY_RES_FILE_NAME":"",
    "SOL_FILTER_XC_LOW":"",
    "SOL_FILTER_XC_UPR":"",
    "SOL_FILTER_XX_LOW":"",
    "SOL_FILTER_XX_UPR":"",
    "STAT_FILE_NAME":"",
    "STAT_KEY":"",
    "STAT_NAME":"",
    "WRITE_LP_GEN_VAR_NAME":"XMSKGEN"
  }
}

```

## 12.8 The Solution File Format

MOSEK provides several solution files depending on the problem type and the optimizer used:

- *basis solution file* (extension `.bas`) if the problem is optimized using the simplex optimizer or basis identification is performed,
- *interior solution file* (extension `.sol`) if a problem is optimized using the interior-point optimizer and no basis identification is required,
- *integer solution file* (extension `.int`) if the problem contains integer constrained variables.

All solution files have the format:

NAME	: <problem name>							
PROBLEM STATUS	: <status of the problem>							
SOLUTION STATUS	: <status of the solution>							
OBJECTIVE NAME	: <name of the objective function>							
PRIMAL OBJECTIVE	: <primal objective value corresponding to the solution>							
DUAL OBJECTIVE	: <dual objective value corresponding to the solution>							
CONSTRAINTS								
INDEX	NAME	AT	ACTIVITY	LOWER LIMIT	UPPER LIMIT	DUAL LOWER	DUAL UPPER	
?	<name>	??	<a value>	<a value>	<a value>	<a value>	<a value>	
VARIABLES								
INDEX	NAME	AT	ACTIVITY	LOWER LIMIT	UPPER LIMIT	DUAL LOWER	DUAL UPPER	CONIC
↪DUAL								
?	<name>	??	<a value>	<a value>	<a value>	<a value>	<a value>	<a value>

In the example the fields ? and <> will be filled with problem and solution specific information. As can be observed a solution report consists of three sections, i.e.

- **HEADER** In this section, first the name of the problem is listed and afterwards the problem and solution status are shown. Next the primal and dual objective values are displayed.
- **CONSTRAINTS** For each constraint  $i$  of the form

$$l_i^c \leq \sum_{j=1}^n a_{ij}x_j \leq u_i^c, \quad (12.10)$$

the following information is listed:

- **INDEX**: A sequential index assigned to the constraint by **MOSEK**
- **NAME**: The name of the constraint assigned by the user.
- **AT**: The status of the constraint. In Table 12.4 the possible values of the status keys and their interpretation are shown.

Table 12.4: Status keys.

Status key	Interpretation
UN	Unknown status
BS	Is basic
SB	Is superbasic
LL	Is at the lower limit (bound)
UL	Is at the upper limit (bound)
EQ	Lower limit is identical to upper limit
**	Is infeasible i.e. the lower limit is greater than the upper limit.

- **ACTIVITY**: the quantity  $\sum_{j=1}^n a_{ij}x_j^*$ , where  $x^*$  is the value of the primal solution.
- **LOWER LIMIT**: the quantity  $l_i^c$  (see (12.10).)
- **UPPER LIMIT**: the quantity  $u_i^c$  (see (12.10).)
- **DUAL LOWER**: the dual multiplier corresponding to the lower limit on the constraint.
- **DUAL UPPER**: the dual multiplier corresponding to the upper limit on the constraint.

- **VARIABLES** The last section of the solution report lists information about the variables. This information has a similar interpretation as for the constraints. However, the column with the header CONIC DUAL is included for problems having one or more conic constraints. This column shows the dual variables corresponding to the conic constraints.

**Example:** lo1.sol

In Listing 12.7 we show the solution file for the lo1.opf problem.

Listing 12.7: An example of .sol file.

NAME	:				
PROBLEM STATUS	:	PRIMAL_AND_DUAL_FEASIBLE			
SOLUTION STATUS	:	OPTIMAL			
OBJECTIVE NAME	:	obj			
PRIMAL OBJECTIVE	:	8.3333333e+01			
DUAL OBJECTIVE	:	8.3333332e+01			
CONSTRAINTS					
INDEX	NAME	AT ACTIVITY	LOWER LIMIT	UPPER LIMIT	
	→DUAL LOWER	DUAL UPPER			
0	c1	EQ 3.00000000000000e+01	3.00000000e+01	3.00000000e+01	-0.
	→00000000000000e+00	-2.4999999741654e+00			
1	c2	SB 5.3333333049188e+01	1.50000000e+01	NONE	2.
	→09157603759397e-10	-0.00000000000000e+00			
2	c3	UL 2.4999999842049e+01	NONE	2.50000000e+01	-0.
	→00000000000000e+00	-3.3333332895110e-01			
VARIABLES					
INDEX	NAME	AT ACTIVITY	LOWER LIMIT	UPPER LIMIT	
	→DUAL LOWER	DUAL UPPER			
0	x1	LL 1.67020427073508e-09	0.00000000e+00	NONE	-4.
	→49999999528055e+00	-0.00000000000000e+00			
1	x2	LL 2.93510446280504e-09	0.00000000e+00	1.00000000e+01	-2.
	→16666666494916e+00	6.20863861687316e-10			
2	x3	SB 1.4999999899425e+01	0.00000000e+00	NONE	-8.
	→79123177454657e-10	-0.00000000000000e+00			
3	x4	SB 8.3333332273116e+00	0.00000000e+00	NONE	-1.
	→69795978899185e-09	-0.00000000000000e+00			

## INTERFACE CHANGES

The section show interface-specific changes to the **MOSEK** Command Line Tools in version 8. See the [release notes](#) for general changes and new features of the **MOSEK** Optimization Suite.

### 13.1 Compatibility

### 13.2 Parameters

#### Added

- *MSK\_DPAR\_DATA\_SYM\_MAT\_TOL*
- *MSK\_DPAR\_DATA\_SYM\_MAT\_TOL\_HUGE*
- *MSK\_DPAR\_DATA\_SYM\_MAT\_TOL\_LARGE*
- *MSK\_DPAR\_INTPNT\_QO\_TOL\_DFEAS*
- *MSK\_DPAR\_INTPNT\_QO\_TOL\_INFEAS*
- *MSK\_DPAR\_INTPNT\_QO\_TOL\_MU\_RED*
- *MSK\_DPAR\_INTPNT\_QO\_TOL\_NEAR\_REL*
- *MSK\_DPAR\_INTPNT\_QO\_TOL\_PFEAS*
- *MSK\_DPAR\_INTPNT\_QO\_TOL\_REL\_GAP*
- *MSK\_DPAR\_SEMIDEFINITE\_TOL\_APPROX*
- *MSK\_IPAR\_INTPNT\_MULTI\_THREAD*
- *MSK\_IPAR\_LICENSE\_TRH\_EXPIRY\_WRN*
- *MSK\_IPAR\_LOG\_ANA\_PRO*
- *MSK\_IPAR\_MIO\_CUT\_CLIQUE*
- *MSK\_IPAR\_MIO\_CUT\_GMI*
- *MSK\_IPAR\_MIO\_CUT\_IMPLIED\_BOUND*
- *MSK\_IPAR\_MIO\_CUT\_KNAPSACK\_COVER*
- *MSK\_IPAR\_MIO\_CUT\_SELECTION\_LEVEL*
- *MSK\_IPAR\_MIO\_PERSPECTIVE\_REFORMULATE*
- *MSK\_IPAR\_MIO\_ROOT\_REPEAT\_PREOLVE\_LEVEL*
- *MSK\_IPAR\_MIO\_VB\_DETECTION\_LEVEL*
- *MSK\_IPAR\_PREOLVE\_ELIMINATOR\_MAX\_FILL*

## Removed

- MSK\_DPAR\_FEASREPAIR\_TOL
- MSK\_DPAR\_MIO\_HEURISTIC\_TIME
- MSK\_DPAR\_MIO\_MAX\_TIME\_APRX\_OPT
- MSK\_DPAR\_MIO\_REL\_ADD\_CUT\_LIMITED
- MSK\_DPAR\_MIO\_TOL\_MAX\_CUT\_FRAC\_RHS
- MSK\_DPAR\_MIO\_TOL\_MIN\_CUT\_FRAC\_RHS
- MSK\_DPAR\_MIO\_TOL\_REL\_RELAX\_INT
- MSK\_DPAR\_MIO\_TOL\_X
- MSK\_DPAR\_NONCONVEX\_TOL\_FEAS
- MSK\_DPAR\_NONCONVEX\_TOL\_OPT
- MSK\_IPAR\_ALLOC\_ADD\_QNZ
- MSK\_IPAR\_CONCURRENT\_NUM\_OPTIMIZERS
- MSK\_IPAR\_CONCURRENT\_PRIORITY\_DUAL\_SIMPLEX
- MSK\_IPAR\_CONCURRENT\_PRIORITY\_FREE\_SIMPLEX
- MSK\_IPAR\_CONCURRENT\_PRIORITY\_INTPNT
- MSK\_IPAR\_CONCURRENT\_PRIORITY\_PRIMAL\_SIMPLEX
- MSK\_IPAR\_FEASREPAIR\_OPTIMIZE
- MSK\_IPAR\_INTPNT\_FACTOR\_DEBUG\_LVL
- MSK\_IPAR\_INTPNT\_FACTOR\_METHOD
- MSK\_IPAR\_LIC\_TRH\_EXPIRY\_WRN
- MSK\_IPAR\_LOG\_CONCURRENT
- MSK\_IPAR\_LOG\_NONCONVEX
- MSK\_IPAR\_LOG\_PARAM
- MSK\_IPAR\_LOG\_SIM\_NETWORK\_FREQ
- MSK\_IPAR\_MIO\_BRANCH\_PRIORITIES\_USE
- MSK\_IPAR\_MIO\_CONT\_SOL
- MSK\_IPAR\_MIO\_CUT\_CG
- MSK\_IPAR\_MIO\_CUT\_LEVEL\_ROOT
- MSK\_IPAR\_MIO\_CUT\_LEVEL\_TREE
- MSK\_IPAR\_MIO\_FEASPUMP\_LEVEL
- MSK\_IPAR\_MIO\_HOTSTART
- MSK\_IPAR\_MIO\_KEEP\_BASIS
- MSK\_IPAR\_MIO\_LOCAL\_BRANCH\_NUMBER
- MSK\_IPAR\_MIO\_OPTIMIZER\_MODE
- MSK\_IPAR\_MIO\_PRESOLVE\_AGGREGATE
- MSK\_IPAR\_MIO\_PRESOLVE\_PROBING
- MSK\_IPAR\_MIO\_PRESOLVE\_USE



- `MSK_IPAR_MIO_STRONG_BRANCH`
- `MSK_IPAR_MIO_USE_MULTITHREADED_OPTIMIZER`
- `MSK_IPAR_NONCONVEX_MAX_ITERATIONS`
- `MSK_IPAR_PRESOLVE_ELIM_FILL`
- `MSK_IPAR_PRESOLVE_ELIMINATOR_USE`
- `MSK_IPAR_QO_SEPARABLE_REFORMULATION`
- `MSK_IPAR_READ_ANZ`
- `MSK_IPAR_READ_CON`
- `MSK_IPAR_READ_CONE`
- `MSK_IPAR_READ_MPS_KEEP_INT`
- `MSK_IPAR_READ_MPS_OBJ_SENSE`
- `MSK_IPAR_READ_MPS_RELAX`
- `MSK_IPAR_READ_QNZ`
- `MSK_IPAR_READ_VAR`
- `MSK_IPAR_WARNING_LEVEL`
- `MSK_IPAR_WRITE_IGNORE_INCOMPATIBLE_CONIC_ITEMS`
- `MSK_IPAR_WRITE_IGNORE_INCOMPATIBLE_NL_ITEMS`
- `MSK_IPAR_WRITE_IGNORE_INCOMPATIBLE_PSD_ITEMS`
- `MSK_SPAR_FEASREPAIR_NAME_PREFIX`
- `MSK_SPAR_FEASREPAIR_NAME_SEPARATOR`
- `MSK_SPAR_FEASREPAIR_NAME_WSUMVIOL`

## 13.3 Constants

### Added

- *`MSK_BRANCH_DIR_FAR`*
- *`MSK_BRANCH_DIR_GUIDED`*
- *`MSK_BRANCH_DIR_NEAR`*
- *`MSK_BRANCH_DIR_PSEUDOCOST`*
- *`MSK_BRANCH_DIR_ROOT_LP`*
- *`MSK_CALLBACK_BEGIN_ROOT_CUTGEN`*
- *`MSK_CALLBACK_BEGIN_TO_CONIC`*
- *`MSK_CALLBACK_END_ROOT_CUTGEN`*
- *`MSK_CALLBACK_END_TO_CONIC`*
- *`MSK_CALLBACK_IM_ROOT_CUTGEN`*
- *`MSK_CALLBACK_SOLVING_REMOTE`*
- *`MSK_DATA_FORMAT_JSON_TASK`*
- *`MSK_DINF_MIO_CLIQUÉ_SEPARATION_TIME`*

- *MSK\_DINF\_MIO\_CMIR\_SEPARATION\_TIME*
- *MSK\_DINF\_MIO\_GMI\_SEPARATION\_TIME*
- *MSK\_DINF\_MIO\_IMPLIED\_BOUND\_TIME*
- *MSK\_DINF\_MIO\_KNAPSACK\_COVER\_SEPARATION\_TIME*
- *MSK\_DINF\_QCQO\_REFORMULATE\_MAX\_PERTURBATION*
- *MSK\_DINF\_QCQO\_REFORMULATE\_WORST\_CHOLESKY\_COLUMN\_SCALING*
- *MSK\_DINF\_QCQO\_REFORMULATE\_WORST\_CHOLESKY\_DIAG\_SCALING*
- *MSK\_DINF\_SOL\_BAS\_NRM\_BARX*
- *MSK\_DINF\_SOL\_BAS\_NRM\_SLC*
- *MSK\_DINF\_SOL\_BAS\_NRM\_SLX*
- *MSK\_DINF\_SOL\_BAS\_NRM\_SUC*
- *MSK\_DINF\_SOL\_BAS\_NRM\_SUX*
- *MSK\_DINF\_SOL\_BAS\_NRM\_XC*
- *MSK\_DINF\_SOL\_BAS\_NRM\_XX*
- *MSK\_DINF\_SOL\_BAS\_NRM\_Y*
- *MSK\_DINF\_SOL\_ITG\_NRM\_BARX*
- *MSK\_DINF\_SOL\_ITG\_NRM\_XC*
- *MSK\_DINF\_SOL\_ITG\_NRM\_XX*
- *MSK\_DINF\_SOL\_ITR\_NRM\_BARS*
- *MSK\_DINF\_SOL\_ITR\_NRM\_BARX*
- *MSK\_DINF\_SOL\_ITR\_NRM\_SLC*
- *MSK\_DINF\_SOL\_ITR\_NRM\_SLX*
- *MSK\_DINF\_SOL\_ITR\_NRM\_SNX*
- *MSK\_DINF\_SOL\_ITR\_NRM\_SUC*
- *MSK\_DINF\_SOL\_ITR\_NRM\_SUX*
- *MSK\_DINF\_SOL\_ITR\_NRM\_XC*
- *MSK\_DINF\_SOL\_ITR\_NRM\_XX*
- *MSK\_DINF\_SOL\_ITR\_NRM\_Y*
- *MSK\_DINF\_TO\_CONIC\_TIME*
- *MSK\_IINF\_MIO\_ABSGAP\_SATISFIED*
- *MSK\_IINF\_MIO\_CLIQUETABLE\_SIZE*
- *MSK\_IINF\_MIO\_NEAR\_ABSGAP\_SATISFIED*
- *MSK\_IINF\_MIO\_NEAR\_RELGAP\_SATISFIED*
- *MSK\_IINF\_MIO\_NODE\_DEPTH*
- *MSK\_IINF\_MIO\_NUM\_CMIR\_CUTS*
- *MSK\_IINF\_MIO\_NUM\_IMPLIED\_BOUND\_CUTS*
- *MSK\_IINF\_MIO\_NUM\_KNAPSACK\_COVER\_CUTS*
- *MSK\_IINF\_MIO\_NUM\_REPEATED\_PRESOLVE*
- *MSK\_IINF\_MIO\_PRESOLVED\_NUMBIN*

- *MSK\_IINF\_MIO\_PRE SOLVED\_NUMCON*
- *MSK\_IINF\_MIO\_PRE SOLVED\_NUMCONT*
- *MSK\_IINF\_MIO\_PRE SOLVED\_NUMINT*
- *MSK\_IINF\_MIO\_PRE SOLVED\_NUMVAR*
- *MSK\_IINF\_MIO\_RELGAP\_SATISFIED*
- *MSK\_LIINF\_MIO\_PRE SOLVED\_ANZ*
- *MSK\_LIINF\_MIO\_SIM\_MAXITER\_SETBACKS*
- *MSK\_MPS\_FORMAT\_CPLEX*
- *MSK\_SOL\_STA\_DUAL\_ILLPOSED\_CER*
- *MSK\_SOL\_STA\_PRIM\_ILLPOSED\_CER*

### Changed

- *MSK\_SOL\_STA\_INTEGER\_OPTIMAL*
- *MSK\_SOL\_STA\_NEAR\_INTEGER\_OPTIMAL*
- *MSK\_LICENSE\_BUFFER\_LENGTH*

### Removed

- *MSK\_CALLBACKCODE\_BEGIN\_CONCURRENT*
- *MSK\_CALLBACKCODE\_BEGIN\_NETWORK\_DUAL\_SIMPLEX*
- *MSK\_CALLBACKCODE\_BEGIN\_NETWORK\_PRIMAL\_SIMPLEX*
- *MSK\_CALLBACKCODE\_BEGIN\_NETWORK\_SIMPLEX*
- *MSK\_CALLBACKCODE\_BEGIN\_NONCONVEX*
- *MSK\_CALLBACKCODE\_BEGIN\_SIMPLEX\_NETWORK\_DETECT*
- *MSK\_CALLBACKCODE\_END\_CONCURRENT*
- *MSK\_CALLBACKCODE\_END\_NETWORK\_DUAL\_SIMPLEX*
- *MSK\_CALLBACKCODE\_END\_NETWORK\_PRIMAL\_SIMPLEX*
- *MSK\_CALLBACKCODE\_END\_NETWORK\_SIMPLEX*
- *MSK\_CALLBACKCODE\_END\_NONCONVEX*
- *MSK\_CALLBACKCODE\_END\_SIMPLEX\_NETWORK\_DETECT*
- *MSK\_CALLBACKCODE\_IM\_MIO\_PRE SOLVE*
- *MSK\_CALLBACKCODE\_IM\_NETWORK\_DUAL\_SIMPLEX*
- *MSK\_CALLBACKCODE\_IM\_NETWORK\_PRIMAL\_SIMPLEX*
- *MSK\_CALLBACKCODE\_IM\_NONCONVEX*
- *MSK\_CALLBACKCODE\_NONCOVEX*
- *MSK\_CALLBACKCODE\_UPDATE\_NETWORK\_DUAL\_SIMPLEX*
- *MSK\_CALLBACKCODE\_UPDATE\_NETWORK\_PRIMAL\_SIMPLEX*
- *MSK\_CALLBACKCODE\_UPDATE\_NONCONVEX*
- *MSK\_DINFITEM\_CONCURRENT\_TIME*

- MSK\_DINFITEM\_MIO\_CG\_SEPERATION\_TIME
- MSK\_DINFITEM\_MIO\_CMIR\_SEPERATION\_TIME
- MSK\_DINFITEM\_SIM\_NETWORK\_DUAL\_TIME
- MSK\_DINFITEM\_SIM\_NETWORK\_PRIMAL\_TIME
- MSK\_DINFITEM\_SIM\_NETWORK\_TIME
- MSK\_FEATURE\_PTOM
- MSK\_FEATURE\_PTOX
- MSK\_IINFITEM\_CONCURRENT\_FASTEST\_OPTIMIZER
- MSK\_IINFITEM\_MIO\_NUM\_BASIS\_CUTS
- MSK\_IINFITEM\_MIO\_NUM\_CARDGUB\_CUTS
- MSK\_IINFITEM\_MIO\_NUM\_COEF\_REDC\_CUTS
- MSK\_IINFITEM\_MIO\_NUM\_CONTRA\_CUTS
- MSK\_IINFITEM\_MIO\_NUM\_DISAGG\_CUTS
- MSK\_IINFITEM\_MIO\_NUM\_FLOW\_COVER\_CUTS
- MSK\_IINFITEM\_MIO\_NUM\_GCD\_CUTS
- MSK\_IINFITEM\_MIO\_NUM\_GUB\_COVER\_CUTS
- MSK\_IINFITEM\_MIO\_NUM\_KNAPSUR\_COVER\_CUTS
- MSK\_IINFITEM\_MIO\_NUM\_LATTICE\_CUTS
- MSK\_IINFITEM\_MIO\_NUM\_LIFT\_CUTS
- MSK\_IINFITEM\_MIO\_NUM\_OBJ\_CUTS
- MSK\_IINFITEM\_MIO\_NUM\_PLAN\_LOC\_CUTS
- MSK\_IINFITEM\_SIM\_NETWORK\_DUAL\_DEG\_ITER
- MSK\_IINFITEM\_SIM\_NETWORK\_DUAL\_HOTSTART
- MSK\_IINFITEM\_SIM\_NETWORK\_DUAL\_HOTSTART\_LU
- MSK\_IINFITEM\_SIM\_NETWORK\_DUAL\_INF\_ITER
- MSK\_IINFITEM\_SIM\_NETWORK\_DUAL\_ITER
- MSK\_IINFITEM\_SIM\_NETWORK\_PRIMAL\_DEG\_ITER
- MSK\_IINFITEM\_SIM\_NETWORK\_PRIMAL\_HOTSTART
- MSK\_IINFITEM\_SIM\_NETWORK\_PRIMAL\_HOTSTART\_LU
- MSK\_IINFITEM\_SIM\_NETWORK\_PRIMAL\_INF\_ITER
- MSK\_IINFITEM\_SIM\_NETWORK\_PRIMAL\_ITER
- MSK\_IINFITEM\_SOL\_INT\_PROSTA
- MSK\_IINFITEM\_SOL\_INT\_SOLSTA
- MSK\_IINFITEM\_STO\_NUM\_A\_CACHE\_FLUSHES
- MSK\_IINFITEM\_STO\_NUM\_A\_TRANSPOSES
- MSK\_MIOMODE\_LAZY
- MSK\_OPTIMIZERTYPE\_CONCURRENT
- MSK\_OPTIMIZERTYPE\_MIXED\_INT\_CONIC
- MSK\_OPTIMIZERTYPE\_NETWORK\_PRIMAL\_SIMPLEX

- `MSK_OPTIMIZERTYPE_NONCONVEX`
- `MSK_OPTIMIZERTYPE_PRIMAL_DUAL_SIMPLEX`

## 13.4 Response Codes

### Added

- `MSK_RES_ERR_DUPLICATE_AIJ (1385)`
- `MSK_RES_ERR_JSON_DATA (1179)`
- `MSK_RES_ERR_JSON_FORMAT (1178)`
- `MSK_RES_ERR_JSON_MISSING_DATA (1180)`
- `MSK_RES_ERR_JSON_NUMBER_OVERFLOW (1177)`
- `MSK_RES_ERR_JSON_STRING (1176)`
- `MSK_RES_ERR_JSON_SYNTAX (1175)`
- `MSK_RES_ERR_LAU_INVALID_LOWER_TRIANGULAR_MATRIX (7002)`
- `MSK_RES_ERR_LAU_INVALID_SPARSE_SYMMETRIC_MATRIX (7019)`
- `MSK_RES_ERR_LAU_NOT_POSITIVE_DEFINITE (7001)`
- `MSK_RES_ERR_MIXED_CONIC_AND_NL (1501)`
- `MSK_RES_ERR_SERVER_CONNECT (8000)`
- `MSK_RES_ERR_SERVER_PROTOCOL (8001)`
- `MSK_RES_ERR_SERVER_STATUS (8002)`
- `MSK_RES_ERR_SERVER_TOKEN (8003)`
- `MSK_RES_ERR_SYM_MAT_HUGE (1482)`
- `MSK_RES_ERR_SYM_MAT_INVALID (1480)`
- `MSK_RES_ERR_TASK_WRITE (2562)`
- `MSK_RES_ERR_TOCONIC_CONSTR_NOT_CONIC (7153)`
- `MSK_RES_ERR_TOCONIC_CONSTR_Q_NOT_PSD (7150)`
- `MSK_RES_ERR_TOCONIC_CONSTRAINT_FX (7151)`
- `MSK_RES_ERR_TOCONIC_CONSTRAINT_RA (7152)`
- `MSK_RES_ERR_TOCONIC_OBJECTIVE_NOT_PSD (7155)`
- `MSK_RES_WRN_SYM_MAT_LARGE (960)`

### Removed

- `MSK_RES_ERR_AD_INVALID_OPERAND`
- `MSK_RES_ERR_AD_INVALID_OPERATOR`
- `MSK_RES_ERR_AD_MISSING_OPERAND`
- `MSK_RES_ERR_AD_MISSING_RETURN`
- `MSK_RES_ERR_CONCURRENT_OPTIMIZER`
- `MSK_RES_ERR_INV_CONIC_PROBLEM`

- MSK\_RES\_ERR\_INVALID\_BRANCH\_DIRECTION
- MSK\_RES\_ERR\_INVALID\_BRANCH\_PRIORITY
- MSK\_RES\_ERR\_INVALID\_NETWORK\_PROBLEM
- MSK\_RES\_ERR\_MBT\_INCOMPATIBLE
- MSK\_RES\_ERR\_MBT\_INVALID
- MSK\_RES\_ERR\_MIXED\_PROBLEM
- MSK\_RES\_ERR\_NO\_DUAL\_INFO\_FOR\_ITG\_SOL
- MSK\_RES\_ERR\_ORD\_INVALID
- MSK\_RES\_ERR\_ORD\_INVALID\_BRANCH\_DIR
- MSK\_RES\_ERR\_TOCONIC\_CONVERSION\_FAIL
- MSK\_RES\_ERR\_TOO\_MANY\_CONCURRENT\_TASKS
- MSK\_RES\_WRN\_TOO\_MANY\_THREADS\_CONCURRENT

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